I. INTRODUCTION

Unconventional superconductors are of great scientific interest because they potentially play host to Cooper pair binding mechanisms that are different from the electron-phonon interaction of conventional superconductivity.\(^1\) The different spatial distributions of higher angular momentum pairing mean that the electrons of Cooper pairs sit in very different Coulomb potentials, and are likely to be stabilised by different binding mechanisms. Therefore, in order to inform theoretical developments, the pairing symmetry in a material must first be unambiguously established, and in this regard the scientific debate on \(\text{Sr}_2\text{RuO}_4\) is ongoing.\(^2,3\)

Early Knight-shift measurements strongly suggested that the superconductivity in \(\text{Sr}_2\text{RuO}_4\) is spin-triplet,\(^4\) with p-wave being favoured due to energetic considerations.\(^5\) Evidence for broken time reversal symmetry came from \(\mu\)SR,\(^6\) and polar-Kerr measurements\(^7\) which, along with considerations of the crystal structure of \(\text{Sr}_2\text{RuO}_4,\(^8\) uniquely identified a two-component chiral p-wave order parameter \((d = \Delta_0(k_x \pm ik_y)\hat{z})\) in d-vector notation as the most likely candidate. However, additional experimental evidence for this is inconclusive.\(^3,9\) Much interest surrounds an apparent discrepancy between theory and experiment regarding spontaneous currents (fields) that are expected to arise as a direct consequence of such a pairing symmetry wherever translational symmetry is broken.\(^2\) These “smoking gun” signals, predicted at sample edges and domain walls formed between regions of opposite chirality,\(^10,11\) have been proposed as the source of the internal fields detected by early \(\mu\)SR measurements,\(^6\) but have so far evaded detection by real-space scanning probe measurements, although they are predicted to be readily detectable.\(^12,13\)

Recent scanning Hall probe microscopy (SHPM) measurements on \(\text{Sr}_2\text{RuO}_4\) illustrated that striking differences in behaviour can be observed between single crystals from different growth batches, even if they are grown under the same nominal conditions.\(^14\) Such sensitivity to crystal quality highlights the importance of extending the search for chiral signals to crystals from different batches with the highest possible degree of order. Scanning SQUID measurements were able to image over the as-grown edge of a single crystal,\(^13,15\) but as yet no measurements over a controlled, well-defined microstructured edge have taken place. Here we describe a series of measurements of mesoscopic disks, etched into the surface of a very high quality sample. The disk edges provide well defined locations where translational symmetry is broken and so would be expected to host observable chiral edge fields. Theoretical investigations of mesoscopic (sample dimensions \(\sim \lambda,\xi\)) chiral p-wave superconductors also predict the emergence of several new magnetic phenomena such as chirality-dependent vortex structures,\(^16\) fractional vortices that contain \(\Phi_0/2,\) and \(2\pi\) vortices \((2\Phi_0)\) which should all be readily detectable by our Hall probe microscope.

It is against this background of complex materials science, a desire to investigate magnetic signatures at sharp
II. EXPERIMENTAL METHOD

Superconducting Sr$_2$RuO$_4$ single crystals were grown using the floating-zone technique with Ru self-flux in a commercial image furnace, and annealed in air (1500 C for 3 days) to remove lattice defects and reduce vortex pinning. Figure 1 shows both the real ($\chi'$) and imaginary ($\chi''$) components of ac susceptibility measurements on the sample prior to annealing and patterning. Both curves are extremely sharp, indicative of low levels of disorder. Defining $T_c$ as the point where $\chi'$ falls to 10% of the low temperature value, and the transition width $\Delta T_c$ as the temperature interval during which $\chi'$ falls from 10% to 90% of the low temperature value, we find $T_c \approx 1.50K$ and $\Delta T_c \approx 0.14K$, which represents the current state-of-the-art for this material, confirming that we have extremely high quality single crystals. Optical lithography and Argon ion milling were used to etch an array of shallow cylindrical pillars into the cleaved ab surface to a depth of 400nm. The inset to Figure 1 shows an optical micrograph of the array of well separated disks which have radii (R) of 2.5, 5, 7.5, 10 $\mu$m.

SHPM has been used to image the stray fields at the ab surface of the sample. This employs standard scanning probe techniques to approach and scan the sample surface with a nanoscale Hall effect sensor with an integrated STM tip. The active area of the Hall cross (800nm×800nm) was defined in an AlGaAs/GaAs heterostructure (2DEG) using electron-beam lithography and wet chemical etching. The sensor is approached towards the sample until a tunnelling current is established at the STM tip. The Hall probe is then retracted a small distance (typically $\sim 100$nm) from the surface to allow safe scanning at high rates. Owing to the strong surface topography of this sample, the sample/sensor separation is somewhat larger than typical and is estimated to be $\sim 1.81$µm by fitting profiles of individual vortices within the disks. We note that it is challenging to distinguish sample/sensor separation and $\lambda$ from such fits [cite Kogan]. Further details of the microscope used for these measurements can be found elsewhere.

III. RESULTS

All of the following SHPM images were captured above the ab surface with magnetic field applied parallel to the crystalline c-axis. If the field is increased after cooling through $T_c$ the sample exhibits a pronounced critical state with complete flux screening from the imaging region at low fields. Increasing the applied field to achieve full penetration leads to the entrance of multi-vortex bundles in an uncontrolled fashion. For this reason all of the following measurements employ a field-cooling protocol from above $T_c$ leading to vortex distributions that are close to equilibrium.

In order to be able to distinguish spontaneous edge currents from conventional Meissner screening currents, and to reduce the probability of breaking the degeneracy of the two chiral states, the applied field was carefully adjusted until contributions from the Earth’s field and remnant fields from the cryostat were cancelled out to achieve as close to a true zero field as possible $H_{\text{eff}} = 0$, as defined by vortex free images in the field-of-view. Such a sequence is displayed in Figure 2 where the scan area was centred over a R=5$\mu$m disk. In small fields vortices are trapped outside the disk and nucleate at preferred pinning sites close to the disk edges where they are observed to order in an approximately triangular formation with a spacing close to that expected for an ideal triangular lattice at this field strength, $a_{\text{tri}}(0.125G) \approx 13.8\mu$m. At zero effective field a ring of weak image contrast is observed near the perimeter of the disk which was shown to be an artefact attributable to electrostatic gating of the Hall sensor. The SHPM technique requires the application of a small sample bias (0.2V) to allow surface detection via tunnel currents from the grounded STM tip. The relatively high sample topography modulates the electric field between sample and sensor and creates an additional parasitic ‘gating’ signal during scanning. A definitive test of whether image contrast is due to a real magnetic feature or a gating signal is to scan the same area above $T_c$. Figure 2(f) contains this image and reveals that the feint disk outline observed at $H_{\text{eff}} = 0$ is also present for $T > T_c$. The numerical difference of images at the two temperatures confirms that there is no
magnetic contrast in the zero field image that can be attributed to chiral edge or domain wall currents above the measurement noise threshold of ±2.5 mG. A similar analysis was conducted for the $R = 2.5 \mu m$ disk and returned the same result.

Figure 3(a) shows images of the same $R = 5 \mu m$ disk after field-cooling in increasing applied fields up to 100 Oe. For low fields, the number of vortices nucleating at the disk edge increases and the disk becomes clearly visible by virtue of its complete flux screening. Eventually, at 1.25 Oe a single vortex penetrates the disk, followed by a second at 1.88 Oe. Individual vortex resolution is lost at ~5 Oe but even in fields up to 20 Oe, when we estimate the disk already contains ~70 $\Phi_0$, a rather inhomogeneous flux distribution is resolved, suggestive of the presence of a quite strong non-uniform pinning potential in the sample. Surprisingly, at 25 Oe the flux distribution inside the disk suddenly becomes completely homogenous within the resolution of the experiment ($\Delta B \approx 5$ mG, spatial resolution $\approx 1.8 \mu m$). This is shown by the linescans across the disks at 20 and 25 Oe (dashed lines), inset in 3(b). Flux continues to preferentially enter the disk homogeneously up to the highest measurement field of 100 Oe, as demonstrated by the diminishing image grayscales shown in (b). At these high fields the grayscales reflect the strength of the diamagnetic screening from the disks. Even at 100 Oe this is appreciably higher than the signal strength of the diamagnetic screening from the disks.

The theoretical fits based on edge and bulk currents when the flux distribution has become homogenous, reveal a steep edged and flat bottomed inverted “top hat” shape to the field profile (Fig. 4). Theoretical comparisons have been made with the critical state model of Clem and Sanchez, using microscopic disks in the high-field limit, when $J_c$ flows everywhere within the disks. The sample/sensor separation ($\approx 1.81 \mu m$) is taken into account when simulating the experimental magnetic field profile. Figure 4 illustrates that the theoretical calculations of the disk field profile based solely on a uniform bulk current ($J_c$) provide a very poor fit to the observed field profiles (dotted lines). Good agreement with the experiment is only achieved when edge currents are included, ($J_E \gg J_c$). In practice, following the approach for the geometrical barrier, profiles with $J_E$ flowing within $d/2$ of the sample edge, where $d = 400nm$ is the disk thickness, and $J_c = 0$ are found to give excellent agreement with the experimental field profiles, (solid lines, Fig. 4). In fact the profile is dominated by $J_E$ and rather insensitive to $J_c$ allowing us to set a limit of $J_c < 10^7 Am^{-2}$. For $J_c > 10^7 Am^{-2}$ the bottom of the profile becomes more rounded and the good agreement is lost.

The theoretical fits based on edge and bulk currents
FIG. 4. (Color online) Experimental magnetic field profiles (circles) across mesoscopic Sr$_2$RuO$_4$ disks (R=5µm) captured after field-cooling from $T > T_c$ to $T=260$mK in applied fields of 30, 40 and 100Oe. Two theoretical fits are shown. First, assuming a constant bulk critical current $J_c=7.75$, 6.5 and 6.0 $\times 10^4$Acm$^{-2}$ respectively (dotted lines), and a second assuming edge supercurrents ($J_E=1.55, 1.25$ and 1.15 $\times 10^6$ Acm$^{-2}$ respectively) flowing within $d/2$ of the edge of the disk and $J_c=0$ (solid lines).

FIG. 5. (Color online) Calculated edge current densities flowing in the R=2.5 and 5µm disks at various applied fields.

are made assuming constant sample/sensor separation ($z=1.81$µm) and are solely parameterised by $J_E$ and $J_c$ respectively. The strength of the screening of flux from the disk at high fields decreases with increasing field as demonstrated by the decreasing magnitudes of the inverted “top hat” profiles in Figure 4. This trend is also captured by the image grayscale values displayed in Figure 3(b). Fits to disk profiles captured at different $H_{\text{eff}}$ therefore require a field-dependent $J_E(H_{\text{eff}})$, as plotted in Figure 5.

The disk edges were observed to play a prominent role in the vortex structures formed in the $R=10$µm disk at $T=1$K shown in Figure 6. Six vortices are seen to form a ring at the centre of the disk, reflecting the rotational symmetry of the mesostructure, in what looks like a discrete analog of Zeldov’s continuous flux dome,24 that is predicted to occur as a consequence of strong edge currents resulting from the geometrical barrier. The bright object at the top-most vertex of the ring contains two vortices whose separation is below the spatial resolution of our experiment. This, and the two additional vortices just inside the disk boundary suggest that pinning forces are still playing a strong role at this temperature.

IV. DISCUSSION

Previously attempts have been made to induce chiral currents in Sr$_2$RuO$_4$ single crystals by introducing an array of 1µm diameter, 1µm deep holes using focussed ion-beam milling. In practice these proved to be very weak vortex pinning centres, and so their effectiveness as sites of broken translational symmetry generating spontaneous chiral edge currents was questioned by the authors. In contrast, the mesoscopic disks discussed here have been observed to have a profound impact on the vortex physics of the system. At very low fields (Fig. 2) vortices are screened from the disks by strong edge currents and take up locations at pinning sites on or near the disk edge, and upon penetration arrange into (disordered) rings at the disk centre, presumably driven in part by currents flowing at the disk edges (Fig. 6). However, despite the presence of sharp sample edges, we see no evidence for spontaneous currents near the edge of the disks that could be attributed to a chiral order parameter. Nor were we able to resolve any spontaneous currents arising at chiral domain walls. We conclude that if present, magnetic signatures from chiral edge currents and chiral domain walls are below the $\pm 2.5$mG noise floor of this experiment.

Figure 7 presents a simulation of the magnetic field signal we would expect to measure above sample edges in a semi-infinite superconducting sample with a chiral p-wave order parameter, where it is assumed that the superconductor is two-dimensional with a single cylindrical Fermi surface. The exact numerical solutions to the inhomogeneous London equations of Matsumoto and Sigrist are complex and cumbersome to derive. Instead Figure 7 presents results based on an adaption of the fitting protocol of Bluhm (equation 1), from which we have calculated the appropriate supercurrent density via Maxwell’s equation (equation 2), and modified to account for the sensor height via the Biot-savart procedure described by Roth et al. Following these steps we arrive at the equation for the stray fields at sample edges (equation 3). In addition the plot shown in Fig. 7 includes averaging to account for the finite Hall probe active area. From this
with established theories of surface barriers, and recent investigations of vortex penetration and expulsion in field-cooled YB$_2$Cu$_3$O$_{7-δ}$ and Nb strips.

As the field is increased further, the vortex density in the disk increases and single vortex resolution is lost. Previous studies of similar disks in BSCCO-2212 have captured evidence of a vortex ‘dome’ forming at the centre of the disk, consistent with the theory of the geometrical barrier. In Sr$_2$RuO$_4$ at 300 mK, in applied fields up to 20 Oe we do not observe a smooth dome but instead a rather inhomogeneous vortex distribution is captured, indicative of a low density of rather strong pinning sites. Tellingly, the grayscale at 20 Oe of 2.72G is about four times greater than that for a single isolated vortex (∼0.6G c.f. Fig. 3(c)), reflecting the fact that the vortices are screened by the strong edge currents resulting in high contrast between the disk and the interstitial regions.

It is therefore surprising that at 25 Oe the vortex distribution inside the disk abruptly becomes homogeneous. It is as if the pinning forces responsible for the inhomogeneity are suddenly “turned off” at this field strength. Interestingly, this also coincides with a peak in the field profile across the disk, which falls quite steeply at higher fields (H$_{\text{eff}}$ ≥25 Oe), as captured by the gradually decreasing gray scales of the images (Fig. 3(b)). Previous theoretical work has predicted that a rotation of the order-parameter d-vector into the a-b plane can occur at sufficiently high c-axis fields, resulting in a profound change of behaviour of the system. In this instance the Cooper pair spins would be parallel to the external field and the degeneracy of the two chiral states would be lifted. More recently, four component Ginzburg-Landau models predicted that three different order parameters can be stabilised in the H-T phase diagram for fields applied along the c-axis. The exact field at which the rotation occurs is not well known but an upper bound of 200 Oe has been suggested. The abrupt change in vortex pinning behavior above 20-25 Oe may be the signature of a field-driven change of the order parameter of this type. We also note that the abrupt change in pinning behavior occurs close to the maximum field at which a dramatic increase in the Meissner fraction was recently observed in μSR measurements at low temperatures, something that was tentatively attributed to a long-range vortex attraction arising from multiband effects. Hence it is possible that these two observations have a common physical origin.

Linescans of the disks at H$_{\text{eff}}$ ≥25 Oe display a steep-sided and flat-bottomed magnetic profile (Figure 4). Critical state theory for saturated thin disks yields very poor agreement with experiment, c.f. dotted lines in Figure 4. However, good agreement is reached with a field profile derived from a model containing only edge currents (J$_E$) flowing within a distance d/2 of the sample edge, c.f. solid lines in Figure 4.

The edge currents used in the disk profile fitting shown in Figure 4 are J$_E$ ~ 2 × 10$^{10}$ Am$^{-2}$ and compare
favourably with theoretical predictions of the geometrical barrier: \( J_E^{GB} = 2H_{c1}/d \sim 10^{10} \text{Am}^{-2} \). This is seemingly in direct conflict with the indications of strong pinning observed below 25 Oe in this experiment, and in previous SHPM measurements of the same sample.\(^{14}\) Up to now we have ignored the fact that the “disks” of this study are not free standing but are on-top of a \( \sim 1\text{mm} \) thick Sr\(_2\)RuO\(_4\) platelet. If bulk pinning were strong, one would expect this to dominate over the role of the relatively thin microfabricated disk. However, in the limit \( J_c = 0 \) it can be completely ignored. The fact that the disk plays such a dominant role at all fields is also consistent with a small value of \( J_c \).

The disks studied here are in the regime \( R \ll \xi_0 \) and \( R \sim 25\lambda \) and so are only nominally in the mesoscopic limit, except very close to \( T_c \).\(^{40}\) It is therefore interesting that we observe the formation of a (disordered) vortex ring, reflecting the rotational disk symmetry, at the centre of the \( R = 10\mu \text{m} \) disk at \( T = 1\text{K} \) \((H_{\text{eff}} = 1 \text{ Oe})\). This provides direct evidence of the influence of the disk boundaries on the internal vortex configuration. Many images at low temperature have provided evidence of a low density of strong pinning sites in this sample. In this instance the formation of a vortex ring is probably aided by the increased measurement temperature of 1K which facilitates the thermal excitation of vortices off the pinning sites, allowing the intrinsic vortex-vortex interactions to determine the vortex configuration. The formation of such a vortex ring is consistent with predictions for “large” mesoscopic disks.\(^{41}\)

V. CONCLUSION

Large mesoscopic disks have been milled into the ab surface of a high quality Sr\(_2\)RuO\(_4\) single crystal in order to provide well-defined regions of broken translational symmetry where current theory for the \( \tilde{d} = \Delta_0(k_x \pm ik_y)\xi \) chiral order parameter predicts spontaneous chiral currents (fields) should form. Scanning Hall probe images reveal no spontaneous magnetic signal at the disk edges above the experimental noise threshold of \( \pm 2.5\text{mG} \), placing an upper limit of \( \approx 0.8\% \) of theoretical predictions. Neither do we observe any magnetic signal anywhere else in the sample that could be attributed to the signature of a chiral domain wall. After field-cooling from \( T > T_c \) the disks strongly screen magnetic flux at the highest fields. Theoretical fits to magnetic field profiles of the disks for \( H_{\text{eff}} > 25 \text{ Oe} \) indicate that the screening is dominated by edge currents flowing within \( d/2 \) of the disk edge, and that the system is in the weak pinning limit \((J_E \gg J_c)\). This final observation is in direct contradiction with several pieces of evidence that suggest the presence of a low density of rather strong pinning sites at low temperatures and low fields \((H_{\text{eff}} < 25 \text{ Oe})\). An abrupt change in the vortex pinning and screening behaviour above 25 Oe may indicate a field-driven change in the order parameter.

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