An energy harvester for low frequency electrical signals

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/(Optional Dedication)/

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Generating electricity from low frequency mechanical agitations produced by ocean waves, plants,
or human motion is emerging as a key, environmentally-friendly technology in combating harmful
emissions caused by burning fossil fuels. The generated electric pulses by the appropriate
transducers, such as triboelectric or piezoelectric generators, need to be rectified and stored in a
sustainable external circuit. The bottleneck, however, is the harvesting circuitry, which mostly
relies on rather expensive up-conversion oscillation technologies. Such circuits are primarily
designed and optimized for frequencies well-above the kHz range, much higher than the
described and optimized for frequencies well-above the kHz range, much higher than the
aforementioned mechanical stimuli, and are therefore energy demanding. Here, we have developed
a sustainable energy harvester that alleviates the need for using up-conversion and allows for
efficient harvesting of the energy from low-frequency voltage pulses, as the ones typically
generated by triboelectric or piezoelectric generators. Our resonant circuit has been designed to
match the overall response originating from such low-frequency oscillating energy sources. Our
design enables the harvester to be operable at frequencies as low as 1 Hz. We demonstrate CAD
simulations, a miniaturized harvester on a printed-circuit-board using low-cost components, and
discuss the scalability of the proposed design, which paves the way to affordable, efficient and
sustainable low-cost energy solutions.

1. Introduction
Alternative renewable energy sources seek to scavenge various forms of energy from the
environment.\textsuperscript{[1]} Established renewable-based energy technologies driven by natural energy, such as
wind\textsuperscript{[2]} and solar\textsuperscript{[3]}, are key approaches towards decarbonizing our energy system.\textsuperscript{[4]} However, the
intermittent output of these sources is incompatible with energy consumers’ needs. Even when
state-of-the-art energy storage solutions become available, the energy system would still require
substantial fossil-based generation as a back-up.\textsuperscript{[5]} Hence, to overcome the limitation of
intermittency and the overwhelming dependence on fossil-based energy generation, new sources,
such as triboelectric and piezoelectric generators, are emerging, as discussed extensively in the
seminal work of Wang.\textsuperscript{[6]} These environmentally-friendly generators convert the low-frequency
mechanical agitations from ocean waves\textsuperscript{[2e, 7]} or human motion\textsuperscript{[8]} into low-frequency alternating
electric signals for energy harvesters.\textsuperscript{[9]} Although the average signal frequency feeding the harvester
is about 1 Hz, the wave’s unpredictable and non-periodic nature can lead to intervals ranging from
0.3 Hz to 300 Hz.\textsuperscript{[7a, 7b, 10]} The low output power varies from 700 $\mu$W to 20 mW.\textsuperscript{[7a, 7b, 10a, 10b]}
Scalable and efficient circuits to interface with low-frequency generators and increase output power are therefore needed.\textsuperscript{[11]}

Furthermore, plants have also been reported to produce oscillating and low-frequency electrical signals. The electric double layer formed by an insulating plant leaf cuticle (from a Rhododendron) and the adjacent conductive cellular tissue has been shown to possess triboelectric properties, where the low-frequency and alternating output power on a single leaf, upon a given force (0.9 N) reached about 15 $\mu$W cm\(^{-2}\). Lab-scale set-ups in whole plants are producing an output power between 200 mW m\(^{-2}\) and 500 mW m\(^{-2}\).\textsuperscript{[12]} The alternating output power in plants has been reported to oscillate between 0.01 Hz and 10 Hz.\textsuperscript{[13]} In fact, microscopically, the existence of electrically excitable plants associated with environmental stress and stimuli has been investigated, even when no external force is applied. Plants such as Mimosa pudica, Helianthus annuus or Dionaea muscipula make use of ion channels to transmit information over long distances.\textsuperscript{[14]} Plants, themselves, translate external stimuli into electrical signals,\textsuperscript{[13-14]} as a survival mechanism\textsuperscript{[15]} and communication strategy.\textsuperscript{[16]} In resemblance to an electrical conducting cable, ion gradients across the plant tissue rapidly convey signals over long distances.\textsuperscript{[16a, 17]} Hence, plants communicate electrically,\textsuperscript{[18]} via alternating, long lasting and low-frequency signals.

Harvesting energy from low-frequency sources, particularly in the Hz regime, is technically challenging. State-of-the-art solutions to harvest low-frequency signals mostly rely on mechanical structure designs,\textsuperscript{[8b, 8i, 19]} where up-conversion oscillation technologies play an important role. Several up-conversion methodologies that convert low-frequency ambient vibrations to higher frequency oscillations via a piezoelectric beam generator have been developed.\textsuperscript{[20]} Yet, these technologies tend to be expensive to manufacture, and unreliable in the long term due to cantilever
impact degradation.[20] The up-conversion process itself is prone to energy losses, which are detrimental to the output power efficiency.

In this work, we have developed a technology to harvest energy from low-frequency sources, eliminating the need for up-conversion techniques. The resonant circuit frequency of our harvester has been modelled and matched to the low-frequency oscillating energy source. We demonstrate an energy harvester prototype, based on an optimized LTC3108 on a miniaturized PCB, which comprises a step-up transformer and a boost converter, to condition and harvest the alternating signals prevenient from a low-frequency pulse train. All considered, this work paves the way for efficient energy harvesting circuits from a variety of low-frequency, green energy sources.

2. Experimental

The energy harvester PCB prototype depicted in Figure 1(a) was designed by using the electronic design automation tool Altium Designer 18.1.7. To minimize the PCB size, the surface-mount variant of all necessary electronic components was selected. PCB trace dimensions were determined using the IPC-2221 standard.[21] PCBs were fabricated using 35 μm copper thickness and 1.6 mm of glass re-enforced Fr-4. The PCB was populated with a Coilcraft LPR6235-752SMR transformer, with a primary inductance of 7.5 μH, a measured secondary coil inductance of 63.56 mH and an inter-winding capacitance of 62.8 pF. The boost converter used was the LTC3108 from Analog Devices, with an SSOP16 footprint and buffer with reference MAX9650. The LTC3108 peripheral capacitors, namely \( C_{\text{res}} \), \( C_{\text{cp}} \) and \( C_{\text{byp}} \), used SMD 0805 footprints. The capacitance values were 10 μF, 620 pF and 2.2 μF, respectively. A polarized tantalum SMD capacitor from AVX, with a value of 1000 μF, was employed as the storage capacitor, \( C_{\text{store}} \). The integrated circuit uses a charge pump approach to power conversion and has been implemented in a PCB. The schematic of the complete circuit is given in Supplementary Figure S1. The miniaturized circuit has a total area of less than 9
cm². Inductance and capacitance measurements were performed using a TENMA 72-10465 LCR Meter.

All simulations were performed using the LTspice® and Saber™ software suites. Small-signal analysis was simulated in Saber™ using a 50 mV peak voltage input. The output voltage over time was simulated using the behavioural model in the time domain, utilizing a 1 Hz pulse train.

The experimental characterization of the PCB prototype was carried out using a 33210A Pulse Generator, from Keysight Technologies, with a programmed input stimulus in the form of periodic square wave pulses, or pulse train. The schematic of the circuit used to determine the V-I power curve is depicted in Figure 1(b). The minimum voltage, current and power required for the harvester to operate, was determined by setting the signal generator to output a 1 Hz, 50 % duty cycle square wave with a 20 Ohm internal load. Varying the resistance of the potentiometer, $R_p$, then results in the power curve shown in Figure 1(c). The input power was calculated as:

$$P = \frac{1}{2} \cdot V \cdot I$$

Figure 1(c) shows that for the targeted low frequency input of 1 Hz square pulses, the circuit requires a minimum input power of 180 $\mu$W, which corresponds to a minimum voltage magnitude of 36 mV. The optimized harvester topology and circuit parameters leading to the power curve depicted in Figure 1(c) are explained in the next sections.

3. Results

3.1. Resonant Circuit

The energy harvester comprises a resonant circuit and a state-of-the-art LTC3108 boost converter, for harvesting energy from an ultra-low input voltage source, below 50 mV. Typically, resonant circuits focus on harvesting high-frequency signals, in the kHz regime. Conventional ranges are...
essentially between 10 kHz and 100 kHz. The resonant circuit used with the LTC3108 is depicted in Figure 2(a). The low-frequency input signal, $V_{\text{res-in}}$, is fed into the resonant circuit through a load impedance stabilizer, constructed by MAX9650. The resonant circuit includes the internal N-Channel MOSFET switch of the LTC3108, the inductance of the secondary winding of the transformer, $L_{\text{sec}}$, and the input capacitance, $C_{\text{res}}$. In order to form a close-loop and stabilize the circuit, the primary winding of the transformer is connected to the drain of the N-Channel MOSFET, namely the SW pin, as suggested by the manufacturer.\(^{[22]}\)

The resonant circuit uses an external step-up transformer with a turn’s ratio of 100, in order to increase the voltage. The frequency of oscillation, $f_{\text{res}}$, is determined by $L_{\text{sec}}$ and $C_{\text{res}}$. The oscillation frequency\(^{[22]}\) and relation between the $L_{\text{sec}}$ and $C_{\text{res}}$ is given by Equation 2:

$$f_{\text{res}} = \frac{1}{2\pi \cdot \sqrt{L_{\text{sec}} \cdot C_{\text{res}}}} \Leftrightarrow C_{\text{res}} = \frac{1}{f_{\text{res}}^2 \cdot 4\pi^2 \cdot L_{\text{sec}}} \tag{2}$$

### 3.2. Boost Converter

The architecture of the LTC3108 is shown in Figure 2(b) and in more detail in Supplementary Figure S1. The output voltage from the resonant circuit stage ($V_{\text{res-out}}$) can be coupled to the charge-pump and rectifier circuit inside the LTC3108, using the capacitor $C_{\text{cp}}$. This enables the output voltage to be harvested. The output voltage of the LTC3108 is configured to be 3.1 V by connecting pin $V_{\text{S1}}$ to VAUX, $V_{\text{S2}}$ to ground and bypassing the VAUX by a 2.2 $\mu$F capacitor $C_{\text{byp}}$. An energy storage capacitor $C_{\text{out}}$ is used to store the output energy. Another large capacitor, $C_{\text{store}}$, is also connected from pin $V_{\text{store}}$ to ground, to power the system in the event the input voltage is lost. This capacitor will be charged to the maximum VAUX clamp voltage, which is 3.1 V for this design. We note that the energy harvester used in this work was designed to provide an output voltage up to 3.1 V; the integrated circuit can also be configured to provide a programmable target output of 2.5 V, 4.1 V or 5.0 V.

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Considering both the input power level from triboelectric generators and the design requirements of the energy harvesting circuit, the value of capacitors $C_{\text{byp}}$, $C_{\text{out}}$ and $C_{\text{store}}$ were chosen as 2.2 $\mu$F, 220 $\mu$F and 1000 $\mu$F, respectively.

### 3.3. Low Frequency Matching

The frequency of the signals generated by triboelectric generators and plants is typically in the range of a few Hz. To allow the electronics to decode and efficiently harvest such low-frequency signals, the resonant circuit needs to be designed to match the overall response originating from these low-frequency oscillating energy sources.

There is a constraint on the circuit resonant component that needs to be taken into account. The value of the secondary inductance has an upper limit, due to a practical size limitation of the inductor with increasing number of turns. Moreover, the concomitant increase in winding resistance would introduce a high level of loss into the circuit. Given this constraint, the value of $L_{\text{sec}}$ was chosen and measured to be 63 mH. This value is based on a primary theoretical inductance of 7.5 $\mu$H and a turn’s ratio of 1:100. Note that it is not unusual for tolerances of 10-20 % to occur in magnetic components due to the intrinsic variability of the permeability of the magnetic material in the core.

The signal frequency generated by triboelectric sources, including plants, varies between 0.3 Hz and 300 Hz$^{[7a, 7b, 10]}$. Assuming a resonant frequency of 200 Hz, Equation 2 leads to a $C_{\text{res}}$ of 10 $\mu$F. Therefore, this value was used instead of the 330 pF, mentioned in the application example described in the LTC3108 datasheet, henceforth referred to as “default”.

Empirical testing of the energy harvesting circuit established that the capacitance value of the input capacitor for the energy harvesting circuit, $C_{\text{cp}}$, is proportional to the one of the resonant capacitor,
$C_{\text{res}}$. It should therefore be similarly scaled, resulting in a desired value of 680 pF. However, we need to consider the parallel inter-winding parasitic capacitance of 62.8 pF, which needs to be subtracted from the scaled $C_{cp}$. Hence, the final value of $C_{cp}$ was set to 620 pF, which is the nearest standard value to the desired 617.2 pF.

3.4. Simulation and Experimental Validation of the Frequency Matching Effect

To understand the effect of $C_{\text{res}}$ and $L_{\text{sec}}$ on the resonant frequency, we performed a simulation analysis using a small-signal model. Note that we did not use switching electronics to enable small-signal frequency analysis, instead we used an averaged model of the boost converter that allows direct frequency analysis.\[23\] The small-signal model used is a linearized power switch model of the form described by Middlebrook,\[23b\] which is established as a method for obtaining accurate frequency responses of switching power regulators. The model uses an averaged model of the power-switching stage to obtain a linear model that reflects the overall frequency domain behaviour of the power converter. The model is linear in nature and can, therefore, be used to calculate the small-signal frequency response directly, without the need for non-linear algorithms, such as Newton-Raphson. It is also common to express the output in decibels (dB), rather than in absolute voltage. For unity gain, the resulting output would be 1 V or 0 dB. Therefore, positive gain is larger than 0 dB and negative gain is smaller than 0 dB.

Simulations were carried out to establish a suitable set of circuit parameters, ensuring the optimal compromise between circuit efficiency and availability of hardware. As discussed in the low frequency matching section, the optimum value for the secondary inductance and capacitance of the resonant circuit, are approximately 63 mH and 10 µF, respectively.

To optimize the energy harvester circuit, we performed a frequency response analysis, while tuning the transformer primary inductance, $L_p$. In Figure 3(a) we show gain as a function of frequency for
different values of the inductance, ranging between 75 nH and 7.5 µH, while using the default value, 330 pF, for \( C_{\text{res}} \). A shift from \( 10^2 \) Hz to \( 10^0 \) Hz, for 0 dB is observed. An improved performance over the frequency range from 0.3 Hz to 300 Hz is notable, albeit with a gain still attenuated at low frequencies. We can conclude that simply using the default value for the boost converter, \( \text{viz. } C_{\text{res}} = 330 \text{ pF and } L_p = 75 \text{ nH}, \) does not yield an effective response, as the gain is negative in the low frequency regime. We therefore performed, in Figure 3(b), the small-signal simulation as a function of the other resonant parameter, \( C_{\text{res}} \). The inductance, \( L_p \), was fixed to 7.5 µH. The resonant parameter \( C_{\text{res}} \) was varied from the default value of 330 pF to 10 µF. Increasing \( C_{\text{res}} \) enabled positive gain at low frequencies. In fact, the positive gain or 0 dB mark, shifts 5 orders of magnitude, from \( 10^5 \) Hz to \( 10^0 \) Hz, enabling harvesting at low frequency.

Increasing \( C_{\text{res}} \) to the calculated optimal value of 10 µF, resulted in a bandwidth improvement at the lower frequency end. Yet, increasing \( C_{\text{res}} \) has its limits. We experimentally verified that there is a practical limit of around 10 µF before the circuit performance begins to degrade, possibly due to magnetic saturation of the Ferrite-based transformer and circuit parasitics, such as the stray capacitance between the transformer windings and wire resistance in the circuit.

Hence, we determine that for the energy harvester to operate in the lowest possible regime, the resonating capacitor needs to be 10 µF, and the related \( C_{\text{cp}} \) needs to be 620 pF. Supplementary Figure S2 shows the effect of varying \( C_{\text{cp}} \) on the output voltage.

### 3.5. Low Frequency Characterization of the Energy Harvester

The charging process of the output capacitor \( C_{\text{out}} \), depicted in Figure 2(b), can be represented as output voltage over time, and therefore serves as the performance indicator of the energy harvester. Figure 3(c) depicts, in green, the simulated output voltage of the default harvester that is not optimized for low frequency. In this case no output voltage is generated. The notable effect of
matching the circuit resonant frequency to lower input frequencies can be seen in the simulation represented in red, where $C_{\text{res}}=10 \, \mu\text{F}$. In less than 1 minute, the output voltage rises from 0 V to 3 V.

Figure 3(c) shows the actual experimental response of a prototype harvester to a low-frequency signal of 1 Hz, using the minimum input signal magnitude of 36 mV, as determined from the data in Figure 1(c). The measured output voltage is presented by the solid blue line. The output voltage reaches a value of 3.1 V within 80 s. The input power scales up to 1 mW, limited by the internal storage capacity of the boost converter.

The output was further characterized as a function of the input signal amplitude, duty cycle and inter-pulse interval, as shown in Figure 4. Figure 4(a) shows the output voltage over time, for different input voltages. For Figure 4(a-c), the first measurement point represents the minimum conditions for the harvester to operate and charge the output capacitor $C_{\text{out}}$. Increasing the amplitude from 36 mV to typical voltages recorded in plants, i.e., 100 mV,[14] the harvester is able to reach the peak voltage of 3.1 V within less than 10 s, for a 1 Hz square pulse. In addition to varying the input magnitude, we also varied the duty cycle. Figure 4(b) shows the output voltage over time for different intervals of the input square wave, or pulse train. The duty cycle varies from 35 % to 80 %. The frequency is fixed at 1 Hz. For a minimum duty cycle of 35 %, the harvester charges up $C_{\text{out}}$ and within 250 s reaches the maximum voltage of 3.1 V. Increasing the duty cycle to 80 % enables the harvester to reach 3.1 V in 25 s. Finally, due to the unpredictable nature of waves and plants’ electrogeneity, the output voltage over time is characterized as a function of the inter-pulse intervals. The inter-pulse interval between two consecutive square wave peaks was varied from 1 s to 3 s. The pulse width was fixed at 0.5 s. As shown in Figure 4(c), even for peaks at 3 s apart, the harvester is able to output about 2.2 V within 400 s. As the inter-pulse decreases, the charging of $C_{\text{out}}$ is faster. At a 1 s inter-pulse interval, the harvester reaches the maximum output
of 3.1 V in less than 1 minute. Note that these results are for the minimum input voltage of 36 mV. Increasing the input voltage to typical recorded spikes in plants, i.e. 100 mV, increases the inter-pulse intervals, at which the harvester can realistically be used, to several seconds. As an example, an output voltage of 2.5 V is reached within 150 s, even when using a 100 mV low-frequency pulse with an inter-pulse interval of 10 s, as shown in Figure 4(d). Hence, within the aforementioned boundary conditions, the circuit can also handle non-periodic input signals.

4. Summary and Conclusion
We demonstrated an energy harvester optimized to operate in the low-frequency regime. The energy harvester consists of a step-up transformer in series with a boost converter, whose input resonant frequency has been matched to that of typical triboelectric generators and electrogenic plants. Our design is validated both by simulations and by experimentally characterizing a home-made, miniaturized, prototype PCB. By optimizing the resonant circuit, the positive gain at low frequencies shifts 5 orders of magnitude, from $10^5$ Hz to $10^0$ Hz, when compared to a default and state-of-the-art boost converter. Our miniaturized prototype enables harvesting of alternating electric signals, with frequencies as low as 0.1 Hz.

The topology allows scalability, i.e. multiple harvesting circuits can be cascaded to the specified bus voltage of a local energy system such as 400 V, based on a standard PV facility, and ultimately connected to the grid.

Supporting Information
Supporting Information is available from the Wiley Online Library or from the author.

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References


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Figure 1. (a) The miniaturized prototype PCB. A ruler and a one-pound sterling coin are shown as a scale reference. (b) Schematic of the V-I curve test circuit. (c) Minimum voltage, current and power for the harvester prototype to operate with an input square wave with a frequency of 1 Hz and a 50% duty cycle.

Figure 2. Overall energy harvester architecture showing (a) the resonant circuit and (b) the LTC3108 boost converter.

Figure 3. (a) Harvester output amplitude as a function of frequency, while varying the transformer primary inductance, $L_p$, from 75 nH to the optimized 7.5 $\mu$H, with the default value of 330pF for the resonant capacitor, $C_{res}$. (b) Frequency response analysis of the energy harvester circuit while tuning the resonant capacitor, $C_{res}$, from the default 330 pF to the optimized value of 10 $\mu$F. (c) Simulated (red) and experimental (blue) output voltage using a 1 Hz input pulse train with 25 mV amplitude for the simulations and 36 mV for the experimental validation. The green trace represents the default LTC3108 simulation, which yields no output. The values for $C_{cp}$ and $C_{res}$ were 620 pF and 10 $\mu$F, respectively.

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Figure 4. PCB prototype characterization. Output voltage over time: (a) varying the input amplitude from 36 mV to 100 mV. The frequency of the input signal was fixed at 1 Hz. The inset illustrates the input signal parameter being changed; (b) varying the duty cycle of the input square wave from 35 % to 80 %, at a fixed input frequency of 1 Hz; (c) varying the inter-pulse interval between two consecutive square wave peaks, from 1 s to 3 s. The pulse width was fixed at 0.5 s and the amplitude was fixed at 36 mV; (d) varying the inter-pulse interval between two consecutive square wave peaks from 1 s to 10 s. The pulse width was fixed at 0.5 s and the amplitude was fixed at 100 mV.
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An energy harvester for low frequency electrical signals
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We devised a technology to harvest energy from low frequency sources, eliminating the need for up-conversion techniques. We accomplish this by modelling and tuning the resonant frequency of an energy harvesting system, which comprises a step-up transformer and a boost converter on a miniaturized PCB prototype.