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# 1 Regional flood hydrology in a semi-arid catchment using a 2 GLS regression model

3

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10

## 11 **Abstract**

12 The regional flood frequency hydrology of the 86,000 km<sup>2</sup> and semi-arid Ebro catchment is  
13 investigated using an extended generalised least square model that includes separate  
14 descriptions for sampling errors and model errors. The Ebro catchment is characterised by  
15 large hydro-climatic heterogeneities among sub-regions. However, differences in flood  
16 processes among sites are better explained by a set of new catchment descriptors introduced  
17 into hydrological regression models, such as new characteristics derived from the slope of  
18 flow duration curves, the ratio of mean annual precipitation to extreme precipitations and the  
19 aridity index. These additions enabled a more direct link to be established between the general  
20 flow regime and the extreme flood characteristics through-out the entire catchment. The new  
21 regression models developed in this study were compared to a set of existing models  
22 recommended for flood frequency estimation in Spain. It was found that the generalised least  
23 squares model developed in this study improves the existing ordinary least squares models

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1 both at regional and trans-regional scales. An adequate description of flood processes is  
2 obtained and, as a direct consequence, more reliable flood predictions in ungauged  
3 catchments are achieved.

4 **Keywords:** Regional flood hydrology; GLS regression model; Ebro catchment; Catchment  
5 descriptors; Prediction in ungauged basins

6

## 7 **1 Introduction**

8 The prediction of flood frequencies in ungauged catchments is essential for both designing  
9 hydraulic infrastructures and effective flood risk management, as floods are one of the most  
10 important causes of economic losses in most parts of the world and most catchments are  
11 ungauged. To be better prepared for future floods, the European Union has recently  
12 established a framework for the assessment and management of flood risks, with the aim of  
13 reducing its adverse consequences by knowing flood levels for given probabilities at any  
14 stream point (EU, 2007).

15 The flood level for a given probability at any stream section is usually calculated by a  
16 hydraulic model that takes flood quantile estimations as input, which can be obtained from  
17 observed data. However, most stream points are ungauged. Thus, spatial information  
18 expansion is required to extend the known information in a few gauged catchments to these  
19 ungauged sites (Merz and Blöschl, 2008). This expansion usually entails two steps: (i)  
20 estimation of regional quantiles at gauged sites for the probability of interest; (ii) use of a  
21 regional method to transfer the known information at gauged sites to ungauged catchments.

22 Several regional flood frequency analyses have been developed in past years. Most of them  
23 are based on the use of the index flood method as regional model to estimate flood frequency  
24 curves (e.g. Robson and Reed, 1999; Bocchiola et al., 2003; Laio et al., 2011; Dawdy et al.,  
25 2012). Regions are assumed to be composed of a set of sites that are homogeneous, which can  
26 be grouped by different methods, such as geographical boundaries, cluster analysis and  
27 pooling methods. Homogeneity of proposed regions is confirmed by passing a statistical  
28 heterogeneity test (Hosking and Wallis, 1997; Castellarin et al., 2008).

1 The prediction at ungauged sites can be conducted by means of either statistical methods that  
2 use series of discharge records or process-based methods that use climate data to run rainfall-  
3 runoff models. A comparison between them in Austria can be found in Viglione et al. (2013).  
4 Statistical methods are usually based on a regression model that tries to explain differences  
5 among flood generation processes through a set of physiographic variables. Catchment  
6 response can be characterised in regression models by either the T-year quantile or the index-  
7 flood (so-called index-flood indirect estimation methods) (Brath et al., 2001). Other methods  
8 exist, such as regional envelope and multivariate probabilistic regional envelope curves  
9 (Castellarin et al., 2007) and regional analysis that incorporates historical and palaeoflood  
10 information at ungauged sites (Gaume et al., 2010), among many others. A complete review  
11 of methods for predicting floods in ungauged basins can be found in Blöschl et al. (2013). In  
12 Spain, a regional flood frequency analysis has been conducted recently to improve flood  
13 frequency estimations at both gauged and ungauged sites, within the Floods Directive  
14 framework (Jiménez-Álvarez et al., 2012). Mainland Spain was divided into 36 homogeneous  
15 regions defined by geographical boundaries. Regional quantiles at gauged sites in most  
16 regions were estimated by a Generalised Extreme Value (GEV) distribution fitted by the L-  
17 moments method with a regional shape parameter, which is estimated by the regional value of  
18 the L-coefficient of skewness (L-CS). An ordinary least squares (OLS) regression model was  
19 developed to estimate quantiles at ungauged sites in each region.

20 The main strength of an OLS model is its simplicity, as the estimation of the model  
21 uncertainty is straightforward. However, OLS assumes that the uncertainty of quantile  
22 estimates at each site are identical, which is not the case as record-lengths vary from site to  
23 site. The OLS also neglects both the correlation between quantiles and the correlation  
24 between regression model errors. In addition, the existing OLS models in Spain use a reduced  
25 set of explanatory variables, usually basin area, precipitation quantiles and mean basin  
26 elevation (CEDEX, 2011; Jiménez-Álvarez et al., 2012). More variables could be added to the  
27 regression model to account for differences in processes that generate floods. To improve the  
28 OLS model currently applied in Spain and overcome its weaknesses, a new regression model  
29 is proposed.

30 In this paper, a regional flood frequency hydrology analysis was carried out in the Ebro River  
31 catchment in Spain focusing on the spatial expansion of information to improve the existing  
32 regression models. The generalised least squares (GLS) technique that includes the clustering

1 tendency of residuals (Kjeldsen and Jones, 2010) was adapted to the recommendations given  
 2 in Spain to estimate the frequency distribution, suggesting the use of a GEV distribution fitted  
 3 through the L-moments method with a given regional shape parameter (Jiménez-Álvarez et  
 4 al., 2012; MARM, 2011). The semi-arid Ebro River catchment was selected as case study  
 5 because it shows a significant heterogeneity of climate drivers, rainfall patterns and soil  
 6 characteristics among homogeneous sub-regions. In addition, a limitation of the existing  
 7 analysis consists of applying an OLS regression model to each of the five homogenous  
 8 regions in which the catchment was divided. This paper also addresses the development of a  
 9 united regression model in the whole Ebro River catchment to avoid undesirable overfitted  
 10 regression models to a reduced set of gauging stations. Summarising, an exploratory analysis  
 11 was conducted to investigate how catchment descriptors explain the differences in flood  
 12 processes among catchments.

13

## 14 **2 Hydrological regression models**

15 Regression models are commonly used to describe the between-catchment variation in the at-  
 16 site estimates of T-year flood quantiles ( $x_T$ ) at gauged sites by relating the hydrological  
 17 response to different physiographic variables (so called catchment descriptors), which then  
 18 take on the role of simplified surrogates of drivers of the flood generation processes. Having  
 19 estimated a regression model, the T-year event can then be predicted in ungauged catchments  
 20 where only the catchment descriptors are available. Denoting the vector of at-site log-  
 21 transformed flood quantiles from  $N$  sites as  $\mathbf{y}$  (Eq. 1), the associated matrix of  $m$  different  
 22 catchment descriptors with a first column of unity as  $\mathbf{X}$ , i.e. the dimension of this matrix is  
 23  $N \times (m+1)$ , and the vector of  $m+1$  regression model parameters as  $\boldsymbol{\theta}$ , a regression model can be  
 24 formulated by Eq. (2).

$$25 \quad \mathbf{y} = \log_{10}(\mathbf{x}_T) \quad (1)$$

$$26 \quad \mathbf{y} = \mathbf{X}^T \boldsymbol{\theta} + \boldsymbol{\eta} + \boldsymbol{\varepsilon} = \mathbf{X}^T \boldsymbol{\theta} + \boldsymbol{\omega} \quad (2)$$

27 where  $\boldsymbol{\varepsilon}$  is the vector of sampling errors of the log-transformed at-site quantile,  $\boldsymbol{\eta}$  is the vector  
 28 of regression model errors, and  $\boldsymbol{\omega}$  is the vector of total regression errors ( $\boldsymbol{\omega} = \boldsymbol{\varepsilon} + \boldsymbol{\eta}$ ).

29 The formulation in Eq. (2) shows that the regression model error can be split into the  
 30 sampling estimate error and the modelling error. The sampling error represents differences

1 between the quantile estimation from observed data and its true value ( $\xi$ ), which is unknown,  
 2 as we would need a record length of an infinite number of years to know it exactly (Eq. 3).  
 3 This error only depends on the observed data at each site, the probability distribution used to  
 4 estimate quantiles and the method used to estimate the distribution parameters. In contrast, the  
 5 modelling error represents the difference between the regression model estimation and its true  
 6 value ( $\xi$ )(Eq. 4). The model error can be also interpreted as the inability of the regression  
 7 model to explain the catchment behaviour perfectly when only lumped catchment descriptors  
 8 are used as surrogate explanatory variables for the more complex, and often non-linear,  
 9 catchment scale hydrological processes. In contrast to the sampling error, the model error  
 10 depends on the structure of the regression model and, thus, on the selection of catchment  
 11 descriptors.

$$12 \quad y = \xi + \varepsilon \quad (3)$$

$$13 \quad \xi = \mathbf{X}^T \boldsymbol{\theta} + \eta \quad (4)$$

14 The two errors represent fundamentally different aspects of the modelling process, and in the  
 15 following the covariance structure of each error type will be discussed. The covariance matrix  
 16 of the regression errors ( $\boldsymbol{\Sigma}_w$ ) is defined as the sum of the covariance matrix of the sampling  
 17 errors ( $\boldsymbol{\Sigma}_\varepsilon$ ) plus the covariance matrix of the modelling errors ( $\boldsymbol{\Sigma}_\eta$ ) (Eq. 5). It is assumed that  
 18 the two errors are mutually independent.

$$19 \quad \boldsymbol{\Sigma}_w = \boldsymbol{\Sigma}_\varepsilon + \boldsymbol{\Sigma}_\eta \quad (5)$$

20 Typically, the parameters of the regression model,  $\boldsymbol{\theta}$ , are estimated by the least squares  
 21 method. Different sub-methods exist depending on the complexity of the covariance structure  
 22 of the errors adopted in the regression model. They are classified, in an increasing complexity  
 23 order, as: ordinary least square (OLS), weighted least squares (WLS), and generalised least  
 24 square (GLS). A more in-depth review of regression models can be found in Rosbjerg et al.  
 25 (2013). Other methods of estimating the model parameters include maximum-likelihood and  
 26 Bayesian methods.

27 The GLS technique was developed for application in hydrology by Stedinger and Tasker  
 28 (1985) to account for the heteroscedasticity and cross-correlation of residuals. Specifically,  
 29 the GLS model assumes that estimates of flood quantiles at different sites are correlated, as  
 30 they have been estimated using correlated flood data. This then leads to a  $\boldsymbol{\Sigma}_\varepsilon$  matrix with

1 diagonal elements equal to the estimation variance of quantiles ( $\sigma_\varepsilon^2$ ) and off-diagonal  
 2 elements equal to the covariance between quantiles across pairs of sites (Eq. 6).

$$3 \quad \Sigma_\varepsilon = \begin{cases} \Sigma_{\varepsilon,ii} = \sigma_\varepsilon^2(y_i) & i = j \\ \Sigma_{\varepsilon,ij} = \text{cov}(y_i, y_j) & i \neq j \end{cases} \quad (6)$$

4 In the GLS model formulation presented by Stedinger and Tasker (1985), the model error  
 5 matrix ( $\Sigma_\eta$ ) only includes non-zero elements along the diagonal, as it assumes that the  
 6 modelling errors are uncorrelated between sites. Based on the observation that localised  
 7 clusters of positive and negative residuals were prevalent among neighbouring catchments  
 8 when modelling a large set of annual maximum series (AMS) of peak flows in the UK,  
 9 Kjeldsen and Jones (2009) extended the GLS model to include off-diagonal elements larger  
 10 than zero into the  $\Sigma_\eta$  matrix to describe inter-site correlations of modelling errors (Eq. 7 and  
 11 8).

$$12 \quad \Sigma_\eta = \sigma_\eta^2 \mathbf{R}_\eta \quad (7)$$

$$13 \quad \mathbf{R}_\eta = \begin{cases} 1 & i = j \\ \rho_{\eta,ij} & i \neq j \end{cases} \quad (8)$$

14 where  $\sigma_\eta^2$  is the variance of modelling errors,  $\mathbf{R}_\eta$  is a matrix describing inter-site correlations  
 15 and  $\rho_{\eta,ij}$  is the correlation of model errors between sites  $i$  and  $j$ . The split between a model  
 16 error variance, assumed constant across all catchments, and a correlation matrix,  $\mathbf{R}_\eta$ , is  
 17 convenient for subsequent model development in the next sections.

18 In the following sections this GLS regression model framework is developed and tested using  
 19 hydrological flood data from a large semi-arid catchment situated in North-East Spain.

20

### 21 **3 Case study: the Ebro River catchment**

22 The Ebro River catchment is located in the Northeast of Spain covering an area of 84,000 km<sup>2</sup>  
 23 (see Fig. 1). The regional hydrology shows significant spatial heterogeneities because of i)  
 24 abrupt changes in orography, as terrain elevation ranges from sea level at the Ebro Delta to  
 25 3,404 m.o.s.l at the Aneto peak in the central Pyrenees, which is the highest point in the  
 26 catchment; ii) heterogeneities in precipitation patterns, as the Southeast part of the catchment  
 27 has a mean annual rainfall of 450 mm, while in some regions of the Pyrenees a mean annual  
 28 rainfall of 2,500 mm is observed, and iii) a great variability in quantiles of maximum daily

1 precipitation, as the 100-year rainfall quantile ranges from 80 mm in the central South part of  
2 the catchment and up to 160 mm in some parts of the Pyrenees.

3 Observed AMS of instantaneous peak flow from 93 gauging stations located in natural or  
4 near-natural catchments were used in the study (Fig. 1). Regional L-moment values for the  
5 five homogeneous regions used in the Ebro River catchment can be seen in Table 1. Eight  
6 different catchment descriptors were readily available for each of the 93 catchments,  
7 including: 1) catchment area in km<sup>2</sup> (A); 2) mean elevation of the catchment over the mean  
8 sea level in m (H); 3) maximum daily precipitation with a  $T$ -year return period in mm ( $P_T$ ); 4)  
9 mean annual precipitation in mm ( $P_m$ ); 5) mean infiltration rate in mm ( $t_{inf}$ ), which was  
10 calculated from a national gridded map obtained previously by the kriging method applied to  
11 a set of site values estimated from either field measurements or a function that simulates the  
12 water transference in a soil; 6) mean catchment slope (S); 7) initial abstraction in mm ( $P_0$ ),  
13 defined as the precipitation needed before runoff begins, which was calculated from a national  
14 gridded map obtained previously using information provided by maps of  $t_{inf}$  and land use from  
15 the CORINE Land cover; and, finally, 8) catchment area (again measured in km<sup>2</sup>) located at  
16 elevations in excess of 1,500 m ( $A_{1500}$ ).

17 A further three catchment descriptors were developed as part of this study to better capture  
18 climatic differences between sites: i) the mean potential evapotranspiration in mm (PET),  
19 which was obtained from temperature series in the period 1940-1995 through the  
20 Thornthwaite and Penman equations; ii) the aridity index ( $I_a$ ), defined as the ratio of  $P_m$  to  
21 PET; and iii) the extremity index ( $I_e$ ), defined as the ratio of  $P_m$  to  $P_T$ .

22 Two additional catchment descriptors were used to capture differences in flood response from  
23 the information given by flow duration curves (FDC). Specifically, a concavity index ( $IC$ )  
24 was adopted, which gives information about the relationship between low-flow and high-flow  
25 regimes (Eq. 9) (Sauquet and Catalogne, 2011). A coefficient was defined to measure the  
26 slope of the upper part of the FDC for the highest flows ( $SFDC_p$ ) (Eq. 10),

$$27 \quad IC = \frac{Q_{0.1} - Q_{0.99}}{Q_{0.01} - Q_{0.99}} \quad (9)$$

$$28 \quad SFDC_p = \frac{Q_{max} - Q_p}{100 p} \quad (10)$$



1 where  $Q_p$  is the daily runoff for an exceedance probability of  $p$  and  $Q_{max}$  is the maximum  
2 daily runoff. Both  $Q_p$  and  $Q_{max}$  are calculated from a FDC standardised by the mean daily  
3 runoff to enable the comparison between catchments.

4 All these descriptors can be obtained easily from digital terrain models and other gridded  
5 dataset of climate, such as rainfall and evapotranspiration, except for the case of those  
6 descriptors that capture the properties of the FDC. In this case, a further analysis should be  
7 carried out to establish relationships between these indexes and different soil descriptors to  
8 enable estimation in ungauged catchments. However, this additional step is beyond the scope  
9 of this paper.

10 The following sub-section addresses how these catchment descriptors can explain the  
11 differences in flood generation processes among catchments.

### 12 **3.1 Explaining flood processes by catchment descriptors**

13 Catchment area,  $A$ , and the respective T-year rainfall quantile,  $P_T$ , are the two first catchment  
14 descriptors usually introduced into a regression model. As expected, catchment area always  
15 exerts the largest influence on the magnitude of floods, as generally larger catchments lead to  
16 larger floods. The inclusion of the rainfall quantile gives additional information about  
17 differences in flood magnitude between similar sized catchments, as larger values of  $P_T$  will  
18 usually result in larger floods being generated.

19 The mean catchment slope,  $S$ , explains differences among catchments due to their  
20 topography. Catchments with steeper slopes are expected to have faster runoff velocity in  
21 hillslopes which reduces the concentration time, and consequently lead to higher peak flow  
22 values.

23 The concavity index,  $IC$ , characterises the upper part of the FDC, explaining differences in  
24 catchment hydrological responses. Larger values of  $IC$  are obtained at sites where the  
25 hydrological response is more smoothed due to the existence of aquifers or the influence of  
26 snowmelt. In contrast, smaller values of  $IC$  are found in catchments with fast runoff responses  
27 due to the existence of impermeable soils or extreme climate conditions, as is often the case in  
28 arid and semi-arid regions (Castellarin et al., 2013).

29 The extremity index,  $I_e$ , explains how large  $P_T$  is in comparison to  $P_m$ . This descriptor gives  
30 information about the variability of extreme rainfall events compared to the mean annual

1 rainfall. Smaller values of  $I_e$  will typically be observed in more arid regions, where larger year  
2 to year variability in extreme rainfall events is observed.

3  $P_0$  is related to the potential maximum water retention of a soil. Therefore, this descriptor  
4 gives information about the portion of precipitation transformed into surface runoff in the  
5 catchment. In fact,  $P_0$  supplies different information than the  $IC$  index. The latter explains the  
6 probability distribution of daily runoffs, capturing the relationship between surface runoff and  
7 subsurface flow, without accounting for the precipitation. However,  $P_0$  gives information  
8 about the hydrologic abstraction process to transform precipitation into surface runoff.

9 Potential evapotranspiration,  $PET$ , gives information about the initial moisture content. A  
10 catchment with wetter soil moisture content will drive a larger flood than a catchment with  
11 dryer soil moisture content, for the case of a similar rainfall event. The aridity index,  $I_a$ , also  
12 accounts for the likely initial soil moisture content before a flood begins.

13

## 14 **4 Methodology**

15 The methodology section describes the GLS regression model used in this study. In the  
16 following four sub-sections, the necessary developments of different aspects of the GLS  
17 model are described in more detail. Firstly, the estimation of the covariance matrix of  
18 sampling errors is presented based on Taylor series approximations (so-called the delta  
19 method). Next, the estimation of the covariance matrix of the modelling errors is addressed.  
20 Then, the estimation of the regression model parameters by the maximum likelihood  
21 technique is described. Finally, three measures to assess the quality of the GLS regression  
22 model are presented.

### 23 **4.1 Covariance matrix of sampling errors**

24 The diagonal elements of  $\Sigma_{\epsilon}$  contain the sampling variance of the log-transformed T-year  
25 quantile of the at-site estimates (Eq. 6), which primarily depends on the frequency distribution  
26 used, the record-length, and the procedure to estimate its parameters. In this paper, Taylor  
27 series expansions were used to obtain approximate analytical solutions of these uncertainties,  
28 but other methods could also have been adopted such as jackknife resampling (Liu and Singh,  
29 1992) or bootstrapping (Efron and Tibshirani, 1993). In the case of the GEV distribution,  
30 which is the frequency distribution recommended in the Ebro River catchment by Jiménez-

1  $\acute{\text{A}}\text{lvarez et al. (2012)}$ , the asymptotic variance of the log-transformed quantile is given by Rao  
 2 and Hamed (2000) and shown in Eq. (11).

$$\begin{aligned}
 \sigma_{\varepsilon}^2(y) = & \left( \frac{\log_{10}(e)}{x_T} \right)^2 \left[ \left( \frac{\partial x_T}{\partial u} \right)^2 \sigma^2(u) + \left( \frac{\partial x_T}{\partial \alpha} \right)^2 \sigma^2(\alpha) + \left( \frac{\partial x_T}{\partial k} \right)^2 \sigma^2(k) \right. \\
 3 & + 2 \left( \frac{\partial x_T}{\partial u} \right) \left( \frac{\partial x_T}{\partial \alpha} \right) \text{cov}(u, \alpha) + 2 \left( \frac{\partial x_T}{\partial u} \right) \left( \frac{\partial x_T}{\partial k} \right) \text{cov}(u, k) \\
 & \left. + 2 \left( \frac{\partial x_T}{\partial \alpha} \right) \left( \frac{\partial x_T}{\partial k} \right) \text{cov}(\alpha, k) \right] \quad (11)
 \end{aligned}$$

4 where  $y$  is the log-transformed quantile defined in Eq. (1),  $u$ ,  $\alpha$  and  $k$  are the location, scale  
 5 and shape parameters, respectively, of the GEV distribution and  $e$  is Euler's number. The  
 6 T-year flood quantile,  $x_T$ , in the case of a GEV distribution is given by Eq. (12).

$$7 \quad x_T = u + \frac{\alpha}{k} \left[ 1 - \left( -\ln \left( 1 - \frac{1}{T} \right) \right)^k \right] \quad (12)$$

8 In the case when the shape parameter is estimated by a regional estimate of the L-coefficient  
 9 of skewness, L-CS, and considered a constant, Eq. (11) can be reduced to only three terms, as  
 10  $k$  is a constant (Eq. 13) (Lu and Stedinger, 1992). Further details on the analytical expressions  
 11 of the individual terms in Eq. (13) can be found in Appendix A.

$$12 \quad \sigma_{\varepsilon}^2(y) = \left( \frac{\log_{10}(e)}{x_T} \right)^2 \left[ \left( \frac{\partial x_T}{\partial u} \right)^2 \sigma^2(u) + \left( \frac{\partial x_T}{\partial \alpha} \right)^2 \sigma^2(\alpha) + 2 \left( \frac{\partial x_T}{\partial u} \right) \left( \frac{\partial x_T}{\partial \alpha} \right) \text{cov}(u, \alpha) \right] \quad (13)$$

13 The off-diagonal elements of  $\Sigma_{\varepsilon}$  describe the covariance between at-site estimates at different  
 14 sites to account for the fact that individual storms are more likely to affect neighbour  
 15 catchments than catchments located further apart. The covariance between log-transformed  
 16 quantiles at different sites is estimated using Eq. (14). Further details on the analytical  
 17 evaluation of this covariance term can be found in Appendix B.

$$18 \quad \Sigma_{\varepsilon,ij} = \text{cov}(y_i, y_j) = \frac{(\log_{10}(e))^2}{x_{T,i} x_{T,j}} \text{cov}(x_{T,i}, x_{T,j}) \quad (14)$$

19 When the L-moment method is used, correlations between probability weighted moments  
 20 (PWM) at two different sites are needed in order to estimate the off-diagonal elements of  $\Sigma_{\varepsilon}$   
 21 (Eq, B9-B11). As in previous studies, this correlation is assumed to be related to the

1 correlation between AMS by a power function as suggested by Eq. (15) (Stedinger, 1983;  
 2 Madsen and Rosbjerg, 1997; Martins and Stedinger, 2002).

$$3 \quad \rho_{b_{ri}, b_{rj}} = \rho_{ij}^{\delta} \quad (15)$$

4 where  $b_{ri}$  is the  $r$ th order PWM at site  $i$ ,  $\rho_{b_{ri}, b_{rj}}$  is the correlation between two  $r$ th order PWMs  
 5 at sites  $i$  and  $j$ ,  $\rho_{ij}$  is the correlation between AMS of peak flows at sites  $i$  and  $j$ , and  $\delta$  is the  
 6 exponent of  $\rho_{ij}$ , which is unknown.

7 A bootstrap experiment was carried out to estimate the values of  $\delta$  from the properties of  
 8 correlations between PWMs following the methodology used by Kjeldsen and Jones (2006).  
 9 For each pair of sites, the overlapping period was identified and a new sample was generated  
 10 by means of a bootstrap technique. A year is selected randomly with replacement from the  
 11 overlapped record. For each selected year the pair of associated annual maximum peak flow  
 12 observations is transferred to the bootstrap sample in order to keep the inter-site correlation.  
 13 The procedure is repeated until the synthetic sample length equals the overlapping length, and  
 14 finally, the PWMs are calculated from the synthetic samples. The procedure is repeated 1,000  
 15 times to estimate the correlation between PWM at different sites.

16 The final step involves the correlation between logarithmic values of AMS at different sites,  
 17  $\rho_{ij}$ , used to estimate  $\rho_{b_{ri}, b_{rj}}$ , which was smoothed by a double exponential expression (Eq. 16)  
 18 proposed by Kjeldsen and Jones (2009). .

$$19 \quad \rho_{\varepsilon, ij} = \varphi_{\varepsilon, 1} e^{-\varphi_{\varepsilon, 2} d_{ij}} + (1 - \varphi_{\varepsilon, 1}) e^{-\varphi_{\varepsilon, 3} d_{ij}} \quad (16)$$

20 where  $\rho_{\varepsilon, ij}$  is the smoothed correlation with distance between sites  $i$  and  $j$ ,  $d_{ij}$  is the distance  
 21 between centroids of catchments  $i$  and  $j$  (in km) and  $\varphi_{\varepsilon, 1}$ ,  $\varphi_{\varepsilon, 2}$  and  $\varphi_{\varepsilon, 3}$  are coefficients  
 22 estimated using the least squares technique.

## 23 **4.2 Covariance matrix of modelling errors**

24 The covariance matrix of the modelling errors,  $\Sigma_{\eta}$ , equals a matrix describing inter-site  
 25 correlations ( $\mathbf{R}_{\eta}$ ) scaled by the variance of modelling errors,  $\sigma_{\eta}^2$ , (Eq. 7-8). Therefore, the  
 26 diagonal elements of  $\Sigma_{\eta}$  describe the uncertainty in model estimations and are equal to the  
 27 variance of modelling errors ( $\sigma_{\eta}^2$ ). The off-diagonal elements of  $\Sigma_{\eta}$  describe the cross-  
 28 correlation of model errors between sites by  $\rho_{\eta, ij}$ , which is smoothed with distance between

1 sites following an expression similar to Eq. (16) with parameters  $\varphi_{\eta,1}$ ,  $\varphi_{\eta,2}$  and  $\varphi_{\eta,3}$ .

$$2 \quad \rho_{\eta,ij} = \varphi_{\eta,1} \exp(\varphi_{\eta,2}d) + (1 - \varphi_{\eta,1}) \exp(\varphi_{\eta,3}d)$$

### 3 **4.3 Estimation of regression model parameters**

4 The proposed model has several unknown parameters: the  $m+1$  parameters of the regression  
 5 model ( $\theta$ ), the variance of the model errors ( $\sigma_{\eta}^2$ ) and the three parameters describing the  
 6 model error correlation with distance ( $\varphi_{\eta,1}$ ,  $\varphi_{\eta,2}$  and  $\varphi_{\eta,3}$ ). All these parameters can be  
 7 estimated by the maximum likelihood technique, assuming that regression residuals follow a  
 8 normal distribution with mean equal to zero and variance given by the covariance matrix  $\Sigma_{\omega}$   
 9 (Kjeldsen and Jones, 2009) (Eq. 17). The negative log-likelihood function,  $-ln(L)$ , for the  
 10 regression model is given by Eq. (18), and is minimised to estimate the model parameter  
 11 values.

$$12 \quad \Sigma_w = \Sigma_{\varepsilon} + \Sigma_{\eta} = \Sigma_{\varepsilon} + \sigma_{\eta}^2 \mathbf{R}_{\eta} = \sigma_{\eta}^2 (\Sigma_{\varepsilon} / \sigma_{\eta}^2 + \mathbf{R}_{\eta}) = \sigma_{\eta}^2 \mathbf{G} \quad (17)$$

$$13 \quad -2ln(L) = ln[\det(\sigma_{\eta}^2 \mathbf{G})] + (\mathbf{y} - \mathbf{X}\theta)^T (\sigma_{\eta}^2 \mathbf{G})^{-1} (\mathbf{y} - \mathbf{X}\theta) \quad (18)$$

14 In practice, the number of unknown parameters can be reduced, as for given values of  $\sigma_{\eta}^2$  and  
 15  $\varphi_{\eta,1}$ ,  $\varphi_{\eta,2}$  and  $\varphi_{\eta,3}$  the regression model parameters that minimise the negative log-likelihood  
 16 function are given by the GLS estimator (Eq. 19). Therefore, the unknown parameters of the  
 17 log-likelihood function are reduced to four:  $\sigma_{\eta}^2$ ,  $\varphi_{\eta,1}$ ,  $\varphi_{\eta,2}$  and  $\varphi_{\eta,3}$ .

$$18 \quad \hat{\theta} = (\mathbf{X}^T \mathbf{G}^{-1} \mathbf{X})^{-1} \mathbf{X}^T \mathbf{G}^{-1} \mathbf{y} \quad (19)$$

### 19 **4.4 Measures to select the regression model**

20 Once a regression model with  $m$  catchment descriptors is fitted to the observations, a  
 21 multicollinearity test should be applied to avoid the inclusion of linear related covariates. The  
 22 variance inflation factor ( $VIF$ ) was used, as it is a common test of multicollinearity (Eq. 20).

$$23 \quad VIF_j = \frac{1}{(1 - R_j^2)} \quad (20)$$

24 where  $R_j^2$  is the determination coefficient between the  $j$ th catchment descriptor and the  
 25 remaining  $m-1$  catchment descriptors used in the regression model. Multicollinearity arises  
 26 when  $VIF$  exceeds a value of five (Montgomery et al., 2012).

1 Griffis and Stedinger (2007) suggested the standard error of prediction (*SEP*) of the true flood  
 2 quantiles as a useful tool to compare regression models (Eq. 21).

$$3 \quad SEP = \sqrt{10^{\ln(10)AVP_{GLS}} - 1} \quad (21)$$

$$4 \quad AVP_{GLS} = \sigma_{\eta}^2 + \frac{1}{N} \sum_{i=1}^N \mathbf{x}_i (\mathbf{X}^T \Sigma_w^{-1} \mathbf{X})^{-1} \mathbf{x}_i^T \quad (22)$$

5 where  $AVP_{GLS}$  is the average variance of prediction for a *GLS* regression model (Eq. 22)  
 6 across all the  $N$  gauging stations used in the regression model and  $\mathbf{x}_i$  is a row vector with the  
 7 catchment descriptors used in the regression model at site  $i$ . Lower values of  $AVP_{GLS}$  and *SEP*  
 8 suggest a more accurate regression model.

9 In addition, the improvement of a more complex GLS model when compared to a simpler  
 10 OLS model should be quantified to decide when the more complex model can be accepted.  
 11 For this purpose, the error variance ratio (*EVR*) was adopted to quantify the relationship  
 12 between the magnitude of the average sampling variance and the magnitude of the model  
 13 error variance (Eq. 23). Griffis and Stedinger (2007) argue that an OLS model should be used  
 14 when *EVR* is greater than 0.2, as the sampling error is negligible compared to the modelling  
 15 error .

$$16 \quad EVR = \frac{tr(\hat{\Sigma})}{N \sigma_{\eta}^2(m)} \quad (23)$$

17 where  $tr(\hat{\Sigma})$  is the trace of the covariance matrix of the sampling errors and  $\sigma_{\eta}^2(m)$  is the  
 18 variance of modelling errors for the regression model with  $m$  catchment descriptors.

19

## 20 **5 Results**

21 This section is composed of two sub-sections. Firstly, the results about the implementation of  
 22 the proposed GLS technique with a view to the existing recommendations given in Spain to  
 23 estimate the frequency distribution is presented. Then, the application of the GLS regression  
 24 model to the semi-arid Ebro River catchment is documented.

## 1 **5.1 Specification of sampling and model error structures**

### 2 **5.1.1 Assessment of sampling variance based on Taylor series**

3 The accuracy of the analytical expressions of the variance of the flood quantile estimates  
4 based on the Taylor series approximations (Appendix A) was assessed through a Monte Carlo  
5 experiment. A set of random synthetic series with varying sample lengths from 10 to 100 was  
6 generated from a GEV distribution. Five experiments were conducted, one for each  
7 homogeneous region in the Ebro River catchment. The regional growth curve was used in  
8 each homogeneous region, with L-mean equal to one and the regional values of L-CV and L-  
9 CS given in Table 1. A total of 10,000 random realisations were generated for each case.

10 The results of the Monte Carlo experiment (Fig. 2) show the Taylor series approximation fits  
11 the sampling variance estimated by Monte Carlo simulations almost perfectly for the three  
12 return periods in Regions 91, 92, 93 and 95, except some slight deviations for shorter record-  
13 lengths in Regions 92 and 94. In Region 93, the analytical expressions overestimate the  
14 sampling variance, mainly for the case of smaller record lengths. These deviations can be  
15 explained by the sharp curvature of the frequency distribution in this region, given by a low  
16 shape parameter (Table 1) that leads to large uncertainties in quantile estimates. All the  
17 gauging stations used in the Ebro River catchment exceed 20 years of record-length. As the  
18 main purpose of the variance-covariance estimates is to give relative weight to the different  
19 sites in the GLS model framework, the performances of the Taylor series approximations  
20 were considered adequate for the purpose of this study.

### 21 **5.1.2 Correlation of sampling errors**

22 The off-diagonal elements of  $\Sigma_{\epsilon}$  represent the sampling covariance between quantiles at  
23 different sites (Eq. 14). Evaluation of these non-diagonal elements requires a functional  
24 relationship between the correlation of the observed flood series and the corresponding  
25 correlation between the PWMs as expressed in Eq. (15). The bootstrap experiment described  
26 in Section 3.1 was executed on the set of 93 gauging stations selected in the Ebro River  
27 catchment. The procedure was repeated 1,000 times to estimate the correlation at different  
28 sites. Figure 3 shows the correlation between AMF series at each pair of sites against the  
29 correlation between PWMs. The results suggest a linear relationship for the case of the first  
30 two order PWMs. Consequently, it is concluded that the value of the power  $\delta$  used in Eq. 15 is  
31 equal to one for all the combinations between the first two order PWM.

1 Next, the three coefficients ( $\varphi_{e,i}$ ) of the double exponential expression (Eq. 16) were estimated  
2 from the AMF data at the 93 observed sites in the Ebro River catchment using a simple least  
3 squares approach. Pairs of gauge stations with an overlapping record exceeding 30 years were  
4 selected to fit the model. The results are reported in Table 2 and the fitted model is shown in  
5 Fig. 4.

## 6 **5.2 Development of a GLS regression model in the Ebro River catchment**

7 Once the covariance matrices of the sampling were obtained, the parameters of a number of  
8 alternative regression models were estimated for the Ebro River catchment.

9 Firstly, the results of the GLS regression model were compared to the results of the existing  
10 OLS regression models developed by Jiménez-Álvarez et al. (2012). This comparison was  
11 conducted on the homogeneous regions 91 and 92. Following on, the results of applying the  
12 GLS regression model in these regions were improved using additional catchment descriptors.  
13 Finally, an exploratory analysis was carried out to obtain a GLS regression model of the entire  
14 Ebro River catchment, aiming to capture its great heterogeneities by a single model.

### 15 **5.2.1 GLS regression model applied to the Region 91**

16 The Region 91 has observed data from 34 gauging stations. Firstly, a GLS regression model  
17 was compared to the existing OLS model using the same catchment descriptors: A,  $P_T$ , H and  
18  $t_{inf}$ . Adopting the GLS model leads to a decrease of 3-5% in the *SEP* (Table 3). However, the  
19 regression parameters are very similar. The benefits of the GLS model from the OLS model  
20 were quantified by the *EVR* measure. The three GLS models selected improve the existing  
21 OLS models, as *EVR* is positive for the three return periods. However, *EVR* is smaller than  
22 20%, showing that the sampling error is negligible compared to the GLS modelling error.  
23 Consequently, the OLS could be preferred in this case, as the use of a more complex GLS  
24 model does not lead to a sufficient improvement from the more simple OLS model.  
25 Nevertheless, the developed GLS regression model is a powerful tool that takes into account  
26 the sampling variance of quantile estimations, the spatial correlation of quantiles between  
27 sites, the error of the regression model and the spatial correlation of residuals. Additional  
28 catchment descriptors were introduced in the analysis to improve the initial results of the GLS  
29 regression model.



1 In this region, climatic differences among catchments are almost negligible. On one hand,  $IC$   
2 provides information about the soil storage capacity and the existence of aquifers. On the  
3 other, as  $P_T$  shows a small variability,  $I_e$  gives information about the initial moisture content  
4 before the flood event. In addition, PET was also included in the two-year return period  
5 regression model.

6 The results of the GLS regression model in Region 91 are shown in Table 4. Small modelling  
7 errors are achieved for the three return periods (Fig. 5).  $SEP$  was reduced to 15-20% from the  
8 30-40% obtained by the OLS model. This is a significant improvement of the GLS regression  
9 model. Furthermore, the  $EVR$  results show values around 40%, which indicates that the  
10 sampling error variance cannot be neglected compared to the modelling error variance.  
11 Consequently, the improved GLS regression model is preferred to the existing OLS model in  
12 the Region 91 of the Ebro River catchment. In addition, no linear related covariates were  
13 found in this region, as  $VIF$  values are smaller than five in all the models (Table 5).

14 The evolution of spatial correlation of modelling errors is also shown in Fig. 6. The  
15 introduction of  $P_T$  into the regression model leads to a significant reduction of the spatial  
16 correlation between residuals, thus suggesting a more complete description of the processes  
17 controlling the between-sites variation in flood quantiles. Furthermore, the introduction of the  
18 last descriptor into the regression models leads to the lowest spatial correlation. It should be  
19 noted the inclusion of  $H$  was considered worthwhile, as its introduction removes almost  
20 completely the correlation of residuals with distance.

### 21 5.2.2 GLS regression model applied to the Region 92

22 The Region 92 has observed data from 25 gauging stations. Firstly, a GLS regression model  
23 was constructed and compared to the existing OLS model using the same set of catchment  
24 descriptors:  $A$ ,  $P_T$  and  $A_{1500}$ . The results show that the GLS model leads to a reduction of  
25 6-9% in the  $SEP$  for the return periods of 25 and 100 years when compared to the benchmark  
26 performance of the existing OLS model (Table 3). In addition, the GLS models for 25 and  
27 100 years are preferred to the existing OLS models in terms of  $EVR$ , as sampling errors are  
28 more than 100% greater than modelling errors. However, for the case of a return period of  
29 two years, the OLS model is preferred, as the GLS model worsens the  $SEP$ .

30 In this region, the existing regression models were improved by introducing the initial  
31 abstraction,  $P_0$ , to explain differences in runoff production. Once the portion of precipitation

1 transformed into runoff is considered in the regression model, the concavity index,  $IC$ , was  
2 introduced to account for the relationship between surface and subsurface processes in the  
3 catchment.

4 The results of the improved GLS regression model in the Region 92 are presented in Table 6.  
5 A reduction of modelling errors is obtained as additional catchment descriptors are included  
6 in the model (Fig. 5). The  $SEP$  values obtained using the GLS model halved those of the  
7 existing OLS regression models, obtaining values around 20-25%. In this region, adopting the  
8 GLS regression model leads to a significant improvement compared to the OLS model for  
9 return periods of 25 and 100 years. The GLS model is clearly preferred to the OLS for all  
10 combinations of catchment descriptors, even for the model with only the catchment area.  
11 Furthermore, regression models with six parameters lead to small  $EVR$  values, i.e., small  
12 modelling variances are achieved compared to the mean sampling variance. However, the  
13 GLS model for the two-year return period requires at least five descriptors to be preferred to  
14 the OLS model, as the regression model errors show a slight increase with respect to the rest  
15 of return periods. Nevertheless, the GLS regression model improves significantly the results  
16 of the OLS model and  $SEP$  is reduced to 25%. In addition, no linear related covariates were  
17 found in this region, as  $VIF$  values are smaller than five in all the models (Table 7).

18 The introduction of the initial abstraction,  $P_0$ , leads to an almost complete eradication of the  
19 cross correlation between model error residuals (Fig. 6), suggesting that this descriptor  
20 effectively explains the local differences between flood series not otherwise captured by the  
21 scale and climate descriptors.

### 22 5.2.3 A GLS regression model for the entire Ebro River catchment

23 A GLS regression model was fitted to the 93 gauging stations of the Ebro River catchment,  
24 with the aim of capturing its great heterogeneities by a single model. In this case, the aridity  
25 index ( $I_a$ ) was found to explain much of the remaining spatial clustering of the regression  
26 residuals when the effects of both catchment area ( $A$ ) and extreme rainfall ( $P_T$ ) have been  
27 taken into account. In the central part of the catchment there exists a large area characterised  
28 as being semi-arid, while sub-humid climate areas can be found at the catchment boundaries,  
29 and small humid climate areas are observed in the Pyrenees. However, for the case of the two-  
30 year return period,  $P_m$  explains better the differences in the magnitude of floods.

1 The results of the GLS regression model for the entire Ebro River catchment are shown in  
2 Table 8. The GLS model gives *SEP* values around 30%, which means that the GLS model for  
3 the entire Ebro River catchment captures its spatial heterogeneities in the regional hydrology  
4 and leads to a good description of the flood processes. However, the results are slightly larger  
5 than those of the GLS models applied individually to the homogeneous regions 91 and 92.  
6 Consequently, a GLS model fitted to a given homogeneous region with a reduced number of  
7 sites leads to more accurate results, as it was expected. Nevertheless, the GLS model for the  
8 entire basin also improves the results of the OLS model. In addition, no linear related  
9 covariates were found in this region, as *VIF* values are smaller than five in all the models  
10 (Table 9).

11

## 12 **6 Conclusions**

13 A regional flood frequency hydrology analysis was carried out focusing on the spatial  
14 expansion of information by a regression model based on the generalised least squares  
15 technique, where inter-site correlations of both sampling and modelling errors were explicitly  
16 accounted for in the error structure of the regression model. The regression model was  
17 developed following the existing recommendations in Spain for estimating flood frequency  
18 curves: (i) a Generalised Extreme Value distribution fitted by the L-moment estimation  
19 method; (ii) at-site estimations of both location and scale parameters and regional estimation  
20 of the shape parameter. The covariance matrix of sampling errors was adapted to reflect these  
21 assumptions case.

22 The semi-arid Ebro River catchment located in Spain was selected as case study because  
23 previous studies encountered great heterogeneities of climate drivers, rainfall patterns and soil  
24 characteristics among sub-regions.

25 An exploratory analysis on catchment descriptors was conducted to explain differences in  
26 flood processes among catchments. The results showed that differences in T-year peak flow  
27 estimates between catchments were mainly explained by: (i) catchment area, which is the  
28 main driver of the flood magnitude; (ii) One day T-year design rainfall, which is the main  
29 driver of the differences in flood magnitude between catchments with similar catchment area;  
30 (iii) the concavity index, which characterises the split between fast surface runoff and slow  
31 subsurface flow based on the FDC; (iv) mean catchment slope, which explains differences  
32 due to the topography that have influence on the runoff velocity in hillslopes; (v) the

1 extremity index, which in the Ebro River catchment gives information about the influence of  
 2 antecedent precipitation on probable initial moisture content before the onset of flood events;  
 3 (vi) potential evapotranspiration, which gives a better description of the probable initial  
 4 moisture content; (vii) the precipitation depth absorbed by the soil before runoff begins,  
 5 which explains differences caused by the hydrologic abstraction process.

6 Summarising, the use of these catchment descriptors in a generalised least squares regression  
 7 model improved the results of the existing ordinary least squares regression models, in terms  
 8 of variance of modelling errors and standard error of prediction. In addition, most of the  
 9 regression models removed almost completely the spatial correlation of residuals, which  
 10 suggests a satisfactory description of the flood processes that controls quantile variations  
 11 between sites. Consequently, the generalised least squares regression model developed in this  
 12 paper can be used for making more reliable predictions in ungauged catchments with the  
 13 purpose of both designing hydraulic infrastructures at sites without observed information, and  
 14 thus improving flood risk management.

15

## 16 **Appendix A: Variance and covariance of the GEV parameters for the case of a** 17 **constant shape parameter**

18 In the case of a GEV distribution, the asymptotic variance of  $x_T$  for a constant shape  
 19 parameter can be simplified by Eq. 11. In terms of L-moments, the remaining two parameters  
 20 of the GEV distribution can be estimated by Equations A1 and A2.

$$21 \quad \alpha = \frac{\lambda_2 k}{(1 - 2^{-k})\Gamma(1+k)} = \lambda_2 K_1 \quad (A1)$$

$$22 \quad u = \lambda_1 - \frac{\alpha}{k}(1 - \Gamma(1+k)) = \lambda_1 - \alpha K_2 = \lambda_1 - \lambda_2 K_1 K_2 \quad (A2)$$

23 where  $\lambda_1$  and  $\lambda_2$  are the first two L-moments,  $\Gamma$  is the gamma function and  $K_1$  and  $K_2$  are  
 24 constants for a given  $k$  parameter (Equations A3 and A4).

$$25 \quad K_1 = \frac{k}{(1 - 2^{-k})\Gamma(1+k)} \quad (A3)$$

$$26 \quad K_2 = \frac{1 - \Gamma(1+k)}{k} \quad (A4)$$

1 Therefore, the variance and covariance of  $u$  and  $\alpha$  parameters, for a given  $k$  parameter in Eq.  
 2 (11), are derived as follows in terms of L-moments:

$$\begin{aligned}
 \sigma^2(u) &= \text{var}(u) = \left(\frac{\partial u}{\partial \lambda_1}\right)^2 \text{var}(\lambda_1) + \left(\frac{\partial u}{\partial \lambda_2}\right)^2 \text{var}(\lambda_2) + 2 \left(\frac{\partial u}{\partial \lambda_1}\right) \left(\frac{\partial u}{\partial \lambda_2}\right) \text{cov}(\lambda_1, \lambda_2) \\
 &= \text{var}(\lambda_1) + \left(\frac{\partial u}{\partial \lambda_2}\right)^2 \text{var}(\lambda_2) + 2 \left(\frac{\partial u}{\partial \lambda_2}\right) \text{cov}(\lambda_1, \lambda_2)
 \end{aligned}
 \tag{A5}$$

$$\begin{aligned}
 \sigma^2(\alpha) &= \text{var}(\alpha) = \left(\frac{\partial \alpha}{\partial \lambda_1}\right)^2 \text{var}(\lambda_1) + \left(\frac{\partial \alpha}{\partial \lambda_2}\right)^2 \text{var}(\lambda_2) \\
 &+ 2 \left(\frac{\partial \alpha}{\partial \lambda_1}\right) \left(\frac{\partial \alpha}{\partial \lambda_2}\right) \text{cov}(\lambda_1, \lambda_2) = \left(\frac{\partial \alpha}{\partial \lambda_2}\right)^2 \text{var}(\lambda_2)
 \end{aligned}
 \tag{A6}$$

$$\begin{aligned}
 \text{cov}(u, \alpha) &= \left(\frac{\partial u}{\partial \lambda_1}\right) \left(\frac{\partial \alpha}{\partial \lambda_1}\right) \text{var}(\lambda_1) + \left(\frac{\partial u}{\partial \lambda_2}\right) \left(\frac{\partial \alpha}{\partial \lambda_2}\right) \text{var}(\lambda_2) \\
 &+ \left(\frac{\partial u}{\partial \lambda_1}\right) \left(\frac{\partial \alpha}{\partial \lambda_2}\right) \text{cov}(\lambda_1, \lambda_2) + \left(\frac{\partial u}{\partial \lambda_2}\right) \left(\frac{\partial \alpha}{\partial \lambda_1}\right) \text{cov}(\lambda_1, \lambda_2) \\
 &= \left(\frac{\partial u}{\partial \lambda_2}\right) \left(\frac{\partial \alpha}{\partial \lambda_2}\right) \text{var}(\lambda_2) + \left(\frac{\partial \alpha}{\partial \lambda_2}\right) \text{cov}(\lambda_1, \lambda_2)
 \end{aligned}
 \tag{A7}$$

6 The variance and covariance of the first two L-moments can be obtained by Eq. A8 (Elamir  
 7 and Seheult, 2004).

$$\text{var}(\lambda) = \begin{bmatrix} \text{var}(\lambda_1) & \text{cov}(\lambda_1, \lambda_2) \\ \text{cov}(\lambda_1, \lambda_2) & \text{var}(\lambda_2) \end{bmatrix} = C \Theta C^T
 \tag{A8}$$

9 where:

$$\Theta = \begin{bmatrix} \text{var}(b_0) & \text{cov}(b_0, b_1) \\ \text{cov}(b_0, b_1) & \text{var}(b_1) \end{bmatrix}
 \tag{A9}$$

$$C = \begin{bmatrix} 1 & 0 \\ -1 & 2 \end{bmatrix}
 \tag{A10}$$

12 where  $\text{var}(b_0)$ ,  $\text{var}(b_1)$  and  $\text{cov}(b_0, b_1)$  can be estimated as follows (Hosking et al., 1985):

$$\text{var}(b_0) = \frac{\alpha^2}{n k^2} [\Gamma(1+2k) - \Gamma^2(1+k)]
 \tag{A11}$$

$$1 \quad \text{var}(b_1) = \frac{2^{-2k} \alpha^2}{n k^2} [\Gamma(1+2k) q(k) - \Gamma^2(1+k)] \quad (\text{A12})$$

$$2 \quad \text{cov}(b_0, b_1) = \frac{\alpha^2}{2 n k^2} [2^{-2k} \Gamma(1+2k) + (1-2^{1-k}) \Gamma^2(1+k)] \quad (\text{A13})$$

3 where:

$$4 \quad q(k) = 1 + \frac{2 k^2}{\Gamma(1+2k)} \sum_{i=1}^{\infty} \left( \frac{\Gamma(2k+i)}{k+i} \frac{(-1/2)^i}{i!} \right) \quad (\text{A14})$$

5

## 6 **Appendix B: Covariance between GEV quantiles at different sites**

7 The covariance between GEV quantiles at different sites with a constant shape parameter can  
8 be obtained by Eq. B1.

$$9 \quad \begin{aligned} \text{cov}(x_{T,i}, x_{T,j}) &= \left( \frac{\partial x_{T,i}}{\partial u_i} \right) \left( \frac{\partial x_{T,j}}{\partial u_j} \right) \text{cov}(u_i, u_j) + \left( \frac{\partial x_{T,i}}{\partial u_i} \right) \left( \frac{\partial x_{T,j}}{\partial \alpha_j} \right) \text{cov}(u_i, \alpha_j) \\ &+ \left( \frac{\partial x_{T,i}}{\partial \alpha_i} \right) \left( \frac{\partial x_{T,j}}{\partial u_j} \right) \text{cov}(\alpha_i, u_j) + \left( \frac{\partial x_{T,i}}{\partial \alpha_i} \right) \left( \frac{\partial x_{T,j}}{\partial \alpha_j} \right) \text{cov}(\alpha_i, \alpha_j) \end{aligned} \quad (\text{B1})$$

10 As the partial derivative of  $x_T$  with respect to the location parameter equals one, Eq. B1 can be  
11 simplified to Eq. B2.

$$12 \quad \begin{aligned} \text{cov}(x_{T,i}, x_{T,j}) &= \text{cov}(u_i, u_j) + \left( \frac{\partial x_{T,j}}{\partial \alpha_j} \right) \text{cov}(u_i, \alpha_j) + \left( \frac{\partial x_{T,i}}{\partial \alpha_i} \right) \text{cov}(\alpha_i, u_j) \\ &+ \left( \frac{\partial x_{T,i}}{\partial \alpha_i} \right) \left( \frac{\partial x_{T,j}}{\partial \alpha_j} \right) \text{cov}(\alpha_i, \alpha_j) \end{aligned} \quad (\text{B2})$$

13 The covariance between  $u$  and  $\alpha$  parameters for a given  $k$  parameter can be obtained as  
14 follows, in terms of L-moments:

$$15 \quad \begin{aligned} \text{cov}(u_i, u_j) &= \text{cov}(\lambda_{1,i} - \lambda_{2,i} K_{1,i} K_{2,i}, \lambda_{1,j} - \lambda_{2,j} K_{1,j} K_{2,j}) \\ &= \text{cov}(\lambda_{1,i}, \lambda_{1,j}) + K_{1,i} K_{2,i} K_{1,j} K_{2,j} \text{cov}(\lambda_{2,i}, \lambda_{2,j}) \\ &\quad - K_{1,j} K_{2,j} \text{cov}(\lambda_{1,i}, \lambda_{2,j}) - K_{1,i} K_{2,i} \text{cov}(\lambda_{2,i}, \lambda_{1,j}) \end{aligned} \quad (\text{B3})$$

$$16 \quad \text{cov}(\alpha_i, \alpha_j) = \text{cov}(\lambda_{2,i} K_{1,i}, \lambda_{2,j} K_{1,j}) = K_{1,i} K_{1,j} \text{cov}(\lambda_{2,i}, \lambda_{2,j}) \quad (\text{B4})$$

$$\begin{aligned}
1 \quad & \text{cov}(u_i, \alpha_j) = \text{cov}(\lambda_{1,i} - \lambda_{2,i} K_{1,i} K_{2,i}, \lambda_{2,j} K_{1,j}) \\
& = K_{1,j} \text{cov}(\lambda_{1,i}, \lambda_{2,j}) - K_{1,i} K_{2,i} K_{1,j} \text{cov}(\lambda_{2,i}, \lambda_{2,j})
\end{aligned} \tag{B5}$$

2 where  $K_1$  and  $K_2$  are given in Equations A3 and A4. Covariance between L-moments can be  
3 obtained in terms of PWM as follows:

$$4 \quad \text{cov}(\lambda_{1,i}, \lambda_{1,j}) = \text{cov}(b_{0,i}, b_{0,j}) \tag{B6}$$

$$\begin{aligned}
5 \quad & \text{cov}(\lambda_{2,i}, \lambda_{2,j}) = \text{cov}(2b_{1,i} - b_{0,i}, 2b_{1,j} - b_{0,j}) \\
& = 4 \text{cov}(b_{1,i}, b_{1,j}) - 2 \text{cov}(b_{1,i}, b_{0,j}) - 2 \text{cov}(b_{0,i}, b_{1,j}) + \text{cov}(b_{0,i}, b_{0,j})
\end{aligned} \tag{B7}$$

$$6 \quad \text{cov}(\lambda_{1,i}, \lambda_{2,j}) = \text{cov}(b_{0,i}, 2b_{1,j} - b_{0,j}) = 2 \text{cov}(b_{0,i}, b_{1,j}) - \text{cov}(b_{0,i}, b_{0,j}) \tag{B8}$$

7 where covariance between PWM can be obtained by the following expressions:

$$8 \quad \text{cov}(b_{0,i}, b_{0,j}) = \sqrt{\text{var}(b_{0,i})} \sqrt{\text{var}(b_{0,j})} \frac{m_{ij}}{n_i n_j} \rho_{b_{0i}, b_{0j}} \tag{B9}$$

$$9 \quad \text{cov}(b_{1,i}, b_{1,j}) = \sqrt{\text{var}(b_{1,i})} \sqrt{\text{var}(b_{1,j})} \frac{m_{ij}}{n_i n_j} \rho_{b_{1i}, b_{1j}} \tag{B10}$$

$$10 \quad \text{cov}(b_{0,i}, b_{1,j}) = \sqrt{\text{var}(b_{0,i})} \sqrt{\text{var}(b_{1,j})} \frac{m_{ij}}{n_i n_j} \rho_{b_{0i}, b_{1j}} \tag{B11}$$

11 where  $m_{ij}$  is the number of overlapping years between sites  $i$  and  $j$ ,  $n_i$  and  $n_j$  are record-lengths  
12 at sites  $i$  and  $j$  respectively, and  $\rho_{b_{ri}, b_{rj}}$  is the correlation between the  $r$ th order PWMs at sites  $i$   
13 and  $j$  given by Eq. 15.

14

## 15 **Acknowledgements**

16 The authors thank the financial contribution made by the COST Office grant ES0901  
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19

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- 24

1 Figure 1. Location of the Ebro River catchment. Solid points show location of the gauging  
2 stations used in the study.

3

4 Figure 2. Comparison between sampling variance estimated by Monte Carlo simulations and  
5 the analytical solution estimated by Taylor series approximation. Regions by rows: a) Region  
6 91; b) Region 92; c) Region 93; d) Region 94; e) Region 95. Return period by columns: 1)  
7 two years; 2) 25 years; 3) 100 years

8

9 Figure 3. Correlation between AMF series and PWMs. a) Between first-order PWMs ( $b_0$ ); b)  
10 between second-order PWMs ( $b_1$ ); c) between first-order and second-order PWMs ( $b_0$  and  $b_1$ )

11

12 Figure 4. Correlation between AMF series and distance between catchment centroids for the  
13 93 flood series from the Ebro catchment. Solid line shows the double exponential function  
14 fitted using the least square technique.

15

16 Figure 5. Evolution of the variance of modelling errors,  $\sigma^2_\eta$ . Regions by rows: a) Region 91;  
17 b) Region 92; c) Entire Ebro River catchment.

18

19 Figure 6. Evolution of correlation of residuals with distance between sites in  $\text{km}^2$ . Regions by  
20 rows: a) Region 91; b) Region 92; c) Entire Ebro River catchment. Return period by column:  
21 1) two years; 2) 25 years; 3) 100 years.

22

Figure 1  
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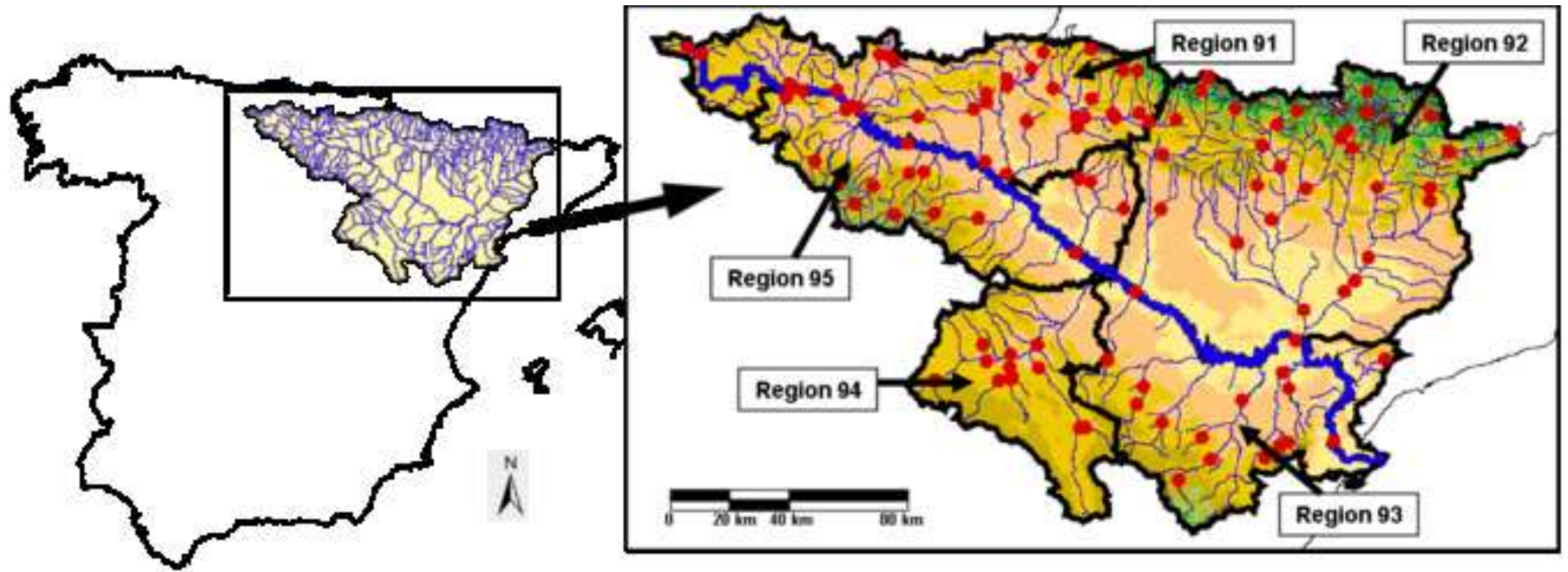


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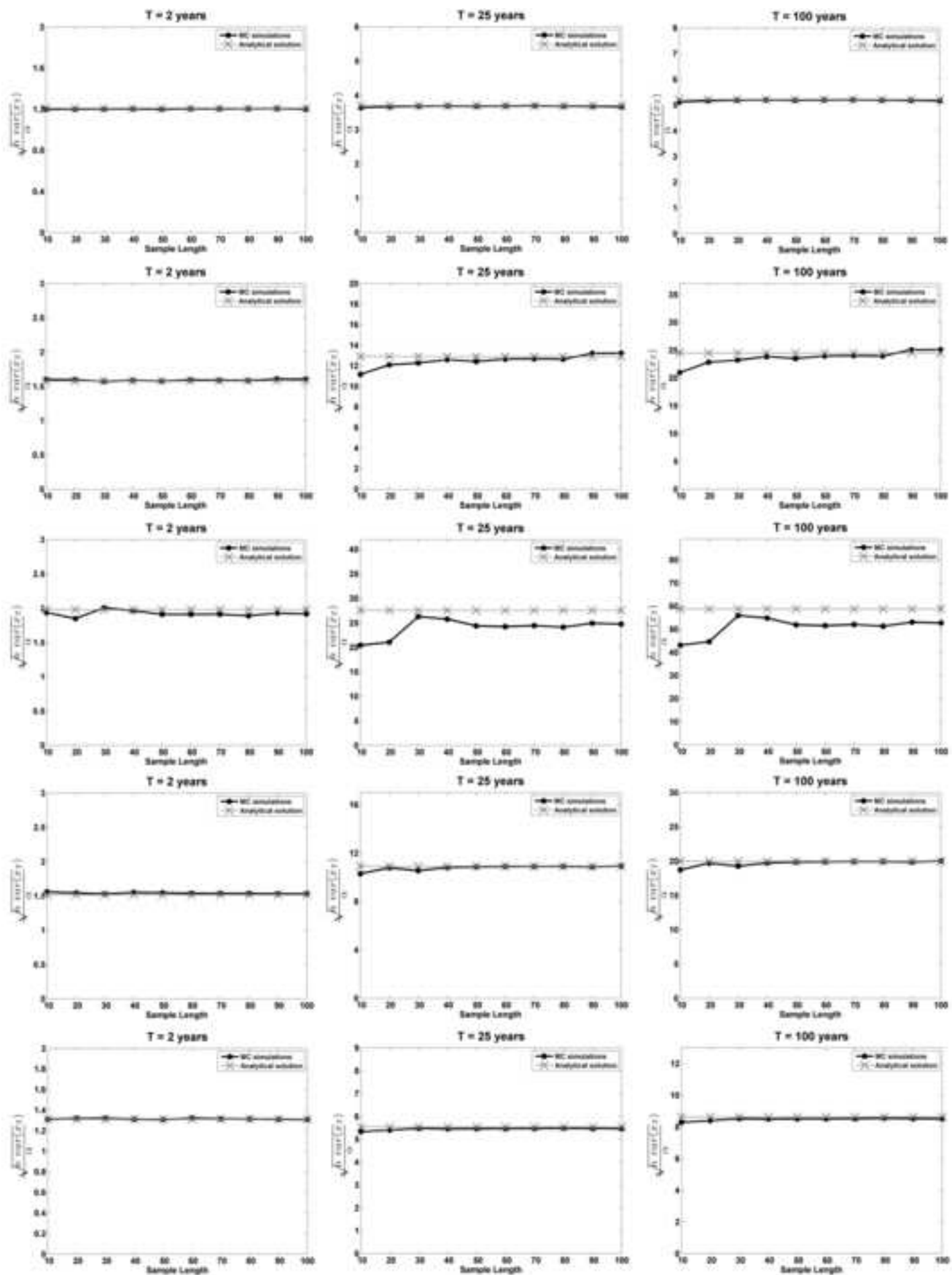


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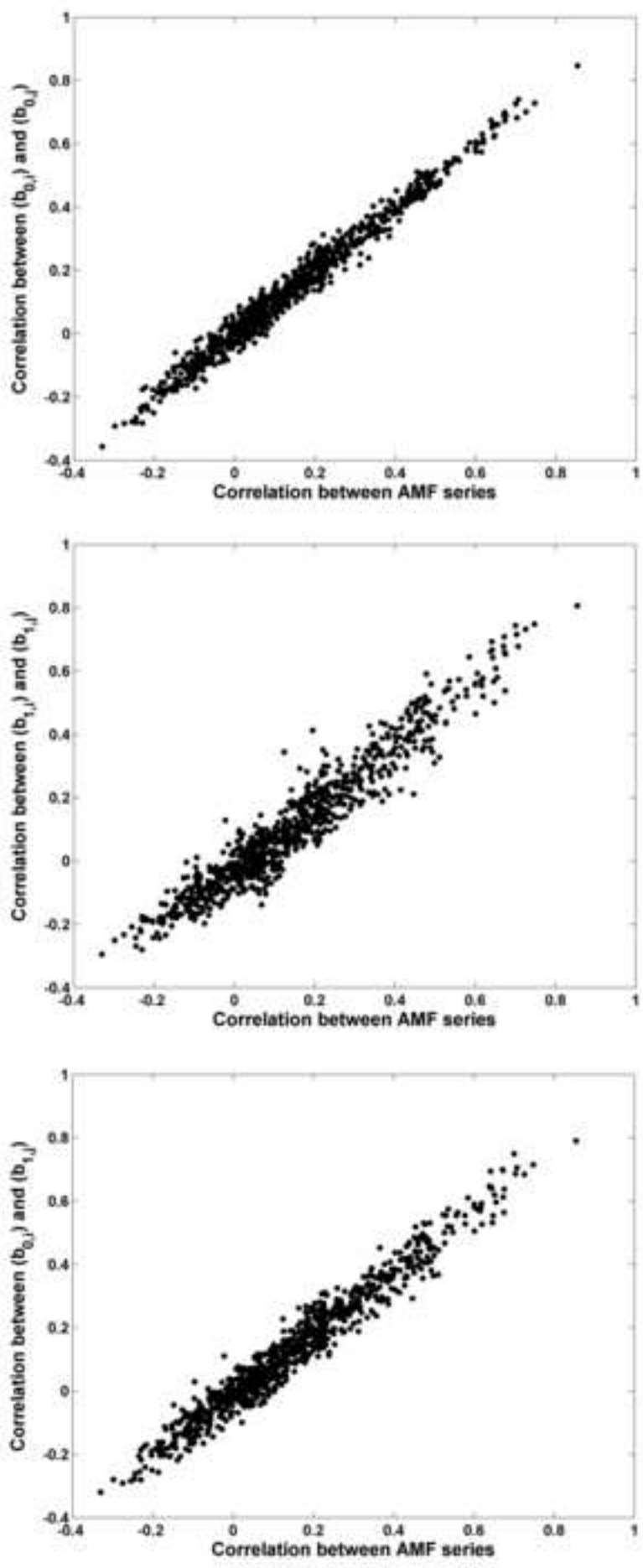


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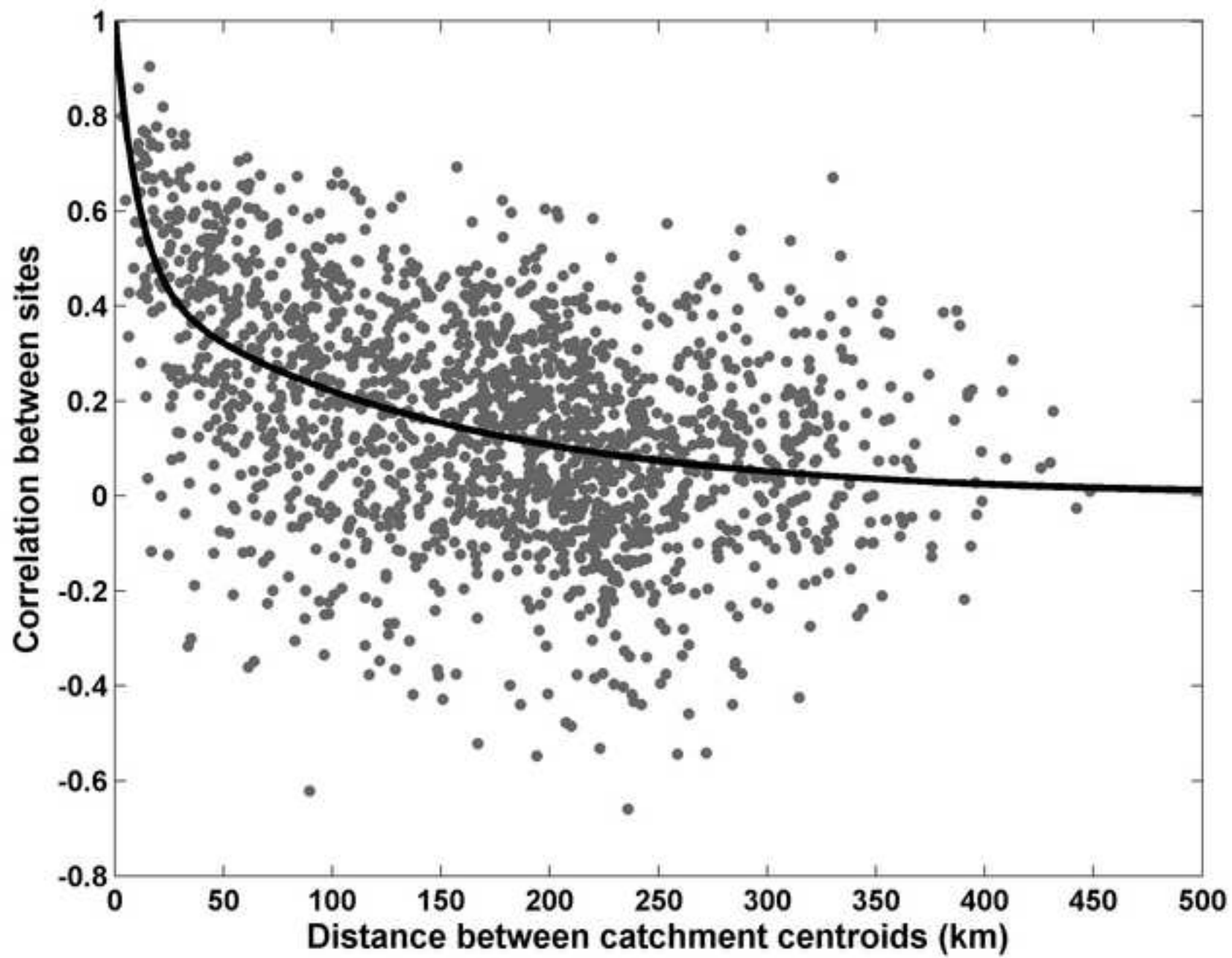


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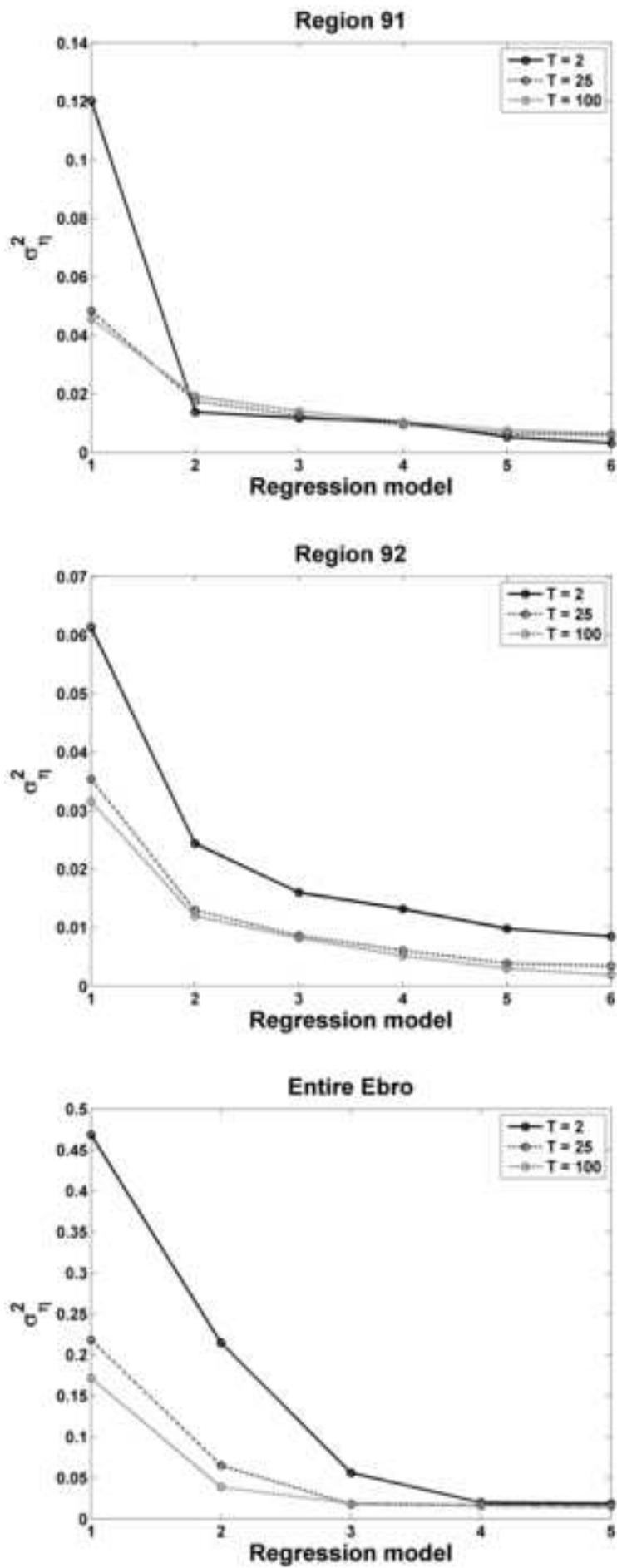
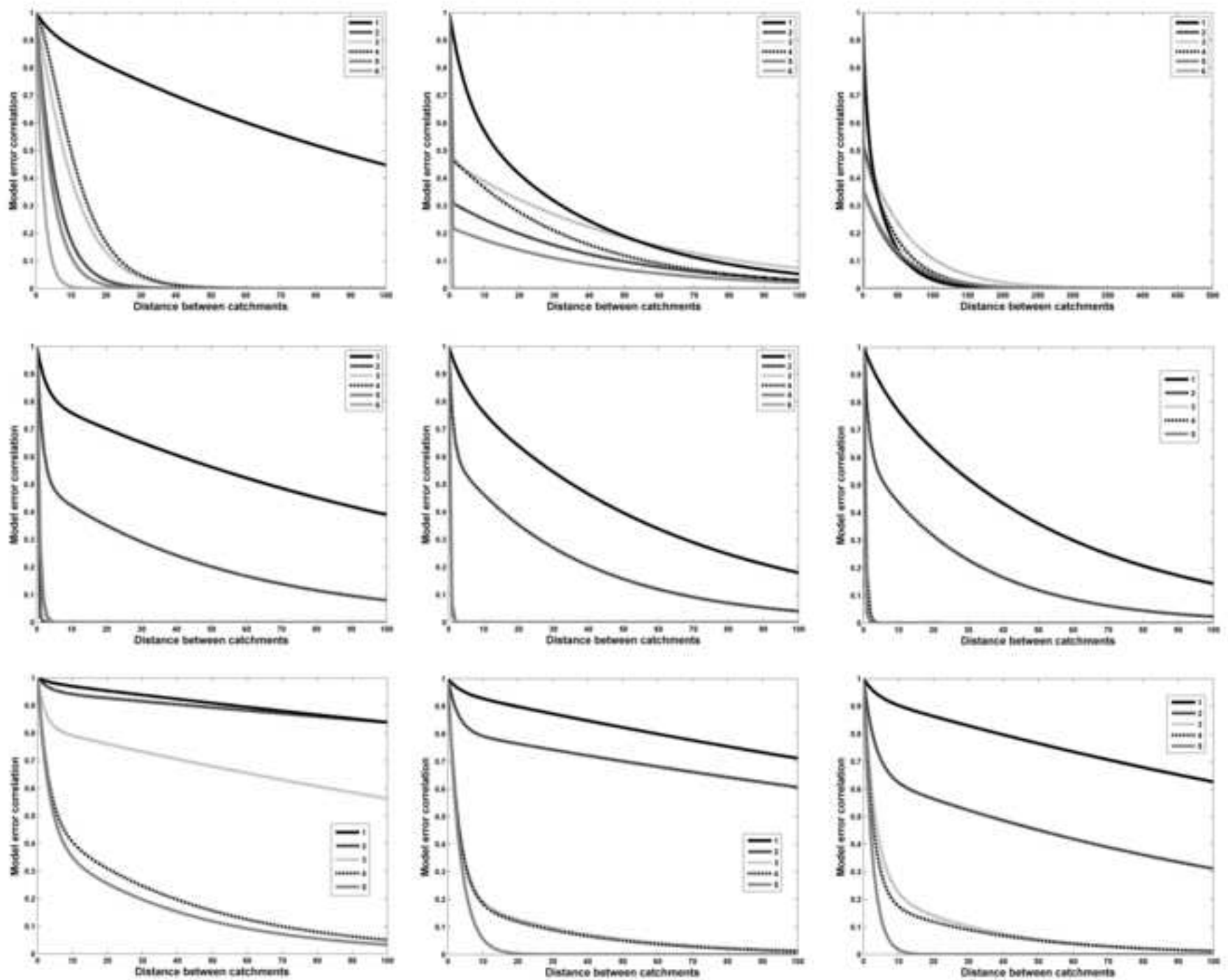




Figure 6  
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**Table 1**[Click here to download Table: Table\\_1.docx](#)

Table 1. Regional values of the L-CS and L-coefficient of variation (L-CV), number of gauging stations, N, and regional shape parameter of the GEV distribution, k, in the five homogeneous regions of the Ebro River catchment.

Region	L-CS	L-CV	N	k
91	0.194	0.257	34	-0.037
92	0.410	0.343	25	-0.343
93	0.489	0.569	10	-0.444
94	0.386	0.497	12	-0.312
95	0.272	0.357	12	-0.154

**Table 2**[Click here to download Table: Table\\_2.docx](#)

Table 2. Coefficients ( $\varphi_{\varepsilon,i}$ ) and results of the root mean squared error ( $RMSE$ ) and coefficient of determination ( $R^2$ ) for the double exponential function (Eq. 14) fitted to the observed data.

$\varphi_{\varepsilon,1}$	$\varphi_{\varepsilon,2}$	$\varphi_{\varepsilon,3}$	$RMSE$	$R^2$
0.5406	0.0952	0.0073	0.210	0.370

Table 3

[Click here to download Table: Table\\_3.docx](#)

- 1 Table 3. Comparison between OLS and GLS regression models for return periods, T, of two, 25  
2 and 100 years.

Region 91						
Coefficient	OLS			GLS		
	T = 2	T = 25	T = 100	T = 2	T = 25	T = 100
Intercept ( $\theta_0$ )	-4.8949	-5.5541	-5.7549	-5.0833	-5.2676	-5.7015
$\log_{10}(A)$	0.7753	0.7733	0.7738	0.7822	0.7743	0.7732
$\log_{10}(P_T)$	2.9029	2.6320	2.5530	3.0057	2.7855	2.5547
$\log_{10}(H)$	0.0296	0.2758	0.3441	0.0337	0.0951	0.3311
$\log_{10}(t_{inf})$	-0.0480	-0.0179	-0.0200	-0.0655	-0.0695	-0.0382
$\sigma^2_\eta$	0.0196	0.0247	0.0268	0.0136	0.0168	0.0176
SEP (%)	33.12	37.40	39.05	29.81	34.15	34.08
EVR	-	-	-	0.100	0.135	0.150
Region 92						
Coefficient	OLS			GLS		
	T = 2	T = 25	T = 100	T = 2	T = 25	T = 100
Intercept ( $\theta_0$ )	-4.2161	-5.7193	-6.0179	-2.9825	-4.7874	-4.9560
$\log_{10}(A)$	0.7025	0.6616	0.6445	0.5987	0.5877	0.5667
$\log_{10}(P_T)$	2.4689	3.1736	3.2754	1.9132	2.8129	2.8796
$\log_{10}(A_{1500})$	0.0555	0.0525	0.0576	0.0888	0.0790	0.0861
$\sigma^2_\eta$	0.0258	0.0253	0.0270	0.0229	0.0117	0.0100
SEP (%)	38.34	37.88	39.23	42.60	31.90	30.26
EVR	-	-	-	0.113	1.194	1.802

3

4

Table 4

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1 Table 4. Parameters and statistics of the GLS regression models fitted in the Region 91 for return periods, T, of two, 25 and 100 years.

T	Model	$\theta_0$	$\log(A)$	$\log(P_T)$	$\log(IC)^9$	$\log(S)^{-1}$	$I_e$	$\log(PET)$	$\sigma_\eta^2$	$AVP_{GLS}$	$SEP$ (%)	$MLE$	$EVR$
2	1	0.1178	0.7845	-	-	-	-	-	0.1202	0.1751	123.7	-81.1	0.011
	2	-5.3561	0.7747	3.1911	-	-	-	-	0.0138	0.0153	29.12	-107.3	0.098
	3	-5.5245	0.7760	3.2620	-9.8808	-	-	-	0.0118	0.0137	27.48	-116.0	0.115
	4	-5.7334	0.8185	3.3343	-10.7554	-0.0246	-	-	0.0105	0.0126	26.28	-122.0	0.129
	5	-5.1518	0.8234	2.7761	-10.2848	-0.0288	0.0169	-	0.0053	0.0066	18.92	-135.9	0.254
	6	-10.468	0.7933	2.8021	-10.1947	-0.0275	0.0271	1.8255	0.0032	0.0042	14.97	-148.2	0.427
25		$\theta_0$	$\log(A)$	$\log(P_T)$	$\log(IC)^9$	$\log(S)^{-1}$	$I_e$	$\log(H)$					
	1	0.5563	0.7433	-	-	-	-	-	0.0484	0.0565	59.08	-77.24	0.047
	2	-5.4299	0.7648	2.9819	-	-	-	-	0.0175	0.0204	33.81	-99.36	0.129
	3	-5.2504	0.7598	2.8763	-12.0162	-	-	-	0.0126	0.0158	29.58	-112.6	0.179
	4	-5.3600	0.7939	2.8953	-12.6452	-0.0309	-	-	0.0095	0.0120	25.68	-119.4	0.238
	5	-4.9145	0.8075	2.5148	-13.4199	-0.0342	0.0125	-	0.0065	0.0084	21.39	-126.2	0.348
6	-5.7168	0.8177	2.5009	-14.2157	-0.0335	0.0103	0.2875	0.0059	0.0076	20.34	-128.12	0.383	
100		$\theta_0$	$\log(A)$	$\log(P_T)$	$\log(IC)^9$	$\log(S)^{-1}$	$I_e$	$\log(H)$					
	1	0.6834	0.7375	-	-	-	-	-	0.0456	0.0522	56.47	-76.38	0.058
	2	-5.5355	0.7617	2.9404	-	-	-	-	0.0193	0.0228	35.86	-96.58	0.137
	3	-5.2784	0.7564	2.8039	-12.5680	-	-	-	0.0141	0.0181	31.73	-110.18	0.187
	4	-5.3863	0.7916	2.8192	-13.1645	-0.0322	-	-	0.0105	0.0136	27.31	-117.09	0.253
	5	-4.9152	0.8034	2.4591	-14.0366	-0.0349	0.0114	-	0.0076	0.0102	23.58	-122.29	0.346
6	-6.0353	0.8188	2.4423	-15.0828	-0.0346	0.0088	0.3956	0.0065	0.0084	21.36	-124.54	0.409	

2

Table 5

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1 Table 5. Results of the *VIF* coefficient for the GLS regression models fitted in the Region 91 for return periods, *T*, of two, 25 and 100 years.

T	Model	log(A)	log(P <sub>T</sub> )	log(IC) <sup>9</sup>	log(S) <sup>-1</sup>	I <sub>e</sub>	log(PET)
2	1	-	-	-	-	-	-
	2	1.0060	1.0060	-	-	-	-
	3	1.0085	1.0066	1.0033	-	-	-
	4	1.1735	1.0102	1.0211	1.1878	-	-
	5	1.2226	1.1117	1.0262	1.1922	1.1625	-
	6	1.3373	1.1140	1.0337	1.1971	2.2382	2.3499
25		log(A)	log(P <sub>T</sub> )	log(IC) <sup>9</sup>	log(S) <sup>-1</sup>	I <sub>e</sub>	log(H)
	1	-	-	-	-	-	-
	2	1.0106	1.0106	-	-	-	-
	3	1.0133	1.0106	1.0027	-	-	-
	4	1.1816	1.0169	1.0202	1.1909	-	-
	5	1.2282	1.0771	1.0262	1.1950	1.1190	-
6	1.2379	1.0812	1.1070	1.2227	1.4795	1.5862	
100		log(A)	log(P <sub>T</sub> )	log(IC) <sup>9</sup>	log(S) <sup>-1</sup>	I <sub>e</sub>	log(H)
	1	-	-	-	-	-	-
	2	1.0109	1.0109	-	-	-	-
	3	1.0137	1.0111	1.0029	-	-	-
	4	1.1835	1.0195	1.0201	1.1934	-	-
	5	1.2303	1.0685	1.0265	1.1974	1.1072	-
6	1.2409	1.0686	1.1066	1.2237	1.4835	1.5802	

2

1 Table 6. Parameters and statistics of the GLS regression models fitted in the Region 92 for return periods, T, of two, 25 and 100 years.

T	Model	$\theta_0$	log(A)	log(P <sub>T</sub> )	log(P <sub>0</sub> )	log(S) <sup>-4</sup>	log(IC) <sup>-2</sup>	log(PET)	$\sigma^2_\eta$	AVP <sub>GLS</sub>	SEP (%)	MLE	EVR
2	1	0.2124	0.6948	-	-	-	-	-	0.0614	0.0910	78.74	-63.31	0.042
	2	-3.8397	0.6907	2.3191	-	-	-	-	0.0244	0.0313	42.50	-69.96	0.106
	3	-3.4487	0.7295	2.6532	-0.8035	-	-	-	0.0160	0.0190	32.55	-75.24	0.162
	4	-3.2008	0.7334	2.5334	-0.8262	-0.0042	-	-	0.0132	0.0164	30.15	-79.37	0.196
	5	-4.2909	0.7631	3.0036	-0.6297	-0.0052	20.7162	-	0.0098	0.0128	26.48	-85.19	0.265
	6	-2.3569	0.7795	2.7762	-0.3597	-0.0042	25.6163	-0.6854	0.0085	0.0116	25.22	-87.92	0.305
25		$\theta_0$	log(A)	log(P <sub>T</sub> )	log(P <sub>0</sub> )	log(S) <sup>-2</sup>	log(IC) <sup>-2</sup>	log(H)					
	1	0.7975	0.6658	-	-	-	-	-	0.0354	0.0482	53.97	-59.05	0.395
	2	-5.5499	0.6670	3.1263	-	-	-	-	0.0130	0.0181	31.72	-68.22	1.071
	3	-5.2879	0.7048	3.4322	-0.7303	-	-	-	0.0086	0.0124	26.02	-72.50	1.616
	4	-4.9948	0.7058	3.3175	-0.7436	-0.0342	-	-	0.0061	0.0101	23.42	-75.76	2.296
	5	-5.2986	0.7235	3.5572	-0.8263	-0.0467	-0.0165	-	0.0039	0.0082	21.05	-78.72	3.566
6	-6.0505	0.7380	3.5820	-0.7889	-0.0375	-0.0213	0.1997	0.0034	0.0081	20.99	-79.15	4.149	
100		$\theta_0$	log(A)	log(P <sub>T</sub> )	log(P <sub>0</sub> )	log(S) <sup>-2</sup>	log(IC) <sup>-2</sup>	log(H)					
	1	1.0508	0.6568	-	-	-	-	-	0.0316	0.0427	50.40	-57.02	0.571
	2	-5.7504	0.6513	3.1881	-	-	-	-	0.0120	0.0170	30.69	-65.60	1.506
	3	-5.4909	0.6891	3.4835	-0.7355	-	-	-	0.0082	0.0124	26.05	-69.80	2.208
	4	-5.1896	0.6899	3.3698	-0.7445	-0.0362	-	-	0.0052	0.0096	22.90	-73.13	3.488
	5	-5.6423	0.7114	3.6705	-0.8368	-0.0491	-0.0171	-	0.0030	0.0079	20.70	-75.77	5.973
6	-6.7731	0.7324	3.7300	-0.7801	-0.0363	-0.0243	0.2851	0.0019	0.0073	19.86	-76.53	9.279	

Table 7

[Click here to download Table: Table\\_7.docx](#)

1 Table 7. Results of the *VIF* coefficient for the GLS regression models fitted in the Region 92 for return periods, T, of two, 25 and 100 years.

T	Model	log(A)	log(P <sub>T</sub> )	log(P <sub>0</sub> )	log(S) <sup>-4</sup>	log(IC) <sup>-2</sup>	log(PET)
2	1	-	-	-	-	-	-
	2	1.0135	1.0135	-	-	-	-
	3	1.2079	1.0142	1.1977	-	-	-
	4	1.2106	1.0327	1.2008	1.0225	-	-
	5	1.2780	1.2812	1.3827	1.0685	1.6025	-
	6	1.3348	1.4027	2.1386	1.2074	1.8078	2.3525
25		log(A)	log(P <sub>T</sub> )	log(P <sub>0</sub> )	log(S) <sup>-2</sup>	log(IC) <sup>-2</sup>	log(H)
	1	-	-	-	-	-	-
	2	1.0087	1.0087	-	-	-	-
	3	1.2122	1.0134	1.2025	-	-	-
	4	1.2168	1.0273	1.2068	1.0209	-	-
	5	1.2461	1.0532	1.2453	1.1967	1.2383	-
6	1.5315	1.0582	1.2676	1.9033	1.9632	3.4105	
100		log(A)	log(P <sub>T</sub> )	log(P <sub>0</sub> )	log(S) <sup>-2</sup>	log(IC) <sup>-2</sup>	log(H)
	1	-	-	-	-	-	-
	2	1.0052	1.0052	-	-	-	-
	3	1.2109	1.0159	1.2096	-	-	-
	4	1.2160	1.0239	1.2137	1.0151	-	-
	5	1.2455	1.0524	1.2552	1.1945	1.2414	-
6	1.5329	1.0554	1.2776	1.9039	1.9690	3.4037	

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1 Table 8. GLS regression models in the entire Ebro River catchment for return periods, T, of two, 25 and 100 years.

T	Model	$\theta_0$	$\log(A)$	$\log(P_T)$	$\log(P_m)^{-5}$	$\log(H)$	$\log(PET)$	$\sigma_\eta^2$	$AVP_{GLS}$	$SEP (\%)$	$MLE$	$EVR$
2	1	-0.0472	0.7429	-	-	-	-	0.4685	0.7817	788.0	-212.5	0.008
	2	-5.1623	0.7519	2.9652	-	-	-	0.2147	0.3676	245.4	-243.1	0.018
	3	-2.7361	0.7607	1.8430	-122.95	-	-	0.0561	0.0801	72.73	-258.8	0.069
	4	0.9896	0.7305	1.3611	-211.59	-0.7869	-	0.0199	0.0229	35.90	-267.9	0.196
	5	3.1365	0.7308	1.4349	-195.29	-0.9033	-0.7030	0.0184	0.0211	34.40	-271.0	0.212
25		$\theta_0$	$\log(A)$	$\log(P_T)$	$(I_a)^{-5}$	$\log(IC)^{-2}$	$\log(PET)$					
	1	0.5265	0.7012	-	-	-	-	0.2182	0.3287	217.1	-196.1	0.060
	2	-5.3890	0.7135	2.9550	-	-	-	0.0653	0.0962	81.57	-230.2	0.199
	3	-4.5950	0.7181	2.6027	-0.0318	-	-	0.0176	0.0195	33.04	-240.1	0.742
	4	-4.2863	0.7097	2.4894	-0.0320	-0.0119	-	0.0159	0.0180	31.64	-247.5	0.821
5	-1.6877	0.7175	2.4654	-0.0264	-0.0132	-0.9109	0.0148	0.0167	30.46	-253.5	0.881	
100		$\theta_0$	$\log(A)$	$\log(P_T)$	$(I_a)^{-5}$	$\log(FDCS_I)^{-1}$	$\log(H)$					
	1	0.7484	0.6881	-	-	-	-	0.1718	0.2434	162.3	-188.9	0.089
	2	-5.4774	0.6993	2.9552	-	-	-	0.0386	0.0478	53.72	-222.5	0.397
	3	-4.7826	0.7055	2.6522	-0.0255	-	-	0.0188	0.0209	34.24	-233.3	0.816
	4	-4.4789	0.7103	2.6070	-0.0280	-0.3016	-	0.0167	0.0189	32.49	-240.4	0.918
5	-5.4395	0.7250	2.6234	-0.0285	-0.3731	0.3117	0.0149	0.0168	30.52	-245.7	1.031	

2

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Table 9

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1 Table 9. Results of the *VIF* coefficient for the GLS regression models fitted in the entire Ebro River catchment for return periods, *T*, of two, 25  
2 and 100 years.

T	Model	log(A)	log(P <sub>T</sub> )	log(P <sub>m</sub> ) <sup>-5</sup>	log(H)	log(PET)
2	1	-	-	-	-	-
	2	1.0619	1.0619	-	-	-
	3	1.0782	1.8467	1.8555	-	-
	4	1.0976	1.9108	2.1729	1.2312	-
	5	1.1006	2.1182	3.8694	1.2924	2.4152
25		log(A)	log(P <sub>T</sub> )	(I <sub>a</sub> ) <sup>-5</sup>	log(IC) <sup>-2</sup>	log(PET)
	1	-	-	-	-	-
	2	1.0636	1.0636	-	-	-
	3	1.0886	1.2022	1.1924	-	-
	4	1.0987	1.2855	1.1984	1.0719	-
5	1.1075	1.2857	1.6745	1.0938	1.5301	
100		log(A)	log(P <sub>T</sub> )	(I <sub>a</sub> ) <sup>-5</sup>	log(FDCS <sub>I</sub> ) <sup>-1</sup>	log(H)
	1	-	-	-	-	-
	2	1.0627	1.0627	-	-	-
	3	1.0899	1.1756	1.1671	-	-
	4	1.1020	1.2281	1.3182	1.1464	-
5	1.1483	1.2313	1.3185	1.2396	1.1411	

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