Quantifying Gravity Wave Momentum Fluxes with Mesosphere Temperature Mappers and Correlative Instrumentation

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Abstract

An Advanced Mesosphere Temperature Mapper (AMTM) and other instruments at the ALOMAR observatory in Norway (69.3°N) and at Logan and Bear Lake Observatory in Utah (42°N) are used to demonstrate a new method for quantifying gravity wave (GW) pseudo-momentum fluxes accompanying spatially and temporally localized GW packets. The method improves on previous airglow techniques by employing direct characterization of the GW temperature perturbations averaged over the OH airglow layer and correlative wind and temperature measurements to define the intrinsic GW properties with high confidence. These methods are applied to two events, each of which involves superpositions of GWs having various scales and character. In each case, small-scale GWs were found to achieve transient, but very large, momentum fluxes with magnitudes varying from ~30 to 800 m²s⁻², that are ~1-2 decades larger than mean values. Quantification of the spatial and temporal variations of GW amplitudes and pseudo-momentum fluxes may also enable assessments of the total pseudo-momentum accompanying individual GW packets and of the potential for secondary GW generation that arises from GW localization. We expect that use of this method will yield key insights into the statistical forcing of the MLT by GWs, the importance of infrequent large-amplitude events, and their effects on GW spectral evolution with altitude.

Key Words: gravity waves, momentum flux, airglow, MLT dynamics
1. Introduction

Gravity waves (GWs) propagating upward from sources at lower altitudes are major drivers of the circulation and structure at higher altitudes due to their pseudo-momentum (hereafter momentum, see McIntyre [1981]) flux and body forces accompanying its divergence. Influences of GW momentum transport are especially significant in the mesosphere and lower thermosphere (MLT), where they account for the closure of the mesospheric jets, the GW-induced residual circulation from the summer to the winter mesosphere, and the corresponding thermal structure of the summer and winter polar mesospheres [Fritts and Alexander, 2003].

The character of GW forcing of the MLT remains largely unknown, however, as systematic global measurements able to quantify all of the relevant scales are not yet possible. While the major sources are known qualitatively, the contributions of GW filtering, interactions, spectral evolution, source intermittency, and GW localization are poorly understood at this time. Multiple observational and modeling studies at altitudes from the lower troposphere to the MLT suggest that GWs having relatively high frequencies and small horizontal scales contribute preferentially to vertical transport of horizontal momentum [e.g., Lilly and Kennedy, 1973; Vincent and Reid, 1983; Fritts and Vincent, 1987; Tsuda et al., 1990; Nastrom and Fritts, 1992; Pfister et al., 1993; Nakamura et al., 1999; Walterscheid et al., 1999; Lane et al., 2001; Yamada et al., 2001; Fritts et al., 2002; Horinouchi et al., 2002; Kim et al., 2003; Fritts and Alexander, 2003; Smith et al., 2008; Plougonven et al., 2008, 2013; Hertzog et al., 2008, 2012; Smith et al., 2009; Yue et al., 2009].

Airglow imagers, in particular, provide important information on GW horizontal scales, propagation directions, phase speeds, localization, intermittency, sources, and instability evolutions [e.g., Taylor and Hapgood, 1988; Swenson and Mende, 1994; Taylor et al., 1995, 1997; Hecht et al., 1997, 2000; Yamada et al., 2001; Fritts et al., 2002; Ejiri et al.,
2003; Nakamura et al., 2003; Suzuki et al., 2004; Li et al., 2005, 2007; Wrasse et al., 2006; Xu et al., 2006; Simkhada et al., 2009; Yue et al., 2009]. Airglow measurements have also been employed to estimate GW momentum fluxes, given their unique sensitivity to the smaller horizontal GW scales believed to account for the dominant fluxes in the MLT [e.g., Swenson and Liu, 1998; Swenson et al., 1999; Fritts et al., 2002; Tang et al., 2002, 2005a, b; Espy et al., 2004a, b, 2006; Suzuki et al., 2007]. However, traditional imagers are limited by measuring only airglow intensity at one or several deep airglow layers (typical layer full-width at half-maximum, FWHM ~7 km) centered from ~85 to 95 km. This imposes uncertainties in estimates of GW amplitudes and even larger uncertainties in estimates of GW momentum fluxes because the Krassovsky ratio of airglow intensity to temperature perturbations, \( \eta = (I'/I)/(T'/T) \), exhibits significant variability at a given GW period (by factors of ~2-5) [e.g., Taori and Taylor, 2006, and references therein]. This is because the intensity fluctuations depend on temperature, pressure, and species chemistry, while the GW momentum fluxes vary as \( (T'/T)^2 = (I'/I)^2 / \eta^2 \) [e.g., Swenson and Liu, 1998; Vargas et al., 2007, also see Section 4 below]. Hence GW momentum flux estimates relying on airglow intensity measurements may be uncertain by factors of ~3-10 or more.

An alternative to the use of airglow intensity fluctuations for GW momentum flux estimates are two-dimensional (2D) images of the OH airglow temperature fields obtained with Mesosphere Temperature Mappers (MTMs) as developed by Utah State University. Several of these are now in operation at the Arctic Lidar Observatory for Middle Atmosphere Research (ALOMAR, 69.3°N) in Norway in winter, at Logan, Utah (41.7°N) in summer, at the Andes Lidar Observatory (ALO, 30.3°S) in Chile, and at South Pole [Pautet et al., An advanced mesospheric temperature mapper for high-latitude airglow studies, Appl. Optics, 2014].
The new Advanced Mesospheric Temperature Mappers (AMTMs) offer a far more quantitative means of estimating GW momentum fluxes at multiple GW spatial scales because they avoid the uncertainties of inferring $T'/T$ from $I'/I$. They also can further reduce uncertainties under the following conditions: 1) the vertical profiles of horizontal wind (and preferably temperature) are measured with collocated lidars and/or radars, 2) these profiles allow one to distinguish between vertically-propagating and evanescent (or ducted) GWs, and 3) the GWs have sufficiently large vertical wavelengths that there is little reduction in the GW temperature amplitude due to phase cancellation across the airglow layer. In such cases, we expect estimates of GW momentum fluxes to be quite precise because all of the GW intrinsic properties and the wind and temperature amplitudes can be computed directly. An additional, and large, benefit that we will exploit here is the measurement of temperature (thus also estimates of horizontal and vertical velocity) perturbations as 2D temperature maps allowing determination of the spatial extent and duration of regions of significant momentum flux within the AMTM field of view (FOV). This is expected to be a major benefit because we currently have a very limited understanding of the spatial extents of GW forcing events in the MLT. Yet such information is critically important, given the expectation that spatially- and temporally-localized events must excite additional GWs that may then propagate to much higher altitudes [Vadas and Fritts, 2001, 2002]. Additionally, momentum deposition statistics (including spatial and temporal intermittency) and secondary GW radiation are likely key to posing new and improved GW parameterization schemes for weather and climate prediction models.

This paper is organized as follows. Section 2 discusses 1) the dependence of GW momentum fluxes on AMTM temperatures, measured and inferred GW parameters, and environmental wind and temperature profiles, 2) the influences of AMTM GW phase averaging, and 3) quantification of GW momentum fluxes for extended and spatially-
localized GW packets. Applications of these methods to two GW packets observed by the AMTM and other instruments at Logan and Bear Lake Observatory (BLO) in Utah and at ALOMAR are discussed in Section 3. A discussion of these results is provided in Section 4. Our summary and conclusions are provided in Section 5.

2. Determination of GW Parameters and Momentum Fluxes

2.1. Dependence on GW and mean parameters

We assume GW propagation in the \((x,z)\) plane without loss of generality and employ the linear 2D perturbation equations describing conservation of momentum, mass, and energy and the definition of potential temperature, \(\theta = (p/\rho R) - (p_0/\rho)^K\), from Fritts and Alexander [2003] for deep GWs in an atmosphere having a mean wind \(U_h\) along the GW propagation direction. Also assuming the GWs of interest to have intrinsic frequencies \(>> f\) (the Coriolis frequency), these equations may be written as

\[
du'/dt + w' \partial U_h/\partial z + \partial (p'/\rho_0)/\partial x = 0 \tag{1}
\]

\[
dw'/dt + \partial (p'/\rho_0)/\partial z - (1/H)(p'/\rho_0) + gp'/\rho_0 = 0 \tag{2}
\]

\[
d(\rho'/\rho_0)/dt + \partial u'/\partial x + \partial w'/\partial z - w'/H = 0 \tag{3}
\]

\[
d(\theta'/\theta_0)/dt + w' (N^2/g) = 0 \tag{4}
\]

\[
(\theta'/\theta_0) = (1/c_s^2)(p'/\rho_0) - (\rho'/\rho_0) \tag{5}
\]

Here \(u', w', p', \rho', \) and \(\theta'\), are the perturbation horizontal and vertical velocities in the plane of GW propagation, pressure, density, and potential temperature, \(g\) is gravity, \(\kappa = R/c_p = 2/7\), 
\(d/dt = \partial/\partial t + U_h \partial/\partial x\), \(p_0\), \(\theta_0\), the density scale height \(H\), and the static stability \(N^2 = d\theta_0/dz\) (buoyancy frequency \(N = 2\pi/T_b\) with \(T_b\) is the buoyancy period) are mean quantities that may vary in altitude, and primes denote perturbation quantities. Assuming GW perturbations vary as

\[
u', w', \theta'/\theta_0, p'/\rho_0, \text{and } \rho'/\rho_0 \sim \exp[i(kx + mz - \omega t) + z/2H] \tag{6}
\]
and neglecting shear and curvature terms in the mean wind, $\partial U_h/\partial z = \partial^2 U_h/\partial z^2 \sim 0$, a GW with wavenumber components $(k, m)$ and observed frequency $\omega = kc$ and phase speed $c$ yields

$$\begin{align*}
- i \omega_1 u^' + ikp'/\rho_0 &= 0 \\
- i \omega_1 w^' + (im - 1/2H) p'/\rho_0 &= -g \rho'/\rho_0 = 0 \\
- i \omega_1 \rho'/\rho_0 + ik u^' + (im - 1/2H)w^' &= 0 \\
- i \omega_1 \theta'/\theta_0 + (N^2/g)w^' &= 0
\end{align*}$$

These equations yield the approximate GW dispersion relation for deep GWs given by

$$m^2 = k^2 \left( N^2/\omega_1^2 - 1 \right) - 1/4H^2$$

which is identical to the anelastic and compressible forms under the above assumptions [Fritts and Alexander, 2003; Lund and Fritts, 2012]. We note, for completeness, that the relations among GW perturbations, $k$, $m$, and $\omega_1$ in Eq. (7-12) would be considerably more complex had we retained mean wind shear and curvature terms [Nappo, 2002]. However, this would have rendered them nearly unusable for our purposes here, given our inability to define all of the GW and mean flow terms quantitatively. In particular, while the first term on the right hand side (RHS) of Eq. (12) is usually by far the dominant term, the second term on the RHS, $1/4H^2$, is often smaller than the neglected shear and curvature terms in complex environments. Indeed, these same reservations apply to all efforts to assess GW propagation and momentum fluxes, whether or not they have been included in the derived equations. Hence, when the $1/4H^2$ term becomes important, then other neglected terms should likely also be considered.

In the large majority of the applications envisioned in this paper, GWs will have sufficiently small vertical wavelengths $\lambda_z = 2\pi/m$ that the last term in Eq. (12) is negligible. This occurs for $\lambda_z^2 << (4\pi H)^2$. With $4\pi H \sim 75$ km for typical MLT conditions, this implies...
GWs having $\lambda_z \sim 25$ km or less will satisfy this condition. The other neglected terms can likewise be assumed to be negligible for local assessments of amplitudes and momentum fluxes for GWs that appear to have a relatively uniform $\lambda_z$ with altitude, even if this is less than $\lambda_z$.

To assess GW momentum fluxes as quantitatively as possible, we need to relate $T'$ measurements by AMTMs and lidars to the GW quantities in Eqs. (7-11). For this purpose, we employ the linearized form of the ideal gas law [Lund and Fritts, 2012], for temperature perturbations, $T'$, and mean temperature $T_0(z)$ that in general varies with altitude, given by

$$T'/T_0 = \rho'/\rho_0 - \rho'/\rho_0 = \theta'/\theta_0 + (\rho'/\rho_0)(1 - p_0/\rho_0 gH)$$

(13)

Using Eq. (11) and the pressure scale height defined as $H_p = RT/g$, this may be rewritten as

$$T'/T_0 = \theta'/\theta_0 + (\rho'/\rho_0)(1 - H_p/H)$$

(14)

Thus, for an isothermal atmosphere with $T_0(z)$ constant, $H_p = H$, and Eq. (14) simplifies to

$$T'/T_0 = \theta'/\theta_0$$

(15)

More generally, for $T_0(z) \neq 0$ and lapse rate $\Gamma = -dT/dz$, the terms in the ideal gas law can be expanded as Taylor series for small $z$ to yield,

$$H - H_p = HH_p \Gamma/T_0 + \text{higher order terms}$$

(16)

For $H$ and $H_p \sim 7$ km, $T_0 \sim 200$ K and $|\Gamma| \sim 2$ K/km, which are typical of, or larger than, mean values in the MLT, Eq. (16) implies differences between $H - H_p$ of $\sim 0.5$ km. Thus Eq. (14) implies that

$$T'/T_0 = \theta'/\theta_0 \pm 0.07 (\theta'/\theta_0 + \rho'/\rho_0) \sim \theta'/\theta_0$$

(17)

This is consistent with the relation inferred by assuming that the GWs of interest have $c_i \ll c_s$ and are thus relatively incompressible. This further implies that $-i\omega_0 \rho'/\rho_0$ in Eq. (9) and $c_s^2$ in Eq. (11) can also be neglected, yielding the equations

$$ik u' + (im - 1/2H)\omega' = 0$$

(18)

$$T'/T_0 = \theta'/\theta_0 = -\rho'/\rho_0$$

(19)
with ~7% uncertainties, except when \( \Gamma \) departs significantly from its mean value.

Finally, for \( \lambda_z < 25 \) km and \( k/m < 0 \) for upward propagation, Eqs. (10), (11), and (19) yield

\[
\frac{T'}{T_0} = \left( \frac{\theta}{\theta_0} \right) = -i\left( Nu'/g \right) \left( 1 - \omega_i^2/N^2 \right)^{1/2}
\]

\[
<u'w'> = (g^2 \omega_i/2N^3) \left( 1 - \omega_i^2/N^2 \right)^{1/2} \left( \frac{T'}{T_0} \right)^2
\]

For a spatially-localized GW packet, \( T(x,y) \) will vary with horizontal position and its spatial extent will define the approximate scale of the region influenced by GW momentum transport and deposition where GW dissipation occurs.

2.2. Influences of phase averaging within the OH layer

Because the OH airglow layer has a typical FWHM intensity (or brightness) of ~7 km [Baker and Stair, 1988], measured temperatures will be less than the maximum values at the peak intensity for GWs for which the layer depth is a significant fraction of \( \lambda_z \). It is usually assumed that the intensity can be approximated as a Gaussian distribution in the vertical

\[
I(z) = I_0 \exp\left[-(z - z_0)^2/2\sigma_z^2\right]
\]

where \( I_0 \) is the peak intensity, \( z_0 \) is the center of the OH layer, \( \sigma_z = z_{FWHM}/2(2\ln2)^{1/2} \), and \( z_{FWHM} \) is the FWHM airglow layer width, typically ~7 km, such that the measured temperature perturbation is given approximately by

\[
<T'> = \int T'(z) I(z) \, dz / \int I(z) \, dz
\]

The phase of the GW yielding the largest \( <T'> \) will occur where the maximum (or minimum) \( T'(z) = T_0 \cos[(2\pi/\lambda_z)(z - z_0)] \) occurs at \( z = z_0 \pm n\lambda_z/2 \), with \( n \) an integer. This yields a ratio of measured to true temperature fluctuations given by

\[
C = \frac{<T'>$}{T'(z_0)} = \exp(-\pi^2 z_{FWHM}^2/4\ln2 \lambda_z^2) = \exp(-1.78 z_{FWHM}^2/\lambda_z^2)
\]

Thus, \( C \approx 0.64, 0.82, \) and 0.89 for \( \lambda_z/z_{FWHM} = 2, 3, \) and 4, respectively, and significant phase averaging (and insensitivity to \( T' \)) occurs only for \( \lambda_z/z_{FWHM} \) less than ~2. Assuming
correlative lidar or radar measurements enable an estimate of \( \lambda_z \), the effect of phase averaging on the momentum flux estimate can be included by rewriting Eq. (21) as

\[
<u_h'w'> = (g^2 \omega_i/2N^2)(1 - \omega_i^2/N^2)^{1/2}(<T'>/T_0)^2/C^2 \tag{25}
\]

where \(<T'> (x, y)\) is the GW amplitude measured by the AMTM and \(C\) is a function of \(\lambda_z/z_{FWHM}\) given by Eq. (24).

In cases where there is significant large-scale wind shear expected to impact GW vertical structure, a steady, linear GW will have a vertical velocity given by a Frobenius expansion [Booker and Bretherton, 1967] with a leading term that varies as

\[
w'(z) \sim \delta z^{1/2} \exp(\pm i \mu \delta z) \tag{26}
\]

Here \(\delta z = z - z_c\), \(z_c\) denotes the height of a critical level for the GW (typically above an upward-propagating GW packet), we assume a uniform shear in the vicinity of \(z_c\), a local vertical wavenumber \( \mu = (Ri^{-1/2}) \) and a corresponding local \( \lambda_z \) that decreases as \(\delta z\), where \(Ri\) is the local Richardson number, \(Ri = N^2/(dU/dz)^2\), and \(dU/dz\) is the mean wind shear. This implies a corresponding \(u'(z) \sim \delta z^{1/2} \exp(\pm i \mu \delta z)\) and \(w'(z) \sim \delta z^{1/2} \exp(\pm i \mu \delta z)\), such that the momentum flux remains constant with altitude in the absence of dissipation. Far from a critical level, GW structure varies only slightly from a uniform \(\lambda_z\), and momentum flux estimates provided by Eqs. (24) and (25) are expected to be good approximations. However, proximity to \(z_c\) (with \(\delta z \sim \lambda_z\) or less) will cause decreasing \(\lambda_z\), increasing phase cancellation within the airglow layer, and reductions in \(<T'> relative to \(T'\), requiring a numerical solution of Eq. (23) to properly estimate the GW momentum flux. In practice, a GW cannot avoid dissipation (and sharply reduced momentum flux) due to instability and/or viscosity and thermal diffusivity as \(z_c\) is approached, though GW momentum transport and “self acceleration” may alter the local mean flow and the GW phase speed itself [Sutherland, 2006; Fritts and Lund, 2011]. Thus, the GW \(T'\) must be small where significant phase averaging
occurs near $z_c$. For additional discussion of the implications of critical level dynamics, the interested reader is referred to Booker and Bretherton [1967] and Fritts [1984].

2.3. Methodology

As noted above, multiple observations suggest that the majority of GW momentum flux from the lower atmosphere into the MLT accompanies GWs exhibiting small horizontal wavelengths, $\lambda_h \sim 100$ km or less, and high observed (and intrinsic) frequencies, $\omega$ and $\omega_i$, with typical observed periods, $T_{\text{obs}} = 2\pi/\omega \sim 1$ hr or less (e.g., Nastrom and Fritts 1992; Fritts and Alexander 2003, and references above). This implies that AMTM sensitivity to GWs having $\lambda_h \sim 10$ to 100 km have the potential to quantify the majority of GW momentum fluxes at the OH airglow altitude (e.g., the AMTM FOVs at ~87 km at ALOMAR and Logan are 180x144 km), whether these GWs are localized within the AMTM FOV or have larger extents.

GWs are typically localized in space and time, yielding a packet having a 2D $<T'>(x,y)$ field (hereafter using $T'$ in place of $<T'>$ in this section for simplicity) at the airglow layer. When GW packet scales exceed the FOV of the AMTM, wavefield fits will be performed for the entire FOV and optimized to define a “best fit” monochromatic GW for a horizontal wavelength, $\lambda_h$, propagation direction, $\phi$, and temperature amplitude, $T'$ (by minimizing the RMS $T'$ error). As most GWs have spatial extents of several $\lambda_h$, a full FOV GW fit is more likely for GWs having larger spatial scales. Optimal fits to the Keograms and 2D FFTs can also provide these estimates, depending on the GW spatial scales (see Section 3 below).

When GW packets are localized within the AMTM FOV in one or both dimensions at one time, or via their signatures in N-S and/or E-W Keograms (determined from temporal sampling of orthogonal AMTM pixel rows) as they propagate through the FOV, we expect
them to exhibit central maxima and roughly elliptical forms with major and minor axes along or across the GW packets. In such cases, it is possible to approximate the $T'(x,y)$ field with a simple spatial form enabling a quantitative estimate of the momentum flux distribution in space and time. Such information is valuable for assessing the GW packet scales and their intermittency of the forcing accompanying GW dissipation and momentum transport.

In most cases, AMTM, airglow, and other measurements indicate that isolated, individual GW packets occur very infrequently. Thus, for general and/or automated GW momentum flux estimates, we expect to employ both 2D FFTs and full-FOV or local wavefield fits to quantify the key parameters, e.g., $\lambda_b$, $\phi$, observed and intrinsic horizontal phase speeds, $c$ and $c_i$, and $T'$, for individual GW packets. These more complex environments will lead to greater uncertainties in fits and GW parameters. Here, however, we will confine our attention to cases for which defining a single GW packet is relatively straightforward. A more complete assessment of uncertainties accompanying superposed GWs, the presence of quasi-2D ducted GWs and/or Kelvin-Helmholtz instabilities (KHI), and possible 3D structures accompanying KH billow breakdown, GW breaking, and/or 3D turbulence, will be addressed separately.

In order to estimate the spatial extent of a GW packet, we assume either a uniform, Gaussian, or half-cosine distribution of $T'(x',y')$ to quantify GW packet characteristics and simplify our GW momentum flux and total momentum estimation procedures. For GW packets within the AMTM FOV, we assume a maximum amplitude $T' = T'_0$ at $(x'_0, y'_0)$ and along-track and cross-track FWHM dimensions of $X'$ and $Y'$ (with $x'$ increasing along the GW propagation direction), we can approximate the spatial variations of $T'(x',y')$ as either

$$T'(x',y') = T'_0 \exp \{-4\ln2[(x' - x'_0)^2/X'^2 + (y' - y'_0)^2/Y'^2]\} \quad (27)$$

or

$$T'(x',y') = T'_0 \cos[2\pi(x' - x'_0)/3X'] \cos[2\pi(y' - y'_0)/3Y'] \quad (28)$$
where Eq. (28) assumes a fit for \(|x' - x'_0| \leq 3X'/4\) and \(|y' - y'_0| \leq 3Y'/4\). We assume GW packet coordinates \((x'_0, y'_0)\) with \(x'_0\) aligned at angle \(\phi\) east of north (see Figure 1, top panel) and geographic coordinates with \(x\) to the east. With this convention, the relations between the GW packet \(\lambda_h, \phi, c\) and the apparent zonal \((x)\) and meridional \((y)\) wavelengths, \(\lambda_x = 2\pi k_x\) and \(\lambda_y = 2\pi k_y\), and phase speeds, \(c_x = \lambda_x/T_{GW}\) and \(c_y = \lambda_y/T_{GW}\) as they would appear in the AMTM image and the N-S and E-W Keograms are shown in Figure 1. Here, \(T_{GW}\) is the GW period and \(k_h^2 = k_x^2 + k_y^2\) implies that \(1/c^2 = 1/c_x^2 + 1/c_y^2\).

2.4. Instrumentation

Our momentum flux assessments in this paper employ MF or meteor radar, sodium lidar, and AMTM measurements to define the temperature and horizontal velocity fields and the \(\sim 87\) km temperature maps at BLO and ALOMAR. The spatial and temporal resolutions of these instruments employed for this study are shown in Table 1.

3. Momentum Flux Estimates

3.1. Event 1: Observations at Logan and BLO, 6 June 2013

N-S and E-W OH (3,1) temperature Keograms showing a number of GW responses from \(\sim 4:30\) to 11 UT on 6 June 2013 are shown in the upper panel of Figure 2. Keograms are generated separately from the AMTM brightness and temperature time series data by sequencing orthogonal pixel rows and columns through each image to create N-S and E-W summary plots of the nocturnal GW activity. The Keograms reveal a superposition of larger- and smaller-scale GW responses having observed periods ranging from \(\sim 20\) min to 6 hr or longer. Our focus here is on the interval within the dashed vertical lines in the Keograms, which is a subset of a longer interval exhibiting a superposition of two GW fields extending from \(\sim 7-9\) UT. Zoomed images of this event in the AMTM emission \(I(x,y)\) and \(T(x,y)\) fields
(N and E up and to the right, respectively) are shown at 10-min intervals in the lower panels of Figure 2. The lower images reveal both

1) a larger-scale GW propagating towards the NNW with \( \lambda_h \sim 21 \text{ km} \), \( \phi \sim -20^\circ \), and \( c \sim 30 \text{ ms}^{-1} \) occupying most of the AMTM FOV and

2) a smaller-scale GW propagating towards the NE with \( \lambda_h \sim 12.5 \text{ km} \), \( \phi \sim 40^\circ \), and \( c \) increasing from \( \sim 0 \) to \( \sim 10 \text{ ms}^{-1} \) confined to the S and W AMTM FOV at these times.

The larger-scale GW spans the AMTM FOV and appears to be a ducted GW, based on correlative wind and temperature measurements and its persistence for \( \sim 5 \text{ hr} \). Winds in the plane of GW propagation exhibit almost no shear, are \( \sim 70 \text{ ms}^{-1} \) opposite to the propagation direction at \( \sim 87 \text{ km} \) (not shown), and imply a large intrinsic phase speed of \( \sim 100 \text{ ms}^{-1} \) and an implied intrinsic frequency of \( \omega_i \sim 0.03 \text{ s}^{-1} \). This is marginally below the maximum \( N \) near 88 km of \( \sim 0.039 \text{ s}^{-1} \), but is substantially above the smaller \( N \sim 0.017 \text{ s}^{-1} \) inferred at higher and lower altitudes (see the discussion of Figure 3 below). In contrast, the smaller-scale GW (which we label Event 1) is more localized in space, more transient, and more dynamically active. See, for example, the indications of phase speed accelerations accompanying the later stages of Event 1 (~8 to 9 UT) at the lower edges of both Keograms. Because Event 1 is confined to the lower left portion of the AMTM FOV, however, its maximum amplitude is not seen in either Keogram. Hence we rely largely on individual AMTM images for its characterization. Key features of the Event 1 GW packet include the following:

1) it arises in place, rather than propagating into the FOV from the SW, beginning \( \sim 7:20 \text{ UT} \), so it can only have propagated into the airglow layer from below,

2) it appears to have a very restricted extent along its direction of propagation at early times, as only \( \sim 4 \) cycles spanning \( \sim 50 \text{ km} \) are visible prior to 8 UT,

3) successive images reveal additional phase fronts, with decreasing \( T' \), thereafter, and
the GW exhibits strong instability at its leading edge beginning ~9 UT (not shown), providing further evidence of amplitude growth with time and altitude.

To diagnose the Event 1 GW packet character in greater detail, we employ the USU Na lidar located at Logan, Utah and the meteor radar (courtesy of N. Mitchell, Univ. of Bath, UK), located at BLO, separated by ~40 km. The $T(z)$ profiles were obtained in the lidar east beam, which is ~30 km E of Logan at the OH layer. The lidar (Logan), lidar east beam, and meteor radar (BLO) locations are shown with the “X” and the black and blue squares, respectively, in the lower right panel of Figure 2. An OH profile obtained by the SABER instrument aboard the TIMED satellite was also available at 12:53 UT ~600 km to the ESE. This shows an OH layer with $z_{FWHM} \sim 7$ km, confirming our assumption above.

Shown in Figure 3 are horizontal winds in the plane of GW propagation, $U_h(z)$, for 1-hr averages at 30-min intervals measured with the meteor radar, $T(z)$ at 30-min intervals measured with the Na lidar, $\lambda_h$, $c$, and $<T>$ measured with the AMTM throughout Event 1, and the inferred $c_i = (c - U_h)$ assuming the OH layer was centered at ~87 km from 7 to 8 UT. $<T>$ was estimated from the power in the 2D Fourier transform for a localized domain within the GW field. Typical uncertainties in AMTM measurements of $\lambda_h$, $c$, $<T>$ and $\phi$ are ~3, 3, and 5 % and ~1° for individual 30-s estimates and ~1, 1, and 2 % and < 1° for a 5-min (10-sample) average.

The lidar profiles indicate a maximum $dT/dz \sim 20$ Kkm$^{-1}$ (dashed line, upper right panel) at 7:30-8:30 UT, implying a maximum $N \sim 0.039$ s$^{-1}$. There is significant uncertainty in the true mean $T(z)$ profiles for Event 1, however, as the profiles shown also include lower-frequency GWs (note the 5-hr or longer period GW contributing ~15 K fluctuations in the Keograms). These structures also must yield horizontal variations in the $T(z)$ structure and altitude of maximum $N^2$ at the site of Event 1 relative to the location of the lidar $T(z)$. For reference, the maximum amplitude of the GW in Event 1 is near the left edge of the lower
right panel in Figure 2, ~120 km from the $U_h(z)$ and $T(z)$ profiles to the E and NE of Logan. The mean temperature gradient over the airglow layer is much less, with $dT/dz \sim 5$-10 K km$^{-1}$ (we estimate an ~25-30% uncertainty in $N^2$) and a corresponding range of $N \sim 0.028$-0.032 s$^{-1}$, depending on the actual airglow altitude during the BLO observations.

The various measurements imply best estimates for the GW parameters at the event times from 7:40-8:00 UT of $\lambda_h \sim 12.5$ km, $U_h \sim -49$ ms$^{-1}$, $c \sim 3$ ms$^{-1}$, $c_i = (c - U_h) \sim 52$ ms$^{-1}$, and $\langle T' \rangle / T_0 \sim 3.7\%$. Given $\omega_i = k_h c_i \sim 0.026$ s$^{-1}$, $N \sim 0.03$ s$^{-1}$, and $z_{FWHM} \sim 7$ km, Eqs. (12), (24), and (25) imply $\lambda_z \sim 1.74 \lambda_h \sim 21.7$ km, $C^2 \sim 0.69$, $u_h' = 7.3$ ms$^{-1}$, $w' = 12$ ms$^{-1}$, and $\langle u_h w' \rangle \sim 43$ m$^2$s$^{-2}$. These parameters are summarized in Table 2 for convenience.

For reference, the smaller and larger limits of likely $N \sim 0.028$ and 0.032 s$^{-1}$ yield estimates of $\langle u_h w' \rangle \sim 33$ and 60 m$^2$s$^{-2}$, respectively. Additionally, a 10% change in $z_{FWHM}$ changes the $\langle u_h w' \rangle$ estimate by ~4%. These various estimates imply a cumulative uncertainty of ~40% about the central value, in the absence of direct measurements of local $dT/dz$ and $z_{FWHM}$. The range of $\langle u_h w' \rangle$ estimates is ~5-10 times those typically measured by radars or inferred from middle atmosphere general circulation models (GCMs) at ~87 km [e.g., Fritts and Alexander, 2003]. Finally, we employ the spatial distribution given by Eq. (28) to approximate the dimensions of this GW packet. These yield an along-track FWHM packet width estimate of $X' \sim 40$ km. The cross-track packet width was much larger. These results are discussed in relation to previous studies and more general MLT dynamics in Section 4.

### 3.2 Event 2: Observations at ALOMAR, 28 January 2014

An overview of Event 2 is provided with N-S and E-W Keograms spanning 12 hr, zoomed and 0.5-2-hr band-passed Keograms spanning 2.5 hr, and six OH airglow $T(x,y)$ fields at 5-min intervals in Figure 4. The Keograms are shown for two intervals: 12 hr spanning an anticipated semidiurnal tide period, and 2.5 hr zooming in on the medium- and
smaller-scale GWs at later times. As in Event 1, the Keograms exhibit a superposition of larger- and smaller-scale GW, tidal, and/or longer-period responses. The Keograms spanning 12 hr suggest a semidiurnal (SD) tide or large-scale inertia-GW (IGW) having a temperature amplitude of $T' \sim 15$ K. Caution is prudent in this interpretation, however, because large-amplitude, ~12-hr features are often seen at ALOMAR and other northern and southern high-latitude sites [e.g., Williams et al., 2006; Fritts et al., 2010]. But near ALOMAR (69°N, 15°E), the SD tide is predicted by the GSWM-09 model to be quite small at this time [Zhang et al., 2010a, b].

For reference, the mean January SD tide is predicted by GSWM-09 to have zonal wind and temperature amplitudes of $u' < 1$ ms$^{-1}$ and $T' < 1$ K, respectively, at all altitudes from 80-100 km. The predicted February SD tide $u'$ increases from $\sim 4$ ms$^{-1}$ at 82 km to $\sim 7.5$ ms$^{-1}$ at 95 km and above, but $T'$ remains $< 0.5$ K at the relevant altitudes. Hence, it remains uncertain whether the large ~12-hr $u'$ and $T'$ observed at ALOMAR are SD tides that are inconsistent with GSWM-09 predictions or are instead large-amplitude IGWs having comparable periods. Additional evidence that such features may often be due to a large-scale IGW comes from the observed vertical wavelength, which for the results shown by Williams et al. [2006] was $\sim 20$ km, whereas the GSWM-09 SD tide estimates are $\sim 30$-40 km. Our current measurements with additional radar and lidar instruments at ALOMAR to be discussed below suggest larger vertical wavelengths than observed by Williams et al. [2006].

The Keograms in Figure 4 exhibit a number of specific features of relevance to our analysis. These include the following:

1) a decrease of the large-scale $T(x,y)$ from $\sim 20$ to 02 UT accompanying the decreasing $T'$ phase of the ~12-hr GW or SD tide,

2) apparent modulations of the large-scale $T(x,y)$ by GWs having periods of $\sim 1$ and 4 hr, and
3) small-scale GWs having ~10-min periods that are visible throughout the 2.5-hr Keograms, but which exhibit two clear, localized responses from ~23:20 to 01:20 UT. The characteristics measured or inferred for each of the dominant wave motions observed during this interval are listed for convenience in Table 3.

Small-scale GWs during this interval a) exhibit increasing $T'$ amplitude modulations at an ~1-hr period after ~22 UT, b) achieve maximum $T'$ amplitudes that are coincident with the final two ~1-hr GW $T'$ maxima, and c) propagate primarily towards ~70° E of N after ~22:20 UT. The second of the two local GW responses occurring between ~00 and 01:20 UT is our focus in Event 2 due to its larger $T'$ amplitude and its confinement largely within the AMTM FOV. Confinement of the GW packet within the AMTM FOV ensures that it almost certainly enters from below and exits above, as it clearly does not enter or exit through the edges of the FOV and its amplitude appears to be too large to have propagated downward from significantly higher altitudes (because it has no earlier OH airglow signature) without displaying instability at the larger amplitudes implied at higher altitudes.

Correspondence of the two GW packets occurring between 23:20 and 01:20 UT with local $T'$ maxima of the ~1-hr GW suggests that the ~1-hr GW likely modulated the environment encountered by the higher-frequency GW packets, enabling or suppressing their propagation into the OH layer via local wind and/or $N^2$ variations. Additional evidence for such a motion is provided below. This provides important clues to the character of the Event 2 GW packet. Either an induced critical level or turning level below the OH airglow layer would seem necessary to modulate the observed Event 2 GW presence in the Keograms.

If a critical level for the Event 2 GW was moving up and down across the OH layer due to variable ~1-hr GW horizontal winds, its $c_i = (c - U_h)$ would be small at OH altitudes, requiring small $\omega_i = k_h(c - U_h)$, hence large $m/k$ and small $\lambda_z$ from Eq. (12). This would also require a small $u' \sim N/m$ or less due to instability constraints (but the lack of evidence of
instability structures implies this condition is not exceeded), small implied \( \frac{<T'>}{T_0} \) from Eq. (20), and long residence and propagation time scales due to a small vertical group velocity. However, the observed \( \frac{<T'>}{T_0} \) is relatively large and the response to the \( \sim 1 \)-hr GW modulation is fairly rapid. Hence a critical level explanation seems not defensible. Alternatively, modulation of \( m^2 \) about zero (accompanying a variable turning level altitude and GW refraction due to horizontal wind and/or \( N^2 \) modulations by the \( \sim 1 \)-hr GW) provides a far more plausible explanation, given the large observed \( T' \) of the small-scale GW packet and the rapid time scale on which responses occur.

To diagnose the Event 2 GW packet environment, structure, and dynamics in greater detail, we employ AMTM measurements to define \( \lambda_h, c, \phi \), and the maximum \( <T'> \) of the GW packet as functions of time. We also employ the AMTM, the ALOMAR SAURA 3.17 MHz MF radar, and the Na lidar to characterize the mean, tidal or IGW, and the medium-frequency (\( \sim 1 \)- to 4-hr period) GW background as fully as possible. The ALOMAR meteor radar confirms the larger-scale winds observed by SAURA, but at coarser spatial and temporal resolutions.

SAURA zonal and meridional winds at 1-km and 7.5-min resolutions are shown versus time and altitude and as time series at 92 km in the left panels of Figure 5 for the 12-hr AMTM Keogram interval at top in Figure 4. These reveal the expected approximate quadrature relation among \( u' \) and \( v' \) for the migrating SD tide or an IGW propagating approximately zonally. They also reveal that \( u' \) exceeds \( v' \), which we expect for a zonally-propagating IGW, but not for the migrating SD tide. As examples, observations at high latitudes and the Canadian Middle Atmosphere Model Data Assimilation System (CMAM-DAS) typically exhibit migrating SD tide \( v' > u' \) near winter solstice [e.g., Baumgaertner et al., 2006; Murphy et al., 2006; Fritts et al., 2010; Xu et al., 2011].
Corresponding Na lidar temperatures are shown in the same formats as the SAURA winds at right in Figure 5, but only for 18-23 UT, because lidar operations ceased at ~22:40 UT. Comparing the wind and temperature fields suggests that the maximum zonal winds at ~20-24 UT accompany decreasing temperatures at the same altitudes. This differs from the observations at ALOMAR during the same interval in January 2003 [e.g., Williams et al., 2006], where large-scale zonal winds were surprisingly well correlated with the temperatures at the same altitudes. Neither correlation is consistent with a migrating SD tide, but the present phase relations are consistent with a large-scale IGW propagating largely in the zonal direction (eastward), for which $u', w'$, and decreasing $T'$ are largely in phase. Different correlations among the wind and temperature fields can arise from tidal and GW superpositions. For example, the predicted GSWM-09 SD tide $u'$ and $T'$ fields exhibit highly variable phase differences throughout the year due to variable superpositions of the contributing modes. Likewise, GWs propagating in opposite directions will yield opposite correlations of $u'$ with $w'$ and $T'$. Together, ALOMAR wind and temperature measurements, the SD tide fields anticipated by GSWM-09, and the polarization relations for IGWs suggest that these observed large-scale ~12-hr wind and temperature fields are most likely evidence of a large-scale IGW propagating largely eastward. The approximate IGW $u'$, $T'$, and $\lambda_z$ at ~87 km inferred from the SAURA radar and Na lidar (assuming a scale height $H$ ~6 km) are $u' \sim 33$ ms$^{-1}$, $T' \sim 16$ K (maximum negative $dT'/dz \sim -3$ Kkm$^{-1}$), and $\lambda_z \sim 30$ km (a phase descent of ~2.5 km/hr$^{-1}$), with Eq. (12) implying $c \sim c_i \sim \omega_i/2$ $\pi \sim 90$ ms$^{-1}$ (see Table 3). Because this IGW has $\lambda_z/\lambda_h \sim 0.007$ and $v'/u' \sim \omega_i/N \sim 0.7$, $w' < 0.3$ ms$^{-1}$ and $<u_h'w'> < 2$ m$^2$s$^{-2}$, smaller than the expected mean (see Eq. (25) and Table 3).

We turn now to the medium- and higher-frequency GWs (periods of ~1-4 hrs) that appear to modulate the GWs at even higher frequencies and are our focus here. Evidence of these motions is apparent in the Keograms in Figure 4 and in the $u$ and $T$ fields and/or time
series shown in Figure 5. As noted above, an ~4-hr GW having $<T'>$ ~3-5 K is seen throughout the 12-hr Keogram, and some evidence of this periodicity is also seen in $u$, where eastward maxima having significant vertical extent (and large $\lambda_z$) occur near ~17, 21, and 01 UT at the OH airglow layer assumed to be near 87 km. The earlier two maxima appear to be correlated with decreasing $T$, suggesting approximately eastward propagation, as discussed above. The observed $<T'>$ ~3-5 K, large inferred $\lambda_z$, and Eqs. (20) and (24) imply $T' \sim <T'>$, $u' \sim (g/N)T'/T \sim 14$ ms$^{-1}$ (assuming a mean plus ~12-hr GW $dT'/dz \sim -5$ Kkm$^{-1}$ and $N \sim 0.016$ s$^{-1}$ near 01 UT, see below), and more negative, but small, total $dT'/dz$ at this time. Additional evidence for $\phi$ and $c$ for the ~4-hr GW is provided by a 3-5-hr band-pass of the AMTM Keograms (not shown). These indicate no obvious phase progression in the N-S direction, but a relatively high phase speed, $c > 200$ ms$^{-1}$, to the east, confirming the inference above of large $\lambda_z$ in the radar data.

Higher-frequency GWs (periods of ~1-1.5 hr) are more apparent at later times (~22-01 UT) in the Keograms, but are also seen throughout the 12-hr $u$ and $v$ observations and prior to ~22 UT in the $T$ fields displayed in Figure 5. Referring to the SAURA velocities in Figure 5, we see largely anti-correlated $u'$ and $v'$, with $u' \sim 15$ ms$^{-1}$ and $v' \sim 5-10$ ms$^{-1}$, suggesting propagation towards the WNW or ESE from ~16-23 UT and generally correlated, but smaller-amplitude, $u'$ and $v'$ from ~22-01 UT, implying propagation towards the NE or SW. During the earlier interval, we also see a clear superposition of GWs having differing directions of propagation in both Keograms. A 0.5-2-hr band-pass of the Keograms reveals primary propagation directions in an ~NW-SE plane from ~16-19 UT, more towards the NW from ~20-23 UT, and strongly towards the ENE after ~23 UT, consistent with the SAURA $u'$ and $v'$ correlations. The latter interval, in particular, confirms the dominant NE propagation direction of the ~1-hr GW inferred from the SAURA measurements from ~23-01 UT (see the right middle panels of Figure 4).
From the AMTM Keograms at ~87 km, we infer maximum \(<T'> \sim 7-10\) K (an \(\sim 15-20\) K peak-to-peak variation) at \(\sim 23:40\) and 00:40 UT for the \(~1\)-hr GW, which implies \(<T'>/T \sim 4\%\) or greater, and \(u_h' \sim 24\) ms\(^{-1}\) or greater from Eq. (20). This is larger than implied by the \(u'\) and \(v'\) time series from the SAURA radar \(~5\) km higher, suggesting either 1) interference of GWs having similar periods and different propagation directions or 2) influences on the larger-scale velocity field by the localized \(~10\)-min GW packets also having an \(~1\)-hr modulation to be discussed further below. There is little evidence of interference after \(~00\) UT, where the phase slopes in the 0.5-2-hr band-passed Keograms are well defined and imply \(c \sim 60\) ms\(^{-1}\). Local momentum fluxes and flow accelerations are expected to accompany localized GW packets having large amplitudes, however, and this will be assessed further below.

Referring to the SAURA velocities and the band-passed Keograms in Figures 4 and 5, we see maximum eastward \(u'\) and northward \(v'\) at 92 km and nearly coincident \(T'\) maxima at \(~87\) km at \(\sim 23:40\) and 00:40 UT. For a GW propagating towards the NE, we expect these velocities to correlate with the most rapidly decreasing \(T'\). This suggests a roughly in-phase relation among the velocities in the GW propagation direction at \(~92\) km and \(T'\) at \(~87\) km. This implies, in turn, a maximum \(\text{d}u_h' / \text{d}z > 0\) at \(~87\) km and a crude estimate of \(\lambda_z \sim 20\) km for an upward-propagating GW with descending phase. A large \(\lambda_z\) estimate is also implied by both the large \(<T'>\) (suggesting relatively little phase cancellation in the OH airglow layer) and the intrinsic phase speed inferred from the band-passed Keograms and the estimated large-scale flow in the GW propagation direction. AMTM images spanning this period suggest a spacing of small-scale GW packets somewhat smaller than the image diagonal, hence \(\lambda_h \sim 200\) km. With \(c \sim 60\) ms\(^{-1}\) and \(U_h \sim 13\) ms\(^{-1}\) at \(~00:30\) UT, \(c_i = (c - U_h) \sim 47\) ms\(^{-1}\) and Eq. (12) yields \(\lambda_z \sim 2\pi c_i / N \sim 18\) km for a hydrostatic GW having \(N^2 >> \omega_i^2\) and local \(N\)
These inferred velocities suggest $<u'h'w'> \sim 30 \text{ m}^2\text{s}^{-2}$, which is significant relative to a mean of $\sim 5\text{-}10 \text{ m}^2\text{s}^{-2}$ (see Table 3).

Limited intervals of the raw and 0.5-2-hr band-passed Keograms from 23-01:30 UT are shown in the left and right middle panels of Figure 4, respectively. These reveal a very close correspondence between the maximum $T'$ amplitudes of two GW packets having observed periods $T_{GW} \sim 10\text{-}min$ and the maximum $T'$ of the $\sim 1\text{-}hr$ GW at $\sim 23:40$ and 00:40 UT. The second small-scale GW packet in the Keograms at left (the Event 2 focus) propagated towards $\sim 70^\circ$ E of N from 00:15 to 01:00 UT. Expanded AMTM images of this GW packet are shown from 00:16-00:41 UT in the lower panels of Figure 4. Phase progressions were estimated from both the slopes of the phase surfaces in the Keograms and the maxima in the AMTM images; the peak $<T'>$ was estimated as in Event 1 from the power in the 2D Fourier transform for a localized domain within the GW field. Finally, $U_h$ was estimated crudely by interpolation between sparse SAURA radar measurements spanning the interval from $\sim 23:45\text{-}00:45$ UT. During this interval, $U_h$ along $c$ decreased from $\sim 17 \text{ ms}^{-1}$ to $\sim 3 \text{ ms}^{-1}$. The resulting estimates for $\lambda_h$, $c$, $c_i$, and $<T'>/T$ from 00:15-00:45 UT are shown at left in Figure 6. Note, in particular, the decreasing $c_i$ and increasing $<T'>/T$ suggesting an intensifying $\sim 1\text{-}hr$ GW from 00:15-00:30 UT in an environment having $d u_h/dz > 0$ at $\sim 87 \text{ km}$ due to the $\sim 1\text{-}hr$ GW structure in the $u'$, $v'$, and $T'$ fields at this time.

Two additional features of the $\sim 10\text{-}min$ GW packet provide further insights into its character and evolution. The first is a distinct difference in the GW packet horizontal phase and group velocities seen in the AMTM images in Figure 4. The maximum $T'$ is seen initially at the leading phase of the GW packet (see images at 00:16-00:26 UT), but is clearly associated with the second phase at 00:31 UT and thereafter. This suggests a group velocity slower by $\sim 10 \text{ ms}^{-1}$, with $c \sim 50 \text{ ms}^{-1}$ and $c_{gh} \sim 40 \text{ ms}^{-1}$ at $\sim 00:25$ UT and both decreasing with time (see the middle left panel of Figure 6). We expect such a difference based on the GW
dispersion relation, Eq. (12), which reveals a ratio of the intrinsic horizontal group velocity to the intrinsic horizontal phase velocity, and an identical ratio of the vertical group and phase velocities, given by:

$$|c_{ghi}/c_i| = |c_{gz}/c_z| = 1 - \frac{\omega_i^2}{N^2}$$

(29)

assuming an intrinsic reference frame in which $U_h = 0$ (and $W = 0$). For hydrostatic GWs having $m^2 \gg k_h^2$ and $N^2 \gg \omega_i^2$, the group and phase velocities converge. But for finite $\omega_i/N$, Eq. (29) shows that $c_{ghi}/c_i$ and $c_{gz}/c_z$ may depart significantly from the hydrostatic limit. The ratio $c_{ghi}/c_i$ computed from the images in Figure 4 prior to the maximum GW amplitude at 00:30 UT assuming $U_h = 0$ is $\sim 0.75$, suggesting $\omega_i/N = k_h c_i/N \sim 0.45$. However, a smaller ratio (and a larger, more accurate $\omega_i/N$) is obtained accounting for the large-scale $U_h$ decreasing for $\sim 16$ to $12$ ms$^{-1}$ from 00:25 to 00:30 UT. This leads to estimates of $c_i \sim 33$ ms$^{-1}$ and $c_{ghi} \sim 23$ ms$^{-1}$ at 00:27 UT and estimates of $c_{ghi}/c_i \sim 0.7$ and $\omega_i/N \sim 0.55$.

Referring to the AMTM images at 00:36 and 00:41 UT in Figure 4, we note a second interesting feature apparently arising within the phase structure of the $\sim 10$-min GW beginning at $\sim 00:29$ UT. Zoomed images of these structures in the AMTM $I(x,y)$ field are shown from 00:33-00:41 UT at right in Figure 6. This feature begins as a brightening of the leading phase of the GW packet and its initial alignment and motion are consistent with the GW phase orientation and motion until $\sim 00:33$ UT. Thereafter, it stalls suddenly (to $c \sim 10$ ms$^{-1}$), develops a corresponding dark phase, immediately exhibits variations along its length having scales of $\sim 3$-5 km, and appears to also initiate additional variations in brightness that are also aligned with the GW phase and have smaller spatial scales in the plane of GW propagation (see the images in Figure 6 at 00:35 UT and thereafter). For reference, the white ovals in the images in Figure 6 have $c = 0$.

The GW phase structures appear unaffected by this feature, but its amplitude decreases sharply following the appearance of this feature (see the $<T'>$/$T$ plot at lower left in
Figure 6). We cannot say with certainty that this feature is due to the ~10-min GW or that it is an indication of instability accounting for the GW amplitude reductions thereafter. However, the apparent initiation of this feature accompanying a large GW amplitude, its rapid development of apparent instabilities at smaller spatial scales, its stalling relative to the GW phase progression, and the strong decrease in the GW amplitude thereafter are all consistent with previous high-resolution observations and modeling of GW instability dynamics. Indeed, we expect to see exactly these indications of secondary instabilities that exhibit smaller-scale 3D structures and motions following their initiation that accompany the local mean flow rather than the GW phase. An assessment of the momentum flux accompanying this GW is provided below. The relation of these results to previous observations and modeling of GW instability dynamics is discussed further in Section 4.

We now employ the measured and inferred ~10-min GW parameters to estimate its momentum flux and tendency for instability. GW parameters at 00:30 UT obtained from the AMTM are $\lambda_h \sim 23$ km, $c \sim 42$ ms$^{-1}$, $c_i \sim 30$ ms$^{-1}$, and $<T>/T_0 = 0.064$. Together with a local mean $T \sim 170$ K, and an inferred mean and ~12-hr GW $dT'/dz \sim -5$ K km$^{-1}$ and $N \sim 0.016$ s$^{-1}$, these yield estimates of $\omega_i = k_h c_i \sim 0.0082$ s$^{-1}$, $\omega_i/N \sim 0.51$, $(1 - \omega_i^2/N^2) = 0.737$, $\lambda_z \sim \lambda_h/1.68 \sim 13.7$ km, $C^2 \sim 0.395$, $u_{h}' \sim 52$ ms$^{-1}$, $w' \sim 31$ ms$^{-1}$, and $<u_h'w'> \sim 806$ m$^2$s$^{-2}$. Either the $dT'/dz$ estimate for this GW relative to the large-scale $dT'/dz$, or the ratio $u_h'/c_i \sim 1.73$, implies $N^2 < 0$ locally within the GW field and a strongly unstable GW amplitude, hence an explanation for the observed instability structure occurring at the time of maximum amplitude. As in Event 1, additional uncertainty in these estimates accompany the uncertainty in $z_{FWHM}$; the smaller $\lambda_z$ in this case causes a 10% change in $z_{FWHM}$ to yield an ~9% change in $<u_h'w'>$. For the GW parameters here, $\theta'/\theta_0$ and $\rho'/\rho_0$ differ in magnitude by <10%, implying that the approximation in Eq. (17) is valid and there is little uncertainty due to differences in $H$ and $H_p$. Hence the overall uncertainty in the Event 2 $<u_h'w'>$ may be ~40-50%.
Finally, performing a least squares fit of the $T'(x',y')$ field described by Eq. (28) to the AMTM image at 00:30 UT, we obtain FWHM packet dimensions of $x' \sim 50$ km and $y' \sim 37$ km. This GW and its associated momentum flux are thus much more localized than the GW packet in Event 1 and should be expected to yield significant secondary GW generation. The relation of these estimates to previous studies and their implications for MLT dynamics will be discussed in greater detail below.

4. Discussion

Our intent in this paper has been to develop and demonstrate a new quantitative method for assessing the momentum fluxes accompanying individual, small-scale GW packets identified in AMTM measurements. Previous assessments employing multiple types of data from the lower stratosphere into the MLT have suggested that the majority of GW momentum fluxes accompanies GWs occurring on small spatial and temporal scales, with typically $\sim 70\%$ of the total momentum flux due to GWs having $\lambda_h < 100$ km and intrinsic GW periods $T_{GW} < 1$ hr [e.g., Fritts and Vincent, 1987; Reid and Vincent, 1987; Nastrom and Fritts, 1992; Pfister et al., 1993]. Large-amplitude GW packets likely to contribute large momentum fluxes are also often highly localized in space and time [Fritts and Yuan, 1989; Fritts et al., 1992, 2002; Swenson and Mende, 1994; Yue et al., 2009], making them strong sources of secondary GWs penetrating to much higher altitudes [Vadas and Fritts, 2001, 2004]. These findings suggest that a method for quantifying the momentum fluxes and spatial localization of GW packets that can be resolved in AMTM FOVs may be able to make important contributions in quantifying both GW forcing of the MLT and the characterization of secondary GW generation accompanying these events.

4.1. Uncertainties in airglow estimates of GW amplitudes

As noted earlier, the Krassovsky ratio, $\eta = (I'/I)/(T'/T)$, and the cancellation factor, $CF$, employed by various authors (which is similar to $\eta$, but also includes the effects of GW
phase averaging across the finite OH airglow layer depth), tend to be highly variable, with
dependence on temperature, pressure, species chemistry, and the GW $\lambda_h$, $\lambda_z$, and $c_i$ [e.g.,
Krassovsky, 1972; Viereck and Deehr, 1989; Hecht and Walterscheid, 1991; Takahashi et al.,
1992; Hickey et al., 1993; Reisen and Scheer, 1996; Hickey and Yu, 2005; Taori and Taylor,
2006; Vargas et al., 2007]. The observed and predicted variations are easily as large as ~2-5
or more for the GW parameters considered by various researchers [e.g., Hickey and Yu, 2005;
Taori and Taylor, 2006, and references therein]. The uncertainties in $\eta$ or $CF$ also imply
quadratically larger uncertainties in GW momentum flux estimates associated with the
cancellation factor, $CF$, thus very large uncertainties for any estimation of GW momentum
fluxes that relies on $I'/I$ measurements. Indeed, Hickey and Yu [2005] note that $CF$s “... differ
by factors of ~10 between models, implying factors of ~100 between derived gravity wave
fluxes ...” for “… phase speeds less than about 40 ms$^{-1}$...”, and by “… factors of 2-3 ...”
(hence factors of up to ~10 for GW momentum fluxes) between models for phase speeds >60
ms$^{-1}$. Hence, estimates of GW momentum fluxes relying on OH layer $I'/I$ measurements must
be regarded as highly uncertain at present (despite the small uncertainties claimed by some
authors) until further modeling and/or detailed comparisons of coincident $I'/I$ and $T'/T$
measurements are performed for a range of GW and environmental parameters. These results
impact momentum flux estimates reported in a number of previous studies [e.g., Swenson and
Gardner, 1998; Swenson and Liu, 1998; Fritts et al., 2002; Liu and Swenson, 2003; Suzuki et
al., 2007; Vargas et al., 2009].

Similar issues apply to the formulation by Gardner et al. [1999] that has been
employed by various authors [e.g., Tang et al., 2002, 2005a, b; Espy et al., 2004a, b, 2006].
As in Swenson and Liu [1998], Gardner et al. [1999] relate $T'/T$ to $I'/I$ with assumptions
about the GW $\lambda_z$, its growth with altitude (which in general is highly uncertain and variable
due to potential GW transience and dissipation), and the width and airglow emission intensity
of the OH layer. This dependence necessarily exhibits the same uncertainties accompanying the inference of $T'/T$ from $I'/I$. However, Gardner et al. [1999] also employ a spectral rather than a discrete formulation that assumes a specific GW spectral form and separability of the spectral dependence on the GW azimuth of propagation, $\phi$, and intrinsic frequency, $\omega_i$. This assumption fails in cases, such as observed here, where the GW field is composed of discrete events propagating in different directions. In summary, a spectral assessment cannot describe the variances and covariances of discrete GWs.

In contrast, our expression for momentum flux based on airglow temperature perturbations in Eq. (21) is the same as employed by a number of previous authors [e.g., Swenson and Gardner, 1998; Swenson and Liu, 1998; Fritts et al., 2002; Liu and Swenson, 2003; Suzuki et al., 2007] except that we employ direct $T'/T$ measurements. The advantage of Eq. (21) in cases where an AMTM or lidar provides a direct measure of the GW $T'/T$, rather than an indirect estimate from airglow $I'/I$ variations, is that direct $T'/T$ measurements avoid the very large uncertainties due to the uncertain relationship between $T'/T$ and $I'/I$ discussed by Hickey and Yu [2005]. These are by far the largest uncertainties in the estimates of GW momentum fluxes, as the other variables in Eq. (21), e.g., $\omega_i$ and $N$, can be determined with high confidence with combined AMTM measurements of the GW $\lambda_h$, $c$, and $\phi$, correlative lidar measurements of $T(z)$ and inferred $N(z)$, and lidar or radar measurements of the mean wind in the plane of GW propagation, $U_h(z)$. As noted above, the AMTM defines the GW $\lambda_h$, $c$, $\phi$, and $<T'>/T$, to within a few % for temporal averages of a few min. Indeed, larger uncertainties are contributed by geophysical variability over the lifetime of the events described here. Similar uncertainties pertain to the lidar and radar estimates of $T(z)$, $N(z)$, and $U_h(z)$. When averaged over the GW event duration, we estimate the cumulative uncertainty in the $<u'w'>$ estimate to be ~40% or less (e.g., the uncertainties shown in Figures 3 and 5 for...
~30-s estimates for Events 1 and 2 yield much smaller uncertainties spanning the GW packet durations).

4.2. Event 1 GW evolution

The Event 1 GW observed over Logan on 6 June 2013 was an unusual GW in several respects. It appeared to arise “in situ”, apparently propagating from below rather than propagating into the AMTM FOV from the SW. It exhibited a large initial amplitude and expanded horizontally to span several phase fronts from ~07 to 08 UT. This GW had a very small $c$ over the interval shown, despite having a large $c_i$ at these times. The large amplitude in the $T'$ field and the large $\omega_i \sim 0.87 N$ imply GW velocities of $u' \sim 7.3$ ms$^{-1}$ and $w' \sim 12$ ms$^{-1}$ and a significant momentum flux, $<u_h'w'> \sim 43$ m$^2$s$^{-2}$. This GW also had an $I'/I \sim 0.22$ (implying $\eta \sim 6$), which is significantly larger than observed for typical GWs, but significantly smaller than the event discussed by Yamada et al. [2001] for which the momentum flux was estimated by Fritts et al. [2002]. Hence it is not surprising that the inferred momentum flux is ~5-10 times mean summer and winter solstice values at ~87 km measured by radars or inferred from middle atmosphere GCMs [e.g., Tsuda et al., 1990; Fritts and Alexander, 2003].

Finally, the large amplitude, large $\omega_i$, and compact spatial distribution of this GW packet of FWHM $X' \sim 50$ km have other possible implications. While the GW had $u' \ll c_i$, suggesting that it was not overturning, it was in the range of $\omega_i/N$ for which modulational instability is expected [Sutherland, 2001; Dosser and Sutherland, 2011], though this does not imply instability and dissipation. The strong GW packet localization also suggests significant potential excitation of secondary GWs having dominant $\lambda_h \sim 100$-200 km that might readily propagate to much higher altitudes [e.g., Vadas and Fritts, 2001, 2004; Vadas, 2007]. Indeed, the larger momentum fluxes accompanying less frequent, but larger-amplitude, smaller-scale
GW packets may well dominate both the mean forcing of the MLT and the generation of secondary GWs having influences extending well into the thermosphere.

4.3. Event 2 GW evolution

The small-scale Event 2 GW discussed above occurred in the presence of several larger-scale GWs, all of which appeared to contribute to the local environment influencing the propagation and character of this GW. Indeed, the ~1-hr and ~4-hr GWs identified here also contributed momentum fluxes comparable to or larger than mean values. Compared to the Event 1 GW, the small-scale Event 2 GW was much more transient, appeared to be strongly modulated by the ~1-hr GW, and achieved a substantially larger peak momentum flux, $<u'_hw'>$ ~806 m$^2$s$^{-2}$ (~80-160 times mean values), and a larger $I'/I$ ~0.35 (implying $\eta$ ~5.5), accompanying the maximum $T'$ of the ~1-hr GW. The occurrence of transient, high-frequency GWs at the maximum $T'$ phase of larger-scale GWs may provide useful insights into the influences of larger-scale GWs on small-scale GW momentum transport. As noted in Section 3.2, this correlation suggests the presence of a GW-induced wind shear, $du_h'/dz > 0$ at the airglow layer, with $u_h' > 0$ in the direction of propagation of the larger-scale GW that will influence the $\omega_i$ and potentially the vertical propagation of the smaller-scale GW.

The very large inferred peak momentum flux for the Event 2 GW is significantly larger than all previous estimates except that by Fritts et al. [2002] for the GW breaking event described by Yamada et al. [2001], which had $I'/I$ ~0.55 and a somewhat larger inferred momentum flux of $<u'_hw'>$ ~900 m$^2$s$^{-2}$. Indeed, these two events exhibit a number of similarities. These include the following:

1) very similar inferred GW velocities: $u'_h$ ~52 ms$^{-1}$, $w'$ ~31 ms$^{-1}$, and $u'_h/c_i$ ~1.73 for Event 2; $u'_h$ ~50 ms$^{-1}$, $w'$ ~36 ms$^{-1}$, and $u'_h/c_i$ ~1 for the Yamada et al. [2001] event,

2) very similar spatial scales and $\omega_i/N$: $\lambda_h$ ~23 km, $X'$ ~50 km, and $\omega_i/N$ ~0.5 for Event 2; $\lambda_h$ ~27 km, $X'$ ~60 km, and $\omega_i/N$ ~0.5 for the Yamada et al. [2001] event, and
3) rapid GW breakdown following initial instability: likely within ~2 buoyancy periods, $T_b$, though initial instability is not captured in the Yamada et al. [2001] image sequence and the latter stages of instability are not seen in Event 2.

4.4. Implications of large-amplitude events

The similarities of the two events described here, and the GW breaking event examined by Yamada et al. [2001] and Fritts et al. [2002], particularly their small spatial and temporal scales, suggest that such events may be important, but challenging to identify and quantify in a routine fashion. If such events are more common and simply not recognized, however, they may well play major roles in momentum transport and deposition in the MLT and in the radiation of secondary GWs to higher altitudes that are not fully appreciated at present. Additional evidence for large-amplitude dynamics is available from various radars and lidars that have provided previous velocity and temperature measurements in the MLT. As examples, Fritts and Vincent [1987] reported GW momentum flux modulations by the diurnal tide observed over Adelaide, Australia with an MF radar having magnitudes as large as $\pm 30 \text{ m}^2\text{s}^{-2}$; Reid et al. [1988] reported a 3-hr averaged momentum flux magnitude of $\sim 66 \text{ m}^2\text{s}^{-2}$ observed with the SOUSY VHF radar at Andenes, Norway; and Fritts et al. [1992] described measurements at the Jicamarca Radio Observatory exhibiting $>15 \text{ ms}^{-1}$ velocity perturbations at a zenith angle of $2.5^\circ$ and an $\sim 60 \text{ m}^2\text{s}^{-2}$ momentum flux for a 1-hr interval. Very large $w'$ and $T'$, $\sim 30 \text{ ms}^{-1}$ and $\sim 20 \text{ K}$, respectively, for a high-frequency GW (observed period $\sim 8 \text{ min}$) have also been observed previously with the ALOMAR sodium lidar (B. Williams, personal communication, 2014). Summarizing, strong and very strong events contributing significantly to total GW momentum transport and deposition are likely not rare, and imager and AMTM measurements spanning a larger part of the MLT than can be accomplished with radars or lidars provide a viable means of describing their statistics. A
broader survey and quantification of strong events would help determine the statistics, scales, and consequences of their influences at MLT altitudes.

5. **Summary and Conclusions**

We have developed a procedure for quantifying the momentum fluxes associated with localized GW packets having small horizontal wavelengths and potentially small packet widths that are challenging or impossible to quantify with traditional radars, lidars, and/or airglow imagers. This procedure employs the new AMTMs and correlative sodium lidar and/or radar measurements to quantify both the GW environment and all of the intrinsic properties for GW packets that may or may not be contained entirely within an AMTM FOV. Specifically, AMTMs provide accurate estimates of GW $\lambda_h$, $c$, $\phi$, and $<T'/T>$ on short time scales. Sodium lidars provide radial winds, $u_r(z)$, and $(T+T')(z)$ in several beams, hence $U_h(z)$, $T(z)$, $T'(z)$, GW $c_i$ (together with AMTM $c$) and estimates of $u'$, $v'$, and/or $w'$. Finally, VHF, MF, or meteor radars provide large-scale winds, yielding $U_h(z)$, large-scale GW $u'(z)$ and $v'(z)$, and potentially the small-scale GW $u_r'(z)$ in the case of narrow-beam radars.

We have applied our momentum flux estimation procedure to two small-scale GW events observed in June 2013 over Logan, UT and in January 2014 over ALOMAR in northern Norway. Each GW event was characterized by a small $\lambda_h$, a small packet width, $X'$, in the plane of GW propagation, a large AMTM amplitude, $<T'/T>$, a high intrinsic frequency, $\omega_i/N \approx 0.5$, and a large or very large inferred momentum flux, $<u_h'w'> \approx 43$ and 806 m²s⁻², respectively. These estimates are substantially larger than the mean GW momentum fluxes expected at MLT altitudes under solstice conditions provided by previous measurements (primarily radars) and inferred from large-scale models.

Identical capabilities exist with similar combinations of an airglow imager, sodium (or other resonance) lidar, and MLT radar, except for quantification of the GW $<T'/T>$. But this is by far the most critical measurement in quantifying momentum fluxes, and cannot
currently be estimated with the needed precision by airglow imagers providing only $I'/I$. Lidars and radars likewise can provide momentum flux estimates using the dual-beam method of Vincent and Reid [1983] or its extension to multiple beams. But such measurements depend on certain assumptions, especially the requirement for statistical homogeneity of the GW field in all lidar or radar beams. However, this is almost certainly not satisfied for small-scale GW packets by lidars and radars having off-zenith beam angles of 15-20°, for which beam separations at ~90 km are 45-60 km and likely not small compared to GW packet dimensions. To the extent that small-scale GW packets contribute significantly to the MLT momentum budget, neither airglow imagers, lidars, nor radars can be expected to characterize the statistics of such small-scale GW events or their implications for secondary GW generation influencing higher altitudes. Spatial and/or temporal localization of small-scale, large-amplitude GWs could also have contributed errantly to some of the large momentum flux estimates by radars cited above, if GW packet localization caused the assumption of statistical homogeneity at different beams to be violated.

Our measurements of GW packet characteristics and momentum fluxes discussed in this paper raise the question of what fraction of the total momentum flux might accompany such large-amplitude, small-scale GWs, and what are the implications for MLT structure, variability, secondary GW generation, and parameterization of the influences of these dynamics. The implications of a large fraction of the total momentum flux due to such GWs would be significant, yet we have a poor understanding of the statistics of such events at present. The occurrence of small numbers of very strong events is similar to inferences of infrequent, strong mountain wave responses from constant-pressure balloons in the stratosphere by Hertzog et al. [2012]. In the MLT, however, propagation conditions appear to also play a major, and perhaps dominant role. Hence we believe an assessment of the
statistics of such events should be considered a high priority for correlative MLT measurements able to perform such studies.

Finally, AMTMs offer the potential to measure the spatial and temporal distributions of momentum flux for GW packets confined within the FOV. Quantification of the GW parameters also yields an estimate of the vertical group velocity, \( c_{gz} \), given in Eq. (29), hence also the vertical extent of the GW packet, from its observed duration. This enables an estimate of the total momentum accompanying the GW packet arising from its transient momentum flux divergence, or more generally, the Eliassen-Palm (EP) flux divergence \cite{Warner and McIntyre, 1999}, at each location. Such measurements would also enable direct estimates of the spatial scales of body forces yielding generation of secondary GWs that have the potential to propagate to much higher altitudes.

Acknowledgments.

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Table 1. Spatial and temporal resolution of the instruments at BLO and ALOMAR used in this study. *The AMTM averages over the OH layer depth.

<table>
<thead>
<tr>
<th>Instrument &amp; location</th>
<th>Vertical resolution</th>
<th>Horizontal resolution</th>
<th>Temporal resolution</th>
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<tr>
<td>AMTM, BLO &amp; ALOMAR</td>
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<td>0.56 km, (320x256) pixels</td>
<td>35 sec</td>
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<tr>
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<td>--</td>
<td>5min</td>
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<tr>
<td>Meteor radar, BLO</td>
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<td>1 hr</td>
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<td>--</td>
<td>10 min</td>
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<td>SAURA radar, ALOMAR</td>
<td>1 km</td>
<td>--</td>
<td>7.5 min</td>
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</table>
Table 2. Measured and inferred GW parameters for Event 1. Uncertainties greater than ~10% are indicated by a range of values or denoted by a “~”.

| $T_{GW}$ (from N) | $\phi$ (from N) | $T''$ (K) | $c$ (ms$^{-1}$) | $c_i$ (ms$^{-1}$) | $\lambda_h$ (km) | $\lambda_z$ (km) | $u_h'$ (ms$^{-1}$) | $w'$ (ms$^{-1}$) | $|dT'/dz|$ (Kkm$^{-1}$) | $<u_h^2_w'>$ m$^2$s$^{-2}$ |
|------------------|-----------------|----------|----------------|-----------------|-----------------|-----------------|-----------------|----------------|------------------|-------------------|
| 70 min           | ~40° (NE)       | 7.8      | ~3             | 52              | 12.5            | 21.7            | 7.3             | ~12            | ~2               | ~43               |
Table 3. Measured and inferred GW parameters for Event 2. Uncertainties greater than ~10% are indicated by a range of values or denoted by a “~”.

<table>
<thead>
<tr>
<th>$T_{GW}$ (hr)</th>
<th>$\phi$ (from N)</th>
<th>$T''$ (K)</th>
<th>$c$ (ms$^{-1}$)</th>
<th>$c_i$ (ms$^{-1}$)</th>
<th>$\lambda_h$ (km)</th>
<th>$\lambda_z$ (km)</th>
<th>$u_{h'}$ (ms$^{-1}$)</th>
<th>$w'$ (ms$^{-1}$)</th>
<th>$dT'/dz$ (K km$^{-1}$)</th>
<th>&lt;$u_h'w'&gt;$ m$^{-2}$ s$^{-2}$</th>
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<td>~5-10</td>
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<tr>
<td>~4-hr</td>
<td>~90° (E)</td>
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<td>&gt;2,800</td>
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<td>~1</td>
<td>~0</td>
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<td>~1-hr</td>
<td>~70° (NE)</td>
<td>~7-10</td>
<td>~60</td>
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<td>~200</td>
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<td>30</td>
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<td>52</td>
<td>~31</td>
<td>~5.5</td>
<td>~806</td>
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**Figure 1.** (top) Example GW packet geometry as seen by the AMTM relating GW scales and orientation. (middle and bottom) Examples of N-S and E-W Keograms and the relations between apparent wavelengths and phase speeds and the observed GW period and phase speed.
Figure 2. (top) 6.5-hr segments of the N-S and E-W Keograms for the Event 1 GW observed over Logan, UT on 6 June 2013. The GW of interest is that showing very little phase motion during the interval examined, from 7:40 to 8:00 UT shown with dashed lines. (bottom) AMTM brightness and temperature fields at 10-min intervals spanning the times of interest. Keograms were computed from the central pixel row or column of the detector for each direction. The lower right panel also shows the locations of the GW relative to Logan (“x”), BLO (blue square), and the east beam of the USU Na lidar at 87 km (black square). Spatial scales of the images are shown at lower left.
Figure 3. (top) Meteor radar winds in the plane of GW propagation from 1-hr averages centered at 7:30 and 8:30 UT (at left), and interpolated to 8:00 UT, and 30-min Na lidar temperature profiles centered at 7:30, 8:00, and 8:30 UT (at right). (center and bottom) AMTM estimates for the GW $\lambda_h$, $c$, $c_i$, and $<T'/T>$ at ~4.5-min intervals spanning the times of interest. Error bars on the line plots in the lower three panels show the uncertainties for 30-s estimates. Error bars are not shown for $c_i$ because measured $U$ uncertainties are not known. Variations at longer time scales represent geophysical variability.
Figure 4. (top) 12-hr segments of the N-S and E-W Keograms for Event 2 observed over ALOMAR on 27-28 January 2014. Seen are apparent periods of ~12, 4, and 1-1.5 hr and the Event 2 GW of ~10 min between 00 and 01 UT. (middle) Expanded view of the Event 2 GW Keogram interval (left) and this same Keogram with a 0.5-2-hr bandpass highlighting the ~1-hr GW background. (bottom) AMTM temperature image sequence showing the evolution of the Event 2 GW. Note that the strongest phase front lags the GW phase speed over this interval. Times in the lower images are in UT for comparison with the Keograms. Spatial scales of the images are shown at lower left.
Figure 5. (left) Zonal and meridional winds from the SAURA MF radar at 7.5-min resolution from 16:02 UT on 27-28 January 2014 from 80-100 km (upper panels) and at 92 km (lower panel). (right) Na lidar temperatures at 10-min resolution from 18:40-22:30 UT on 27 January 2014 from 80-100 km (upper panel) and at 90 km (lower panel).
Figure 6. (left) AMTM estimates for the Event 2 GW $\lambda_h$, $c$, $c_i$, and $<T'/T>$ at ~1.3-min intervals spanning this event. (right) AMTM intensity images showing the initiation and evolution of an apparent instability feature accompanying the maximum GW amplitude in Event 2. Note the very different horizontal phase speed and evolution to 3D structure accompanying this event. Error bars on the line plots in the left three panels show the uncertainties for 30-s estimates. Error bars are not shown for $c_i$ because measured $U$ uncertainties are not known. Variations at longer time scales represent geophysical variability. Spatial scales of the images are shown at lower right.