Mapping the radio sky with an interferometric network of low-frequency radio receivers

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[1] The structure of the 100 kHz radio sky is determined with two interferometric networks of 10 radio receivers which are distributed over local areas of ~1 × 1 km² and ~10 × 10 km². The radio waves arrive at individual receiver pairs with small time differences which are used to determine the arrival direction of the electromagnetic waves including both the bearing and the elevation angle. The results show that the major part of the 100 kHz radio wave energy comes from the horizon at bearings which are consistent with known locations of Long Range Navigation (LORAN) transmitters. Some part of the radio wave energy arrives from the sky at elevation angles which are consistent with the first and second sky hop waves of LORAN transmissions. A minor part of the 100 kHz radio wave energy comes from lightning discharges at distances up to ~1000 km with bearings which are consistent with lightning locations reported by the arrival time difference (ATD) lightning detection network of the UK Met Office. The angular resolution for mapping the radio sky depends on the network geometry, the instrumental timing accuracy, and on the signal-to-noise ratio of the radio waves. The resulting angular resolution of the interferometric networks used in this study is ~1° in bearing at zero elevation and several degrees in elevation.


1. Introduction

[2] It was recently found that the area above thunderclouds is the source of diverse electromagnetic phenomena. For example, it was reported that sprites [e.g., Füllekrug et al., 2001; Cummer and Füllekrug, 2001; Pasko et al., 1998; Cummer and Inan, 1997], gigantic jets [Cummer et al., 2009], and upward electron beams [e.g., Füllekrug et al., 2011, 2010; Roussel-Dupré et al., 1998] exhibit distinct electromagnetic signatures. In the future, it may be also possible to detect the radiation from other lightning-related events, such as streamer discharges above thunderclouds [Qin et al., 2012], lightning-induced particle precipitation [e.g., Gemelos et al., 2009; Rodger et al., 2007; Inan et al., 2007], or more generally energetic charged particles above thunderclouds [Füllekrug et al., 2013]. The radio emissions from electromagnetic phenomena above thunderclouds contain valuable information about the source, e.g., the location, intensity, and the spatial and temporal development of the source.

[3] Numerous methods have been developed to locate lightning discharges on the ground. For example, arrival time difference analysis [e.g., Lee, 1986; Lewis et al., 1960], direction finding [Cummins et al., 1998], time of group arrival [Dowden et al., 2002], or matching waveform tables [Said et al., 2010]. The corresponding radio receiver networks operate on the global scale ~10³–10⁴ km [e.g., Rodger et al., 2006; Sato and Fukunishi, 2003; Füllekrug and Constable, 2000], on the mesoscale ~10¹–10³ km [e.g., Shao et al., 2006; Betz et al., 2004; Cummins et al., 1998], and on the regional scale ~10⁻¹–10² km [e.g., Krebipel et al., 2008].

[4] However, networks operating at low frequencies from ~30–300 kHz and on the local scale ~10⁰–10¹ km have been little studied. This contribution explores the opportunities arising from such local scale interferometric networks to determine the detection and location of electromagnetic radiation sources above thunderclouds. The study focuses in particular on the pulsed 100 kHz radio emissions from Long Range Navigation (LORAN) transmitters which are extremely stable and very well documented [Füllekrug, 2010; United States Coast Guard, 1994]. This contribution presents the underlying theory to determine the arrival direction of the electromagnetic waves, including both the bearing and the elevation angle. The theory is validated by measurements with interferometric networks on two different local scales of ~1 × 1 km² and ~10 × 10 km².

2. Theory

[5] Consider a network of N radio receivers which form (N − 1) linearly independent pairs of instruments. Thus, a
network of 10 instruments forms 9 independent pairs. The kth pair of instruments is characterized by its relative location, expressed in Cartesian coordinates by its pair vector

\[ \mathbf{b}_k = (x_i - x_j, y_i - y_j, z_i - z_j), \]  

(1)

where \( i \) and \( j \) are the instruments of the kth pair.

[6] The unit vector pointing to the source is

\[ \mathbf{r} = (\cos \varphi \cos \theta, \sin \varphi \cos \theta, \sin \theta), \]  

(2)

where the bearing \( \varphi \) counts clockwise from the geographic north and the elevation angle \( \theta \) counts from the horizon upward to the zenith. The source detection is based on the observation of arrival time differences \( \Delta t_k \) which correspond to observed path length differences \( \Delta l_k \) by use of the speed of light \( c \)

\[ \Delta l_k = c \Delta t_k. \]  

(3)

[7] When the source is far away from the network, i.e., the distance to the source \( R \) is much larger than a characteristic average baseline \( \delta_b \), e.g., \( R/\delta_b > 100 \), the theoretical time difference \( \Delta t_k^* \) is calculated from the scalar product between the source vector \( \mathbf{r} \) and the pair vector \( \mathbf{b}_k \)

\[ \Delta t_k^*(\varphi, \theta) = \frac{1}{c} (\mathbf{r}, \mathbf{b}_k). \]  

(4)

The observed and theoretical time differences define a mean square deviation

\[ J(\varphi, \theta) = \sum_{k=1}^{N-1} \left( \Delta t_k - \Delta t_k^*(\varphi, \theta) \right)^2, \]  

(5)

where the summation extends over \( (N - 1) \) independent receiver pairs. The best solution \( (\varphi_0, \theta_0) \) for the bearing and the elevation angle minimizes the deviation

\[ (\varphi_0, \theta_0) = \arg \min_{(\varphi, \theta) \in \mathcal{H}} J(\varphi, \theta), \]  

(6)

where \( \mathcal{H} \) is the upper hemisphere of a unit sphere.

[8] When the source is closer, e.g., \( R/\delta_b < 100 \), the distance between the source and the network needs to be taken into account. The theoretical time difference \( \Delta t_k^* \) in this case is

\[ \Delta t_k^*(\varphi, \theta; R) = \frac{1}{c} \left( R_i - R_j \right), \]  

(7)

where \( R_i \) is the distance between the source and the kth instrument and \( R_j \) is the distance between the source and the

Table 2. Rustrel Network Coordinates\(^a\)

<table>
<thead>
<tr>
<th>No.</th>
<th>Lat (°N)</th>
<th>Lon (°E)</th>
<th>Height (m)</th>
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<tr>
<td>01</td>
<td>43.94527</td>
<td>5.53473</td>
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<td>43.98687</td>
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<td>07</td>
<td>43.94092</td>
<td>5.48386</td>
<td>1009</td>
</tr>
</tbody>
</table>

\(^a\)Geographic coordinates of the seven radio receivers which form the interferometric network on Plateau d’Albion near Rustrel in Southern France.

3. Experiment

[9] An interferometric network of radio receivers was deployed on an old airfield at Charmy Down near Bath in South West England. Daytime recordings during the time interval from 14:36:45–14:56:45 UTC on 13 May 2011 were collected. The network consists of 10 wideband digital low-frequency radio receivers which record vertical electric field strengths in the frequency range from ~4 Hz to ~400 kHz with a sampling frequency of 1 MHz, an amplitude resolution of ~35 μV/m and a relative timing accuracy of ~12 ns provided by the GPS clock [Füllekrug, 2010]. The radio receivers are distributed over an area of ~1 × 1

Figure 1. Vertical electric field recordings in the frequency range from ~4 Hz–400 kHz with 10 radio receivers. An offset of 100 mV/m is added consecutively to the recordings. All recordings exhibit highly coherent waveforms with small time delays which reflect the propagation of electromagnetic waves across the network.
reflect the propagation of electromagnetic waves across the
are highly coherent (Figure 1). The small time differences
results from logistic constraints and accessibility to the area.

The waveforms recorded by the Charmy Down network
consists of several sets of transmitters (chains) with differ-
tly, the individual timings of all instruments of the Rustrel
SST 43.7397 –1.1804 174.74 175 858 28 62
RNT 54.8083 8.2935 58.00 60 804 30 66

LORAN Transmitters With Respect to Charmy Down Networka

<table>
<thead>
<tr>
<th>Name</th>
<th>Lat (°N)</th>
<th>Lon (°W)</th>
<th>ϕ (°)</th>
<th>Ψ (°)</th>
<th>d (km)</th>
<th>Δtgs1 (μs)</th>
<th>Δtgs2 (μs)</th>
</tr>
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<tbody>
<tr>
<td>LSY</td>
<td>49.1486</td>
<td>–1.5047</td>
<td>166.29</td>
<td>166</td>
<td>260</td>
<td>88</td>
<td>187</td>
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<tr>
<td>ANT</td>
<td>54.9112</td>
<td>–3.2872</td>
<td>351.22</td>
<td>351</td>
<td>393</td>
<td>60</td>
<td>131</td>
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<tr>
<td>SST</td>
<td>43.7397</td>
<td>–1.1804</td>
<td>174.74</td>
<td>175</td>
<td>858</td>
<td>28</td>
<td>62</td>
</tr>
<tr>
<td>RNT</td>
<td>54.8083</td>
<td>8.2935</td>
<td>58.00</td>
<td>60</td>
<td>804</td>
<td>30</td>
<td>66</td>
</tr>
</tbody>
</table>

aGeographic coordinates of the four LORAN transmitters Lessay (LSY), France, Soustons (SST), France, Anthorn (ANT), UK, and Rantum (RNT), Germany. The expected bearing ϕ and the average observed bearing Ψ of the LORAN transmitters observed with the network at Charmy Down agree within ~1°. The distances d between the LORAN transmitters and the network enable the determination of the corresponding arrival time differences between the ground wave and the sky wave (Δtgs) which are calculated here for an ionospheric height of 60 km for daytime (Δtgs1) and 90 km for nighttime (Δtgs2).

4. Solution Accuracy and Network Resolution

The waveforms of the sources recorded by the network demonstrate specific time delays between different instruments. The bearing and elevation to the source can be found by substituting these time delays into (5) and subsequent minimization (6). Thus, the accuracy of the solution is defined by three factors which can be analyzed separately: (i) the accuracy of the time differences, (ii) the accuracy of the minimization procedure, and (iii) the network resolution.

The accuracy of the time differences depends on the timing accuracy of the GPS clocks (~12 ns), the accuracy of the network synchronization (~100 ns for the Charmy Down network and ~300 ns for the Rustrel network), and on the signal-to-noise ratio of a source. All of the above depend on the wavelength to baseline length ratio. For the Charmy Down experiment, the overall accuracy level of the time differences is estimated to be ~100 ns by use of the LORAN signals. For the Rustrel experiment, the over-
all accuracy level of the time differences is estimated to be 

\(~300\text{ ns}\).

[17] 2. The accuracy of the minimization procedure (6) is fixed and equals 0.5°, because this procedure is evaluated on a fixed \(1° \times 1°\) grid in the upper hemisphere \(U\) of a unit sphere. It is possible to provide any desired accuracy on this step which is only restricted by the computational costs. For the Charmy Down and Rustrel experiments, half of a degree accuracy is more than enough, because the best network’s resolution is estimated to be not better than 1° (see below in this section).

[18] 3. The network resolution is defined by the network geometry and depends on the accuracy level of the time differences. The network of \(N\) instruments is characterized by \((N - 1)\) linearly independent arrival time differences for a signal source arriving from a specific direction \((\varphi_0, \theta_0)\). All possible directions in the sky (the upper hemisphere \(U\)) form a 2-D surface in the \((N - 1)\)-dimensional ATD phase space. This surface can be written in the parametric form as a set of equations by use of (4) and (2):

\[
t_k = \frac{1}{c} (b_{kx} \cos \varphi \cos \vartheta + b_{ky} \sin \varphi \cos \vartheta + b_{kz} \sin \vartheta), \quad k = 1, \ldots, N - 1,
\]

where \(t_k\) is the time difference for the \(k\)th use of (4) and (2) pair, \(c\) is speed of light, \((b_{kx}, b_{ky}, b_{kz})\) is the \(k\)th station pair vector and \((\varphi, \vartheta) \in U\) is the direction to a source which varies over the entire sky (the upper hemisphere \(U\) of a unit sphere).

[19] Arrival time differences from actual measurements have a certain accuracy, e.g., for the Charmy Down experiment, 100 ns. This means that the exact time differences \(t_k\) which correspond to an exact solution always differ from the observed time differences \(t_{ok}\) within the accuracy level \(\delta t_k\) which is 100 ns for all pairs in the Charmy Down experiment and 300 ns in the Rustrel experiment.

[20] All physical sets of time differences that correspond to the observed set of time differences \(t_{ok}\) within the accuracy level \(\delta t_k\) belong to an intersection of the cube (11) with the surface (10):

\[
| t_k - t_{ok} | \leq \delta t_k, \quad k = 1, \ldots, N - 1,
\]

where \(t_k\) are the cube variables, \(t_{ok}\) is the cube center which corresponds to the set of observed time differences and \(\delta t_k\) is the accuracy level for the \(k\)th station pair, which is 100 ns for all pairs in the Charmy Down experiment and 300 ns in the Rustrel experiment.
where \((\varphi, \theta) \in \mathcal{U}\) varies over the entire sky (the upper hemisphere \(\mathcal{U}\) of a unit sphere). This intersection defines an area in the sky where the signal with the observed time differences \(t_{Ok}\) could arrive from. The collection of such intersections of all possible cubes centered at all possible sky points \((\varphi, \theta) \in \mathcal{U}\) results in the resolution map of the network. This resolution map characterizes the network geometry and shows the structure of solution areas in the sky for a fixed accuracy level of the time differences.

[21] Based on this concept, the resolution maps of the Charmy Down and Rustrel networks are calculated in the following way. The solution areas are centered on regularly spaced sky points \((\varphi_s, \theta_s)\) with 10° steps in bearing and 15° steps in elevation starting from the \((0^\circ, 0^\circ)\) point. These sky points \((\varphi_s, \theta_s)\) correspond to the cube centers \(t_{Ok}\) in the ATD domain:

\[
t_{Ok} = \frac{1}{c} (b_{kx} \cos \varphi_s \cos \theta_s + b_{ky} \sin \varphi_s \cos \theta_s + b_{kz} \sin \theta_s),
\]

\[
k = 1, \ldots, N-1.
\]

The solution areas are obtained by checking the conditions (12) on the entire sky \((\varphi, \theta)\) covered by the \(0.1^\circ \times 0.1^\circ\) grid. The sky points \(t_k(\varphi, \theta)\) (10) that belong to the solution area (12) are characterized by the distance \(T(\varphi, \theta; \varphi_s, \theta_s)\) to the center of the area \(t_{Ok}(\varphi_s, \theta_s)\) (13) in the ATD domain measured in nanoseconds:

\[
T(\varphi, \theta; \varphi_s, \theta_s) = \sqrt{\sum_{k=1}^{N-1} (t_k(\varphi, \theta) - t_{Ok}(\varphi_s, \theta_s))^2}.
\]

[22] Figure 2 shows the resolution map of the Charmy Down network for time differences with an accuracy level of 100 ns calculated by use of the described method. Color scale corresponds to the distance \(T(\varphi, \theta; \varphi_s, \theta_s)\) measured in nanoseconds. Taking \(T(\varphi, \theta; \varphi_s, \theta_s) = 100\) ns as one sigma level, the resulting bearing accuracy of the network varies from \(\sim 1^\circ\) to \(\sim 2^\circ\) for the zero elevation and from \(\sim 3^\circ\) to \(\sim 6^\circ\) for 75° elevation. The resulting elevational accuracy varies from \(\sim 10^\circ\) to \(\sim 15^\circ\) for the zero elevation and from \(\sim 1^\circ\) to \(\sim 2^\circ\) for 75° elevation angle.

[23] Similarly, Figure 3 represents the resolution map of the Rustrel network calculated for time differences with an accuracy level of 300 ns. Taking \(T(\varphi, \theta; \varphi_s, \theta_s) = 300\) ns as one sigma level, the resulting bearing accuracy of the network varies from \(\sim 0.5^\circ\) to \(\sim 1^\circ\) for the zero elevation and from \(\sim 1.5^\circ\) to \(\sim 3^\circ\) for 75° elevation. The resulting elevational accuracy varies from \(\sim 6^\circ\) to \(\sim 10^\circ\) for the zero elevation and from \(\sim 0.5^\circ\) to \(\sim 1^\circ\) for 75° elevation angle.

[24] The solution areas demonstrate larger extent in elevation close to the horizon, when compared to higher elevation areas. This is common for flatly distributed networks and known as the “fish eye effect” which results in the poorest resolution of the flat network in the coordinate normal to the plane of the network for the signals arriving close to that plane. The resolution map shows how the network geometry defines the structure of the radio sky image produced by the network, in which areas the network has a good or poor resolution.

[25] In practice, signals are always recorded with a certain signal-to-noise ratio. This means that a stationary transmitter appears on a radio image as an area in the sky defined by the resolution map of the network.

5. Mapping the Radio Sky

[26] The low-frequency radio sky is mapped by treating each 10 µs long time interval of the recordings as a separate radio source, because 10 µs corresponds to one oscillation.

Figure 4. Map of the radio sky in the frequency range 90–110 kHz for all sources with a significant signal-to-noise ratio. Green arrows indicate LSY-ANT interference. Red, orange, and brown arrows indicate RNT-ANT, RNT-SST, and RNT-LSY interference. White arrows indicate clusters of lightning discharges.

Figure 5. Map of the radio sky after exclusion of the interference between transmitters of the Lessay chain and the Sylt chain by removing the transmissions of the Sylt chain.
at a carrier frequency of 100 kHz. This is possible for the Charmy Down network because the longest baseline (~1.26 km) constitutes one third of the 100 kHz wavelength (~3 km) such that all instruments of the network record at least ~70% of the same 10 μs long cycle. The recordings of each 10 μs cycle are used to calculate the phase of its 100 kHz spectral component. The phase difference measured between two instruments corresponds to a time of arrival difference

\[ \Delta t_k = \Delta \phi_k / 2\pi \cdot 10 \mu s. \]  

(15)

The time differences of nine linearly independent pairs of instruments are used for the subsequent analysis. The bearing and elevation angle are subsequently determined by the use of the theory and those experimental measurements with a significant signal-to-noise ratio recorded during the time interval from 14:36:45–14:56:45 UTC on 13 May 2011. The resulting bearings and elevations are mapped on a grid of 1° × 1°. The logarithm of the total number of source counts in each grid cell is used to calculate the final radio map which exhibits a rich information content (Figure 4).

[27] Several different structural elements can be discriminated. The map is dominated by the four LORAN transmitters (LSY, SST, ANT, and RNT), which can be clearly identified on the horizon. The expected and observed bearings are in excellent agreement (Table 3). The LORAN transmissions from the horizon are associated with a distortion in elevation in accordance with the resolution map (Figure 2). The size of the observed patches in the sky above the horizon corresponds to a timing accuracy of ~30 ns for LSY and ~100 ns for the other LORAN transmitters as a result of their lower signal-to-noise ratio.

[28] Another structural element on the map are the arcs in the sky which connect different LORAN transmitters. These arcs result from the interference between LORAN transmitters in different chains as described in section 3. The interchain interference can be removed by excluding the emission times of the interfering LORAN transmitters from the Sylt chain (Figure 5), because the transmission times of LORAN transmitters are well documented.

[29] The last structural element on the radio map are diffuse clusters of radio sources in the sky. These clusters are seen more clearly when all LORAN transmissions are removed from the map (Figure 6a). Integrating the source counts over all elevation angles results in the number of

\[ N_{\text{diffuse}} = \int_0^{\pi} \log_{10} N(\theta, \phi) \, d\theta \, d\phi. \]

Figure 6. (a) Map of the radio sky after exclusion of all LORAN transmitters which reveals clusters of lightning discharges in thunderstorms at known locations. (b) The azimuthal distribution of lightning discharges calculated from an integration of the map over all elevation angles.

Figure 7. Relative locations of the Charmy Down network (blue circle), LORAN transmitters (black triangles), and lightning discharges (red stars) during the measurements. The bearings from the network to major thunderstorms (Figure 6) are indicated by black lines and equal 125°, 135°, 200°, and 310°. The bearing to a thunderstorm which was hidden behind the LSY transmitter is indicated by the magenta line and equals 160°.
and a distance of 50–80 km. This aim can be achieved by analyzing the sky waves of the LORAN transmissions arriving from different directions of the sky no longer belong to the same 10 μs cycles of the different instruments’ recordings. Certain time shifts dependent on the instrument location and LORAN transmitter analyzed are introduced into the recordings of each instrument to compensate this 10 μs cycle mismatch. Thus, the total arrival time difference consists of this cycle correction shift which can be calculated with 1 μs precision (because the exact bearings of the LORAN transmitters are known) and the delay calculated by use of the 10 μs cycle phase difference between the two instruments (15).

Figure 8. Examples of the demodulated waveforms of a single LORAN pulse for the LORAN transmitters (a) LSY, (b) SST, and (c) ANT as observed with a network deployed in Southern France.

Source locations of the ground and sky waves are determined by the use of the technique described in section 2, equations (5) and (6). The way to calculate the arrival time differences of the LORAN signals is a little different than the one used for the Charmy Down network because the baselines (~10 km) in the Rustrel experiment are longer than the wavelength (~3 km) and the radio signals arriving from different directions of the sky no longer belong to the 10 μs cycles of the different instruments’ recordings. Certain time shifts dependent on the instrument location and LORAN transmitter analyzed are introduced into the recordings of each instrument to compensate this 10 μs cycle mismatch. Thus, the total arrival time difference consists of this cycle correction shift which can be calculated with 1 μs precision (because the exact bearings of the LORAN transmitters are known) and the delay calculated by use of the 10 μs cycle phase difference between the two instruments (15).

[32] The resulting nighttime radio map shows the elevations of the sky waves (Figure 9), which are calculated based on the processing of the 10 μs cycles corresponding to the maxima of the ground wave and the first and second hop sky waves of the waveforms shown in Figure 8. The results agree with the expected elevations within ~2° (Table 4). It is interesting to note that the ground wave from ANT is not present as a result of the attenuation over the large distance from the network.

Figure 9. Locations of the ground wave and the first and second sky hop waves for the LORAN transmitters (a) LSY, (b) SST, and (c) ANT as observed with a network deployed in Southern France.
6. Summary

[33] The design of an interferometric network of low-frequency radio receivers is described to map the 100 kHz radio sky. The design is validated with the operation of a network of instruments distributed over an area of ~1 × 1 km² and ~10 × 10 km². The resolution map of the network is used for a quantitative assessment of the angular resolution of the network which is important for an interpretation of the radio maps. The resulting bearing accuracy of the 1 × 1 km² (Charmy Down) network varies from ~1° to ~2° for 0° elevation and decreases for higher elevations varying from ~3° to ~6° for 75° elevation. The resulting elevation accuracy varies from ~10° to ~15° for 0° elevation and increases with elevation varying from ~1° to ~2° for 75° elevation angle. 10 × 10 km² (Rustrel) network provides better resolution because of longer baseline lengths. Its resulting bearing accuracy varies from ~0.5° to ~1° for zero elevation and from ~1.5° to ~3° for 75° elevation. The resulting elevation accuracy varies from ~6° to ~10° for zero elevation and from ~0.5° to ~1° for 75° elevation angle.

[34] Charmy Down 100 kHz radio image exhibits three main structural elements which are associated with LORAN transmitters, LORAN interchain interference and close (up to ~1000 km) lightning activity. The ability of the network to detect and locate the radio signals arriving from an elevation is validated with the operation of the network deployed in Rustrel, Southern France. The elevation angles of the first and second hop sky waves from LORAN transmissions are determined by the network in agreement with the expected elevation angles within ~2° accuracy.

[35] A future application of the small-scale interferometric network is, for example, to use the network for the detection of transient events which have higher signal-to-noise ratios than LORAN transmissions because they cover a broader frequency range. On the other hand, transient events are not repetitive such that averaging is not possible to increase the signal-to-noise ratio. As a result, the resolution map for a specific network geometry defines the angular resolution for individual transient events. Such kind of data analysis could be applied in the future to the radio recordings of multihop sky waves from lightning discharges [Shao et al., 2013; Smith et al., 2004], relativistic electron beams above thunderclouds [Füllekrug et al., 2011], and sprite streamers above thunderclouds [Qin et al., 2012]. But the methodology could also be used to study the low-frequency electromagnetic radiation emanating from source regions created by HF heating of the ionosphere during the presence of auroral electrojet current [Moore et al., 2012] or to study in more detail the arrival of auroral kilometric radiation on the ground [LaBelle and Anderson, 2011].

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