Conserved cis-regulatory modules control robustness in *Msx1* expression at single cell resolution

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ABSTRACT

The process of transcription is highly stochastic leading to cell-to-cell variations and noise in gene expression levels. However, key essential genes have to be precisely expressed at the correct amount and time to ensure proper cellular development and function. Studies in yeast and bacterial systems have shown that gene expression noise decreases as mean expression levels increase, a relationship that is controlled by promoter DNA sequence. However, the function of distal *cis*-regulatory modules (CRMs), an evolutionary novelty of metazoans, in controlling transcriptional robustness and variability is poorly understood. In this study, we used live cell imaging of transfected reporters combined with a mathematical modelling and statistical inference scheme, to quantify the function of conserved *Msx1* CRMs and promoters in modulating single cell real time transcription rates in C2C12 mouse myoblasts. The results show that the mean expression-noise relationship is solely promoter controlled for this key pluripotency regulator. In addition, we demonstrate that CRMs modulate single cell basal promoter rate distributions in a graded manner across a population of cells. This extends the rheostatic model of CRM action to provide a more detailed understanding of CRM function at single cell resolution. We also identify a novel CRM transcriptional filter function that acts to reduce intracellular variability in transcription rates and show that this can be phylogenetically separable from rate modulating CRM activities. These results are important for understanding how the expression of key vertebrate developmental transcription factors is precisely controlled both within and between individual cells.

Keywords: single cell transcription, *cis*-regulatory module, *Msx1*, promoter, robustness
INTRODUCTION

Transcription is a fundamentally stochastic process that occurs discontinuously in bursts in single cells as described by random telegraph models of gene expression (Cai, et al. 2006; Paulsson 2005; Pedraza and Paulsson 2008; Raj, et al. 2006; Raser and O'Shea 2005; Suter, et al. 2011). Experiments in microbial systems and in Drosophila have revealed that stochasticity in gene expression can be actively used to generate cellular diversity of adaptive value in large cell populations (Samoilov, et al. 2006; Wernet, et al. 2006), whilst in vertebrates, cell-to-cell variations in the expression of key developmental regulators in progenitor cells have been shown to drive cell fate choices during lineage differentiation (Chang, et al. 2008; Raj and van Oudenaarden 2008). Comparative embryology and developmental genetics, on the other hand, have revealed that transcription factor and signalling networks are expressed and deployed in a highly stereotypic and exquisitely precise spatio-temporal fashion during development. Furthermore, studies in yeast have shown that the expression of essential, haplo-insufficient genes is controlled in a more precise manner when compared to non-essential genes, such as those involved in the stress response, and that noise in the expression of these dose dependent genes appears to have been reduced by natural selection to prevent deleterious stochastic variations (Batada and Hurst 2007; Lehner 2008; Newman, et al. 2006). Random fluctuations in gene expression are therefore subject to regulation and can be either beneficial or deleterious for cell function depending on the type of gene and biological process.

Noise and robustness in gene expression can be controlled at a number of different levels. A large number of studies in yeast and bacteria have demonstrated that noise in gene expression decreases as mean expression levels increase (Bar-Even, et al. 2006; Newman, et al. 2006), and that promoter sequence, length and chromatin structure are all major...
determinants of this relationship (Carey, et al. 2013; Hornung, et al. 2012; Tirosh and Barkai 2008). In addition, random fluctuations in gene expression can be buffered at both the RNA and protein levels (Barriere, et al. 2011; Pedraza and Paulsson 2008; Raser and O’Shea 2005), while signalling pathways such as \textit{wnt} have been proposed to filter out and reduce transcriptional noise (Arias and Hayward 2006). Moreover, transcription factors do not function in isolation but work in a highly coordinated manner within gene regulatory networks (GRNs) and particular network motifs, for example, feed-forward or feedback loops, have been shown to buffer out fluctuations in gene expression (Alon, et al. 1999; Barkai and Leibler 1997; Macneil and Walhout 2011; Mangan and Alon 2003).

Within GRNs key transcription factors interact with DNA sequence elements called \textit{cis}-regulatory modules (CRMs), such as transcriptional enhancers and silencers, and promoters, to control the expression of large numbers of target genes (Jeziorska, et al. 2009). Communication between CRMs and their target promoters is a key metazoan novelty in transcriptional control. CRMs may be predicted to play an important role controlling transcriptional noise as, for example, shadow enhancers in Drosophila have been shown to promote gene expression robustness in response to various stimuli (Boettiger and Levine 2009; Frankel, et al. 2011). However, the full dynamic scope of CRM function beyond spatiotemporal control has still to be determined and the majority of studies investigating the control of transcriptional noise have been performed in bacteria and yeast. As such, the involvement of CRMs in regulating transcriptional variability has not been well explored (Macneil and Walhout 2011).

In this study, we used live cell imaging of transfected reporters and mathematical modelling to quantify the function of mouse-fugu conserved \textit{Msxl} CRMs and promoters in regulating single cell transcription rates in real time in C2C12 mouse mesenchymal cells. We
predicted that variability in the expression of *Msx1* would be finely controlled as *Msx1* is an important regulator of pluripotency in mesenchymal stem cells, acting at a key node in a GRN, to control proximodistal branchial arch patterning and craniofacial and dorsal CNS development (Hu, et al. 2008; Odelberg, et al. 2000; Satokata and Maas 1994). Also, the spatial and temporal expression of *Msx1* is highly conserved across vertebrates and appears to show an ON/OFF behaviour akin to ultrasensitivity (Hu, et al. 2008). Our results showed that the negative correlation between transcriptional noise and mean expression is not determined by distal CRMs but is solely promoter derived for vertebrate *Msx1*. We found that *Msx1* CRMs function to modulate single cell basal promoter rate distributions in a graded manner across a population of cells. This further refines the rheostatic model of CRM action, proposed on the basis of single time point reporter measurements, to provide a more detailed understanding of CRM function. Unexpectedly, our results also identified a novel CRM transcriptional filter, or robustness control, function that acts to reduce intra-cellular variability in transcription rates. By combining promoters with homologous mouse-fugu CRMs we identified examples of conservation and divergence in CRM function and showed that CRM robustness control can be phylogenetically separable from rate modulating CRM activities. These results are important for understanding how the expression of key developmental regulators is finely controlled, which in principle will also have important ramifications for synthetic biology and gene therapy.
MATERIALS AND METHODS

Plasmid Construction

The pGL3-vGFP3xnls Venus fluorescent protein reporter plasmid used as a backbone for all species specific CRM-promoter reporter constructs was cloned as follows: recombinant PCR was performed to insert a triple nuclear localisation sequence in frame at the 3’ end of the Venus gene from pCS2Venus. This generated a vGFP3xnls fragment flanked by NcoI-XbaI sites. The luciferase gene from pGL3-BASIC (Promega) was then excised as an NcoI-XbaI fragment and replaced with vGFP3xnls. Species specific CRM-promoter hybrid fluorescent reporters were then generated as follows: the mouse and fugu Msx1 promoter regions were PCR cloned as HindIII fragments from genomic DNA and inserted into pGL3-vGFP3xnls. The SV40 promoter was PCR amplified as a HindIII fragment from pGL3-PRO (Promega) and cloned into pGL3-Venus. Individual species specific CRMs were then PCR amplified as XmaI-BglIII fragments from genomic DNA and cloned upstream of the respective promoter Venus reporters. The fidelity of all reporter constructs was verified by sequencing. The oligonucleotides used are shown in Supplemental Table 1.

Cell culture

C2C12 myoblast cells were grown in Dulbecco’s modified Eagle’s medium supplemented with 10 % foetal bovine serum (Growth Medium (GM)).

Flow cytometry

Flow cytometry based measurement of reporter activity was performed as described in (Jeziorska, et al. 2012). 2x10^5 cells per well were seeded in 6-well plates. The next day cells were transfected with 1 µg of pGL3-vGFP3xnls reporter plasmid and 250 ng pCMV-mCherry expression vector using lipofectamine 2000 (Invitrogen). pCMV-mCherry contains the
cytomegalovirus promoter driving the expression of a mCherry reporter and was used to control for transfection efficiency. After 42-46 hours cells were washed twice with PBS, trypsinized and harvested in 1 ml GM. GM was removed, cells were then washed twice with PBS, resuspended in 800 μl Cell Fix (BD Biosciences) and incubated overnight at 4 °C in the dark. To activate wnt signalling 40 mM LiCl was added to each well 20 hours after transfection.

To measure MSX1 protein levels, cells were pelleted, washed with PBS and then permeabilised using 0.1% Triton X-100 in PBS for 15 min at room temperature. Cells were subsequently washed with PBS and blocked using 20% FBS in PBS for 1 hour at room temperature. Cells were then incubated overnight at 4 °C with 1:200 dilution anti-Msx1 (Clone 4FII; Abcam) mouse monoclonal antibody, washed three times with 5% FBS in PBS and incubated for 1 hour with 1:200 dilution goat anti-mouse AlexaFluor647 antibody (Invitrogen). Cells were washed again with PBS, resuspended in 500 μl Cell Fix and analysed on a BD Influx Cell Sorter. Venus was excited using the blue laser (488 nm) and measured with the 530/40 bandpass (BP) filter set, mCherry was excited using the yellow laser (561 nm) and measured using the 593/40 BP filter while Alexa647 was excited with the red laser (642) and measured using the 670/30 BP filter set.

**Real Time Imaging**

1.25X10^4 cells per well were seeded in 0.17 mm glass bottom 96-well plates (MatriCal). The next day cells were treated with Hoechst 33342 (Invitrogen) to label individual nuclei. To do this, GM was removed, cells were washed twice with PBS and then incubated with 400 ng/ml Hoechst in GM at 37°C for 30 min. Cells were then washed twice with PBS and GM without phenol red was added back to the well. Cells were then transfected with 200 ng reporter plasmid using Lipofectamine 2000 (Invitrogen) according to the manufacturer’s instructions.
The 96 well plate was subsequently transferred to a Cellomics KineticScan KSR machine. The KSR contains a humidified incubator, an inverted fluorescent Zeiss microscope with a high resolution CCD camera and an integrated computer system. Real time images were generated with a 10x magnification, 0.4 numerical aperture objective using both the Hoechst and GFP filter sets. The Hoechst channel was used to focus and we acquired images every 30 mins for 48 hours. Cells were segmented, tracked and fluorescence levels extracted using custom software. The autofluorescence GFP value of an untransfected cell reached a maximum of 7000 units. To remove background we set a pre-selection threshold value of 8000 fluorescent units in the GFP channel and measured the response profiles for cells which have at least 10 measurement points above this value. We synchronised fluorescence response profiles in silico to the point of cell division as determined by a rise and then post-mitotic drop in Hoechst staining. This enabled us to restrict fluorescent reporter measurements to individual cell generations. We previously calculated that 15 or more cells per experiment were required for robust transcription rate estimates (Woodcock, et al. 2013) and therefore randomly selected 30-35 fluorescent onset curves for each reporter construct.

**Extraction of single cell fluorescence time-course data**

Segmentation based on the nuclear stain (Hoechst) was performed using standard routines built into KineticScan V2.2.0.1 (BUILD 27) software (Thermo Scientific) and data were exported to a Microsoft Access database. For subsequent tracking we extracted cell positions and fluorescence intensities using custom plugins for ImageJ software ([http://rsb.info.nih.gov/ij](http://rsb.info.nih.gov/ij)) employing Jackcess, a java library for reading from and writing to Access databases ([http://jackcess.sourceforge.net/](http://jackcess.sourceforge.net/)). We have developed novel routines for cell tracking written in C based on a statistical scoring algorithm which accounts for dense cell cultures at 10X or 20X resolution and significant movement, ie translocation of more
than a cell diameter between subsequent frames. Confidence scores are computed taking into account distances to neighbouring cells, extent of cell movement, and alternative cell-to-cell assignments. We have been able to automatically define up to two cell divisions in one time-course by using variations in Hoechst staining intensity between cells and a characteristic drop in Hoechst intensity after cell division. The software is described in (Downey, et al. 2011). Single cell trajectories for all M\text{x}1 promoter containing reporters are shown in Supplemental Fig. 1.

**Computational Genomics**

We implemented a computational approach analogous to the one described in (Picot, et al. 2010) to identify conserved regions.

**Hierarchical model of transcriptional dynamics**

The model is described in detail in (Woodcock, et al. 2013). This method incorporates both intrinsic and extrinsic noise into the estimation (Finkenstadt, et al. 2013) and has been used to enable estimation of transcription rates when the plasmid copy number is unknown (Woodcock, et al. 2013). It consists of two layers: the single cell layer and the population layer. The single cell layer takes the form of a pair of stochastic differential equations describing how the mRNA and protein level change in time, and an equation which describes the measurement process. These equations are

\[
\begin{align*}
    dM(t) &= \left( c\tau(t) - \delta_M M(t) \right) dt + \sqrt{c\tau(t) - \delta_M M(t)} \ dW(t), \\
    dP(t) &= \left( \alpha M(t) - \delta_P P(t) \right) dt + \sqrt{\alpha M(t) - \delta_P P(t)} \ dW(t), \\
    F(t) &= \kappa P(t) + \epsilon_{\sigma^2},
\end{align*}
\]

where \( c \) is the copy number, \( \tau(t) \) is the transcription rate at time \( t \), \( \delta_M \) and \( \delta_P \) are the mRNA and protein degradation rates respectively, \( \alpha \) is the translation rate, \( \kappa \) is the measured
fluorescence per protein, and $\sigma^2$ is normally distributed measurement noise, with variance $\sigma^2$. $M(t)$, $P(t)$ and $F(t)$ are respectively the mRNA, protein and fluorescence levels at time $t$ and $dW(t)$ denotes a Weiner process. In this model, $\tau(t)$ can take one of two values depending if the gene is actively transcribing, namely $\tau_0$ when transcription is only occurring at a basal level and $\tau_1$ in the active state. We also need to estimate the time when transcription changes between these states, which we refer to as the switch time, $T$. These equations capture the difficulty in estimating transcription rate when the copy number is unknown, as their respective parameters only appear as a product and so they would not normally be identifiable in a conventional estimation procedure. This is because the estimated values could trade-off against one another, meaning there would be an infinite number of possible combinations of $\tau(t)$ and $c$ that would be equally valid. We specifically address this problem in (Woodcock, et al. 2013) and we employ a similar method for our parameter estimation here.

In conventional parameter estimation methods, each estimate for each cell in the sample would be undertaken separately and the results then amalgamated and analysed as a group. In our estimation scheme, we follow (Finkenstadt, et al. 2013) and make the assumption that each individual rate, and therefore each parameter, comes from a distribution over the population. Collectively, these distributions are referred to as the population layer. These are then estimated concurrently with the parameters for all of the time series simultaneously. To do this, we employ a Markov Chain Monte-Carlo (MCMC) estimation procedure which is highlighted in Figure 2. This involves iteratively updating the parameter and distribution estimates by evaluating their ability to describe the data using a likelihood function derived from the single cell layer above and the probability density functions
comprising the population layer. As such, the parameter estimates feed into the population distribution estimates, which themselves feed into the parameter estimates and so on. This cyclical information transfer allows a parameter estimate to “borrow strength” from the other estimates of the same parameter, leading to a more robust estimation (Finkenstadt, et al. 2013).

It is this principle that we exploit to tease apart the copy number and transcription rate. Crucially, if we assume a distribution over the transcription rate as well as a distribution over the copy number then this constrains the estimates of $c$ and $\tau(t)$ to be similar to those of the rest of the population; the degree of similarity is encapsulated in the population distributions. There are still an infinite number of possible combinations, but because of the population layer we can now assign a probability to these and so as the MCMC procedure iteratively updates the parameter estimates, they will begin to coalesce into their respective distributions. As this continues, the distributions become tighter and so the number of viable combinations diminishes. Eventually the estimates converge on the parameter values which best explain the data, while accounting for the similarity constraints imposed by their respective distributions.

One caveat in this approach is that the transcription rate and copy number values the MCMC method will estimate will be somewhat arbitrary as there is no way of discerning the correct absolute value for either parameter. However, as there is no reason to think that the distribution of plasmid copies entering the cell would be different between the different constructs, we can assume the same copy number distribution for each of the constructs. This means that if we estimate the distributions and parameter estimates for the entire data set at the same time, all of the transcription rates in each of the constructs will be estimated relative to the same copy number distribution. This will still not allow us to estimate the absolute
transcription rate values, but they are estimated proportional to the same copy number distribution and so can be compared to each other.
RESULTS

Msx1 promoter and comparative cis-regulatory module identification

We recently developed and validated a new measurement and mathematical modelling pipeline to estimate copy number independent single cell transcription rates using transiently transfected fluorescent reporter time courses (Downey, et al. 2011; Woodcock, et al. 2013). We now apply this pipeline to analyse the function of individual CRMs and promoters in controlling variability and robustness in Msx1 expression in real time in C2C12 mesenchymal cells. The Msx1 gene has a relatively simple cis-regulatory organization as a 5kb DNA genomic fragment located immediately upstream of mouse Msx1 can fully replicate endogenous Msx1 expression in transgenic mice (MacKenzie, et al. 1997). Using computational genomics, we identified four putative CRMs within this region, similar to the blocks of sequence conservation discovered by (Miller, et al. 2007), that are conserved in position and sequence between mouse and fugu (Fig. 1A). Furthermore, we identified only one copy of Msx1 in teleosts with a complete complement of CRMs homologous to those in mammals despite a separate round of whole genome duplications within actinopterygians (see Supplemental Text). Among these CRMs, mouse CRMB and D have previously been identified as limb bud and branchial arch enhancers (MacKenzie, et al. 1997), while CRMA and C are uncharacterized. The mouse Msx1 minimal promoter has previously been defined in transgenic mice and C2C12 cells in culture (Takahashi, et al. 1997) and we used a custom discovery tool (Granier, et al. 2011; Jeziorska, et al. 2012) (see also Supplemental Text) to identify the orthologous promoter region in fugu on the basis of a conserved transcription factor binding site configuration (Fig. 1B).

Quantitative validation of a reporter assay for studying Msx1 promoter-CRM communication
Msx1 spatiotemporal expression is highly conserved across vertebrates. However, branchial arches develop faster and morphogenetic fields are much smaller in teleosts than in mouse. This similarity and difference provides an attractive biological rationale for a quantitative functional comparison of homologous promoter and CRMs from mouse and fugu Msx1. To do this, we first tested our experimental system using flow cytometry to compare the activity of transfected mouse and fugu promoters with endogenous MSX1 protein levels in mouse C2C12 mesenchymal cells, an established cell line to study Msx1 transcriptional control and its associated regulatory functions (Lee, et al. 2004; Shetty, et al. 1999; Takahashi, et al. 1997; Wang and Abate-Shen 2012; Wang, et al. 2011). This revealed that mouse basal Msx1 promoter activity is higher compared to that of the homologous fugu promoter region (Fig. 1D). We then treated cells with LiCl to activate the wnt signalling pathway, as Msx1 is a known wnt target (Miller, et al. 2007; Willert, et al. 2002), and observed a 1.6-fold mean increase in endogenous MSX1 (Fig. 1E) and a concomitant increase of 1.6-fold for the transfected fugu and 1.8-fold for the mouse promoter constructs (Fig. 1D) in response to LiCl. This is within the expected range of responses to Wnt signalling described previously generically as well as for Msx1 (Goentoro and Kirschner 2009; Willert, et al. 2002) suggesting that transient transfection does not bias the quantitative output significantly in our system. Furthermore, the conservation of quantitative responses among orthologous Msx1 promoters to the same input confirms our selection of the correct fugu Msx1 promoter region.

Estimation of real time single cell transcription rates using live cell imaging and mathematical modelling

To estimate copy number independent transcription rates we transiently transfected C2C12 cells with reporter constructs containing both inter- and same-species CRM and promoter Msx1 components (Fig. 1C) and performed live cell imaging to generate fluorescent onset
curves for approximately 30-35 randomly picked cells for each construct (Supplemental Fig. 1). We used a nuclear localized Venus fluorescent protein reporter in an effort to restrict measurement errors caused by cell size or shape dependent variations. We truncated the trajectories of the time courses when the maximum fluorescence was reached as our previous work showed that reporter signal is diluted and distributed equally into daughter cells after cell division (Downey, et al. 2011). This enabled us to restrict fluorescent measurements to a single cell cycle (Fig. 1F) and minimise inaccuracies in transcription rate estimations caused by nuclear envelope breakdown and segregation of reporter plasmids after division.

We estimated the parameters of our hierarchical model of transcriptional dynamics for single cells across all constructs using our previously described methodology developed in (Woodcock, et al. 2013). This inference scheme allows the estimation of all the rates in a population of cells simultaneously, which enables population information to be used in the single cell inference and vice versa. Cyclical information transfer between the population and single cell levels guides the inference towards combinations of rates which are consistent with the rest of the population, allowing us to distinguish between the contribution of plasmid copy number and transcription rate to overall expression levels in a population of cells containing variable plasmid copy number (Fig. 2A). Although we do not identify absolute values for the per-copy transcription rate we are able to estimate the ratio of the per-copy transcription rate between different constructs and cells. We have shown using synthetic data that the value of the plasmid copy number has no effect on the ability of the algorithm to correctly estimate transcription rates (Woodcock, et al. 2013). The model can explain, for example, divergent fluorescent trajectories between two cells of the same experiment (Fig. 2B, left) as a result of copy number (Fig. 2B, centre) rather than transcription rates (Fig. 2B, right). For this reason, we can analyse the contributions of individual promoters and CRMs
by comparing entire transcription rate distributions across all experiments. Our transient transfection approach therefore complements studies using integrated reporters in stable cell lines where the genomic location of reporter integration is known to affect the timing and size of transcriptional bursts (Becskei, et al. 2005; Raj, et al. 2006; Skupsky, et al. 2010).

**Basal promoters display dynamic intra- and intercellular transcription rate ranges**

Studies in yeast and bacteria have shown that basal promoters are important determinants of the inverse relationship between mean expression and noise (Carey, et al. 2013; Hornung, et al. 2012; Tirosh and Barkai 2008). We therefore analysed the real time activity of the orthologous mouse and fugu Msx1 promoters at single cell resolution to test if this relationship also holds true for metazoans. In order to examine both the rate distributions within a given cell and the population-wide distributions of average single cell transcription rates we displayed the calculated transcription rate distributions for each cell along the y-axis and sorted each individual cell along the x-axis according to ascending average transcription rates for all graphs. This revealed single cell transcription rate distributions with promoter-specific ranges and showed that the corresponding range of switch times derived from the posterior distribution narrows with increased transcription rate (Fig. 3A-C). This suggests that the progression from the basal to the active state occurs more rapidly in those cells with a high transcription rate. The data also showed that the basal mouse Msx1 promoter has a 2.3-fold higher mean single cell transcription rate compared to the orthologous fugu sequence (Table 1). This is consistent with the population average measurements in Figure 1D determined using flow cytometry, further validating our single cell approach.

We assembled all basal promoter construct single cell rates to investigate the relationship between mean transcription rate and noise. This demonstrated that the range of transcription rates inside each single cell (measured as SD) increases in correlation with the...
average rate (Fig. 3D and 3E). However, the average intracellular transcription rate increases faster than the corresponding SD of rates inside each cell resulting in a decrease in the coefficient of variation (CV) per single cell with increasing average rate. Intracellular variation in transcription rates would in our context be understood as 1/CV (the signal-to-noise ratio in control theory) of single cell transcription rate distributions implying that promoters on their own already display an (average-rate dependent) robustness behaviour, consistent with previous analyses examining the relationship between mean rate and noise in yeast and bacteria (Carey, et al. 2013; Hornung, et al. 2012; Tirosh and Barkai 2008). One trivial explanation could be that more transfected templates in a given cell would, when averaged over time across a single cell, lead to an overall higher level of reporter fluorescence and underlying transcription rate. Importantly, we showed that this is not the case here as the estimated template copy numbers of the cells in Fig. 3F (y-axis) do not correlate with increased average transcription rates (Fig. 3D).

Our analysis revealed four different dynamic promoter behaviours within single cells (Fig. 3G). Cells can acquire either a high or a low average rate very quickly (identified by a low SD and narrow spread of switch times), the range of rates can be traversed slowly (with high SD) or there might be more than one transcription rate optimum per cell, hinting at a variety of preferred promoter states.

**Msx1 CRMs modulate single cell promoter transcription rate distributions in a graded manner**

It has been proposed that CRMs use either a rheostatic or binary mode of action to modulate fixed promoter rates (for a review see (Jeziorska, et al. 2009)). However, single time point population measurements are unable to distinguish between these two models. To generate a more detailed understanding of CRM function, we assayed both for the ability of Msx1
CRMs to modulate real time promoter rate distributions in single cells, and also for conservation and divergence of function between mouse and fugu CRMs. As *Msx1* CRMD and CRMB are known to function as classical enhancers both *in vivo* and in C2C12 cells (MacKenzie, et al. 1997; Woodcock, et al. 2013), we compared the transcription rates of CRMD and CRMB containing reporters to the respective promoter-alone constructs within a population of cells. We first noted that fugu and mouse CRMD and CRMB increase mean promoter single cell transcription rates when analysed across a population of cells (Table 1). The transcription rate distributions of CRMD and CRMB (in red) show that both fugu and mouse CRMD (Fig. 4A) and CRMB (Fig. 4B) shift the respective basal promoter rate distributions (in blue) upwards: more cells within a population display a higher average rate. Closer inspection of the transcription rate distributions in Fig. 4A, however, also suggest that mouse CRMD (red) has the capacity to function as either an activator or repressor of the SV40 promoter in single cells depending on basal promoter rates (blue). The population of cells with a lower mean promoter transcription rate is repressed by mouse CRMD, whereas the population with a higher mean transcription rate is activated. This leads to a bimodal rate distribution at single cell resolution, an affect that is not discovered when only population average measurements are used.

We next examined the single cell transcription rate distributions of constructs containing the previously uncharacterised CRMC and CRMA regions. Despite a low sequence conservation (56% between fugu and mouse) CRMC increases the proportion of cells with a higher mean rate, irrespective of species origin of CRMC or promoter (Fig. 5A and Table 1). However, CRMA, which is highly conserved between fugu and mouse (71%), unexpectedly displays an evolutionary divergence of function as fugu CRMA enhances promoter transcription rates while mouse CRMA silences under our identical cellular and
experimental conditions. In fact, adding mouse CRMA to SV40 yields a rate distribution below that of the basal SV40 promoter alone (Fig. 5B), suggesting that sequence evolution within CRMA in the lineage towards mammals has changed its functionality. Surprisingly, the intracellular ranges of rates acquired through adding CRMC and CRMA are consistently narrower than those of the basal promoters, CRMB or CRMD constructs across the entire spectrum of average rates (Fig. 5 vs Fig. 4). This is suggestive of a novel CRM intracellular filter function that reduces intracellular variability in transcription rates (compare red and blue in Fig. 5A and 5B vs Fig. 4A and 4B). The use of the posterior probability as a measure of transcriptional variability is discussed in the Supplemental Text.

**Differential contributions of promoters and CRMs to transcription rate distributions in real time**

In order to perform a statistical analysis on the results as the basis for uncovering general promoter and CRM functional properties we sorted the transcription rate distributions for all 573 single cells by ascending transcription rate means. This demonstrated that while the range of rates increases with the mean rate inside single cells, the mean grows faster, leading to a CV reduction and therefore an increase in the signal-to-noise ratio $\text{SNR}=1/\text{CV}$ (Fig. 6A and 6B). The results also display a significant contraction of the range of switch time values with increasing single cell transcription rate means, suggesting that the more rapid transition at higher transcription rates is a global phenomenon (Fig. 6A). We next colour-coded single cell rate distributions depending on the different promoters used in order to determine the contributions of promoters to the overall transcription rate distribution (Fig. 6C). This showed that the rate distributions are separable and reflect those of the underlying basal promoter-alone constructs (Fig. 6D).
To investigate the regulatory roles of CRMs we plotted the averages of all single cell transcription rates in a log scale as a cumulative distribution function across the population and discovered that a Kolmogorov-Smirnov test finds log-normality for each CRM (purple lines in Fig. 7A). CRMs lead to a shift in the basal promoter population mean or variance in log space (black in Fig. 7A). Enhancer CRMs (such as CRMB, C and D) increase, while silencers (CRMA) decrease the basal promoter population mean rate (black stippled line in Fig. 7A) with each individual CRM modulating the mean with differing strength. CRMB, C and D cause more cells within a population (at \( \phi > 0.5 \)) to acquire a higher average transcription rate (Fig. 7A and B). The continuous nature of such dynamic features would not be visible if only population averages were measured and could be mistaken for ultrasensitive behaviour (Hu et al. 2008). Our results therefore show that Msx1 CRMs function in a graded, non-linear manner to transform basal promoter rate ranges at single cell resolution.

**Identification of conserved CRMs that function to reduce intracellular variability in transcription rates**

Our real time single cell transcription rate estimations allowed us to investigate the role of CRMs in controlling variability and robustness in Msx1 expression. The results showed that the intracellular transcription rate ranges for CRMA and CRMC containing constructs are consistently narrower than those of the basal promoters and CRMB or CRMD containing constructs across the entire range of average rates (Fig. 7C compared to 7B). Despite the fact that CRMA can be either activating (Fig. 5B, fugu CRMA) or silencing (Fig. 5B, mouse CRMA), CRMA’s intracellular transcription rates (blue) are largely contained within (pink) the basal promoter (red) single cell rates and occupy its lower half in the overall cell population. The same is true for CRMC (green), where the overlap (yellow) is confined to the upper bound of the intracellular rate distribution of the basal promoter in 80% of single cell
profiles. This action of cutting out the higher or lower ranges of the intracellular basal promoter rate range represents a novel functionality of CRMs that operates to reduce variability in intracellular transcription rates, irrespective of each cell’s average rate (depicted graphically in Fig. 7D). Furthermore, distribution of standard deviations for single cell transcription rate estimates indicates that variations in intracellular transcription rates are reduced for all CRM containing constructs compared to the promoter-alone (Fig. 7E). This reduction is most pronounced for CRMA and CRMC constructs confirming the capacity of Msx1 CRMs to reduce intracellular variability in transcription rates. The results therefore suggest that Msx1 CRMs can function as important regulators of robustness in the control of gene expression in addition to modulating transcription rates.
DISCUSSION

Random fluctuations in gene expression can be either beneficial or deleterious for a number of fundamental biological processes and can be subject to regulatory control. For example, noise in the expression of key dose dependent genes must be filtered out to ensure robust cellular function (Batada and Hurst 2007; Lehner 2008; Newman, et al. 2006). In this study, we used mathematical modelling to estimate transcription rates for 573 single cell reporter time courses and analysed the function of CRMs and promoters in controlling variability and robustness in *Msx1* expression at single cell resolution.

We assessed the contribution of *Msx1* CRMs to the well described gene expression level-noise relationship. We found that both the fugu and mouse *Msx1* basal promoters and the heterologous SV40 control promoter displayed a wide range of rates. The shapes of these rate distributions were determined by the species origins of the component used (Fig 6C, D). We observed a basal promoter-based robustness control that is dependent upon the average rate: the higher the average rate within a given cell, the lower the CV and the higher the SNR (Fig. 3E). This observation held true for all CRM containing constructs (Fig. 6B) demonstrating that the noise-mean rate relationship is indeed solely promoter-controlled in vertebrates. These results imply that distal CRMs do not affect the noise-mean expression relationship and are consistent with studies in yeast implicating promoter sequence and nucleosome occupancy at the transcriptional start site in expression noise control (Carey, et al. 2013; Hornung, et al. 2012; Tirosh and Barkai 2008). In addition to this, recent work in worms has demonstrated promoter-based robustness control in spatial expression and suggested that promoter sequence and length can qualitatively affect promoter robustness (Barriere, et al. 2011). Our findings expand on this by analyzing the temporal characteristics of promoter function.
We also investigated the mode of CRM action at single cell resolution and found conservation of CRM function despite low overall DNA sequence similarity, an observation congruent with the billboard model of CRM function (Arnosti and Kulkarni, 2005), as well as divergence of function among highly similar sequences. We discovered that both Msx1 enhancer and silencer CRMs transform basal promoter rate distributions in a CRM-specific but non-linear fashion across a population (Fig. 7A). This suggests that Msx1 CRMs act to modulate fluctuating promoter rate distributions, and not a single fixed rate as suggested from single time point measurements, in a graded manner. We also show that cell to cell variability in transcription rate averages across a population is log-normally distributed, while the estimated rates inside a single cell are not, suggesting underlying multiplicative effects acting upon a fundamentally stochastic process within a population in accordance with current thermodynamic models of combinatorial transcription factor binding (Gertz, et al. 2009; Janssens, et al. 2006; Segal, et al. 2008). While intercellular variability of transcription rate averages is dominated by promoter and species-specific features (Figures 6 and 7), different CRMs affect inter- and intracellular rates independently. This leads to mean and variance shifts in the log-scale (for CRMB, C, D) across a population and/or to variance reduction (CRMA, C) in the intracellular transcription rate distributions (Fig. 7B, C, D).

Previous single molecule studies have shown that transcriptional events are discrete and occur in bursts, interspersed by pauses whose length is proportional to the inverse of the transcription rate (Davenport, et al. 2000; Galburt, et al. 2009; Hodges, et al. 2009). Whilst the stability of the fluorescent reporter used in our study limited our ability to detect transcriptional bursts, we speculate that distal CRMs may function as individual operating units to regulate either burst size (the number of mRNA molecules produced per burst) or frequency (the rate at which a promoter changes from an inactive to an active state) as shown.
for promoter proximal transcription factor binding sites (Carey, et al. 2013; Hornung, et al. 2012; Suter, et al. 2011). Indeed, studies in yeast have demonstrated that transcriptional variability can be decoupled from mean expression by differential regulation of either burst frequency or strength (Murphy, et al. 2010; To and Maheshri 2010). Future comparative analyses, using destabilised reporters, are thus needed to understand the molecular causes for these dynamic CRM and promoter functions.

In contrast to promoter-based robustness control that is becoming stronger with higher average transcriptional rates within a population, CRM mediated reduction in intracellular variability covers the entire spectrum of rates within a population (Fig. 7C, D). This indicates that CRMs can function as important regulators of gene expression robustness to ensure that the expression of key developmental transcription factors is precisely controlled. A comparison between fugu and mouse CRMA reveals a change in its function from enhancer to repressor under the same conditions (Fig. 5). Despite this change, the filter function of CRMA remains shared across mouse and fugu (Fig. 7C), suggesting that this is inherited from a common ancestor while other rate modulating activities of the same CRMs have evolved separately. Such evolutionary decoupling of rate modulating CRM activities from transcriptional robustness control could provide a mechanism for individual genes to be expressed faster (or slower) than others without affecting their accuracy. We expect that transcription rate filtering is just one in a large class of dynamic functionalities of vertebrate CRMs that remain to be discovered using quantitative single cell transcription rate measurements.
ACKNOWLEDGEMENTS

We thank Prof Laurence Hurst (Bath) for critical reading of the manuscript and Dr Atsushi Miyawaki (RIKEN Institute) for the pCS2Venus plasmid. DJW was funded by BBSRC SABR (BB/F005938/1) and EPSRC (GR/S29256/01) grants and the EU (BIOSIM Network Contract 005137). KWV, SO and JER were funded by Wellcome Trust Programme Grants (WT 066790/E/02/Z and 066745/Z/01/Z), awarded to GK.
REFERENCES


FIGURE LEGENDS

Fig. 1. Msx1 CRM and promoter identification. (A) Genomic organization of potential CRMs and promoters for mouse, human, chicken and fugu Msx1 based on sequence conservation. The fugu Msx1 orthologue displays a similar configuration to that of other vertebrates. Coloured boxes indicate putative regulatory regions, numbers represent percent sequence similarity to mouse. (B) Experimental and computational pipeline for fugu Msx1 basal promoter identification. A conserved transcription factor promoter binding site configuration is displayed. (C) Single- and hybrid-species Msx1 CRM-promoter reporter constructs. (D) Mouse Msx1 basal promoter has a higher activity than the orthologous fugu region. (E) Endogenous MSX1 and both the mouse and fugu Msx1 promoter reporters (shown in D) respond similarly at the quantitative level to the same exogenous stimulus. After transfection C2C12 cells were grown for 20hrs and then incubated for a further 24hrs with or without 40mM LiCl. Flow cytometry was used to measure endogenous MSX1 protein and reporter fluorescence in 10000 cells. Average Msx1 promoter reporter fluorescence was background corrected, then normalized to the activity of a co-transfected CMV-mCherry reporter construct in each cell. (F) Simultaneous acquisition of fluorescent reporter and Hoechst intensity time course measurements. The SV40 Pro-vGFP reporter construct was transfected into Hoechst labelled C2C12 cells. Images were acquired at 30 min intervals after transfection and fluorescent and Hoechst intensities were extracted. Cell divisions were automatically recognised using the Hoechst channel allowing for reporter onset curves to be restricted to a single cell cycle.

Fig. 2. Estimation of copy number independent transcription rates using a hierarchical model of transcriptional dynamics. (A) We simultaneously estimated probability density functions (pdfs) of the copy number, c, and transcription rate τ1 in arbitrary units (A.U.) for
each single cell time course. M(0) is initial mRNA value, P(0) is the initial protein value, T is the switch time and a and b are the parameters of the hierarchical distributions. (B) The fluorescence profiles of two randomly picked cells of a given experiment differ significantly (left panel). Stippled lines indicate the switch times for each individual cell. This represents the time point where transcription switches from the basal rate to the active rate. While the calculated probability density function (pdf) for copy number differs between these cells (middle), the pdf of transcription rates are very similar (right). The hierarchical estimation procedure is used to confirm the form and robustness of these ‘stack’ plots and shows how likely a given transcription rate (in A.U.) is within single cells across experiments. These pdfs permit an unbiased, copy-number independent transcription rate assessment across all single cells in all experiments. In the ensuing figures, the probability densities of the stack plots showing transcription rate distributions are encoded as colour intensities of heat maps.

**Fig. 3. Basal promoters display intra- and inter-cellular transcription rate ranges.** Transcription rate and switch time pdfs for the fugu Msx1 promoter (A), mouse Msx1 promoter (B) the SV40 promoter (C) and all cells carrying basal promoter constructs (D). Transcription rates, plotted as heat maps at single cell resolution, are shown in blue. Each column represents a single cell, sorted by average intracellular transcription rate on the y-axis (in comparable A.U.s), the colour intensity in the heat map indicates the probability of a particular rate. For each single cell, the switch times are centred around the median switch time to allow comparisons across cells irrespective of the absolute activation time. This display format also applies to Figures 4-7. (E) The width of the intracellular rate spectrum (measured as SD) increases with the average rate, but the coefficient of variation (CV=SD/mean rate of each single cell) decreases. The corresponding line of best fit is shown in red. (F) The estimated DNA template copy numbers (pink) for all cells in D with mean
transcription rates sorted in ascending order illustrates that there is no relationship between transcription rate and copy number seen as a result of our estimation process of these variables. (G) We observe four different classes of promoter transcription rate behaviours within single cell time courses. The top row shows a representative rate distribution arising from each of the four classes and the bottom row shows the corresponding time series.

**Fig. 4. Classical Msx1 enhancers increase the number of cells with a higher mean transcription rate in a graded manner.** Basal promoter transcription rate probabilities are in blue, while those of constructs carrying the CRMD (A) and CRMB (B) are plotted in red. Overlap in pink indicates rates where enhancer action does not differ from the basal promoter alone. Note that even under the action of these classical enhancers transcription rate distributions are wide within single cells and many show more than one optimal set of rates, irrespective of copy number. The entire rate distribution (and not a single rate) is modified by enhancer action.

**Fig. 5. Evolutionary conservation and divergence of Msx1 CRMC and CRMA function.** (A) The previously uncharacterized CRM, CRMC from fugu and mouse, acts as an enhancer upon various promoters. The intracellular rate ranges are narrow compared to the basal promoter. (B) Sequence conservation does not guarantee functional conservation. Fugu CRMA acts as an enhancer of the fugu and mouse promoters while mouse CRMA acts as a silencer of the mouse and SV40 promoters. However despite this evolutionary change in function revealed here, the intracellular SD of transcription rates is very narrow for CRMA and C compared to the basal promoter and CRMB and CRMD containing constructs. Notably, mouse CRMA conveys pure repression upon the SV40 promoter with an extremely narrow intracellular rate distribution.
Fig. 6. Differential contributions of promoters and CRMs to single cell transcription rates. Aligning by average rate and colour coding all 573 single cell profiles according to either the promoters or CRMs used allows us to quantify complex promoter dynamics at single cell resolution. (A) The corresponding range of switch times derived from the posterior distribution narrows with increased transcription rate. (B) Intracellular SD of estimated rates increases with mean rate (upper graph). At the same time the mean rate increases more quickly than the width of the intracellular rate spectra, leading to a decrease of the intracellular CV (lower graph). (C) When colour-coded by promoter type, different transcription rate ranges are observed within a given population. Purple is overlap of red and blue, white is overlap of red, green, blue. Their respective order follows that of the basal promoter rate spectra without CRMs. (D) Promoters set specific transcription rate distributions across a population and within each cell.

Fig. 7. Identification of a novel CRM robustness control function for Msx1 CRMA and CRMC. (A) CRMs affect means and variances of average rates within a population of cells in a non-linear fashion. A cumulative distribution function of single cell rate averages in log space provides a generic description for CRM action at the population scale with single cell resolution. Plotting entire single cell rate distributions reveals dynamic enhancer functionalities of CRMB and CRMD (B) and novel intracellular rate filter functions of CRMA and CRMC (C). In these graphs all single cell data are colour-coded as indicated based on the CRMs they contain. (D) Overview graphic displaying the quantitative properties of promoter behaviour and CRM action. This highlights two different activity states (yellow and pink) of the basal promoter, each regulated by a different CRM. Given that the spread of rates (SD) increases with increased average rates in shorter periods of time this implies acceleration of transcription rate choices as a means to accomplish the described
distributional properties. (E) Distribution of standard deviations for transcription rate estimates indicates repression of transcriptional noise for all CRMs. Gamma distributions were fitted to the standard deviations of the transcription rate MCMC estimates for every cell in each CRM configuration across all promoter types. As all estimations were performed under identical parameterisations, this showed that the uncertainty in the transcription rate estimate for the promoter alone was generally higher across the population, indicating that the time series themselves were more variable due to transcriptional noise.
Figure 1
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Figure 7: Graphs illustrating the relationship between transcription rate and cell number for different constructs. The equations and annotations provide insights into the effects of CRMs on transcriptional noise and activity.
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Table 1: Population level statistics showing mean and standard deviation of single cell mean transcription rates