THz-Frequency Modulation of the Hubbard $U$ in an Organic Mott Insulator


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We use midinfrared pulses with stable carrier-envelope phase offset to drive molecular vibrations in the charge transfer salt ET-F$_2$TCNQ, a prototypical one-dimensional Mott insulator. We find that the Mott gap, which is probed resonantly with 10 fs laser pulses, oscillates with the pump field. This observation reveals that molecular excitations can coherently perturb the electronic on-site interactions (Hubbard $U$) by changing the local orbital wave function. The gap oscillates at twice the frequency of the vibrational mode, indicating that the molecular distortions couple quadratically to the local charge density.

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Nonlinear phononics, the coherent excitation of anharmonically coupled collective lattice modes, can be used to create transient crystal structures with new electronic properties [1]. Examples of such nonlinear phonon control are ultrafast insulator-metal transitions [2], melting of magnetism [3], and light-induced superconductivity [4–6]. Nonlinear phononics has been realized and understood in the limit of cubic anharmonic coupling [7,8], which results in rectification of an excited lattice oscillation and in the net displacement of the atomic positions along a second vibrational mode. Change in the electronic properties results then from the altered bond angles and nearest-neighbor atomic distances [9], which perturb hopping amplitudes and exchange interactions. However, local parameters like Mott correlations, of importance in many complex materials, are not modulated by nonlinear phononics.

In this Letter, we show that the on-site Coulomb integral can be modulated in molecular solids by driving local molecular degrees of freedom to large amplitudes [10,11]. The excitation of local modes at midinfrared frequencies is different from the case of nonlinear phononics in that the molecular orbital and, concomitantly, the on-site charge density are controlled [12,13], with each site maintained in its electronic ground state.

A Mott insulator is a half-filled solid in which electrons are made immobile by their mutual Coulomb repulsion. This physics is often described by the extended Hubbard Hamiltonian

$$\hat{H} = -t \sum_{j,\sigma} \langle \hat{c}_{j\sigma}^\dagger \hat{c}_{j+1\sigma} + \text{H.c.} \rangle + V \sum_j \hat{n}_j \hat{n}_{j+1} + U \sum_j \hat{n}_{j\uparrow} \hat{n}_{j\downarrow},$$

where $U$ and $V$ represent on-site and nearest-neighbor-site Coulomb repulsions, and $t$ denotes the tight-binding hopping amplitude [14,15]. In Eq. (1), $\hat{c}_{j\sigma}^\dagger$ ($\hat{c}_{j\sigma}$) is the creation (annihilation) operator for an electron at site $j$ with spin $\sigma$, while $\hat{n}_j$ is the associated number operator and $\hat{n}_j = \hat{n}_{j\uparrow} + \hat{n}_{j\downarrow}$. The key features of the Hubbard model are well reproduced in some molecular solids and, in one dimension, by the charge transfer salt Bis-(ethylenedithio)-tetraathyfulvalene-difluorotetracyanoquinodimethane (ET-F$_2$TCNQ). The crystal structure of this material is shown in Fig. 1(a). One-dimensional Mott physics is observed along the crystallographic $a$ axis, where a half-filled chain of ET molecules is characterized by small intersite tunneling amplitude ($t \approx 40$ meV) and large Coulomb repulsion ($V \approx 120$ meV and $U \approx 840$ meV). Hence, although the system is fractionally filled, a large correlation gap is found. As shown in Fig. 1(b), the reflectivity spectrum of ET-F$_2$TCNQ exhibits a sharp charge transfer band centered at 5500 cm$^{-1}$ [16]. Note the small electron-lattice interaction in ET-F$_2$TCNQ [17] is insufficient to drive a Peierls distortion, so that Mott physics is retained down to very low temperatures. Moreover, since our experiments are performed at room temperature, far above the 30 K Néel temperature [16] and $U \gg k_B T \gg \tilde{r}^2/U$, no long-range Néel spin order is present.

In this and other charge transfer crystals, one finds collective phonon modes only at very low frequencies, well separated from higher-frequency localized molecular vibrations, which are observed in the midinfrared. Here we consider the physical situation discussed schematically in Fig. 2. A single localized vibration of the ET molecule...
is resonantly driven along the electric field of a midinfrared optical pulse. This vibrational excitation leads to a time-dependent deformation of the valence orbital wave function and variation of local charge densities at twice the frequency of the driving field. This, in turn, modulates the Hamiltonian parameters introduced in Eq. (1). To account for this physics, extra terms are added whose form is justified as follows: First, we assume that the classical vibrational mode coordinate $q_j$ only couples to the local charge density and neglect the coupling to other lattice modes [18]. In general, this gives additional terms of the form $\hat{n}_j f(q_j) + \hat{n}_j g(q_j)$, where $f(q_j)$ and $g(q_j)$ are two functions of the local mode coordinate that are not known a priori. Expanding the functions $f$ and $g$ as a series, we obtain
\begin{equation}
\hat{H}_\text{vib} = \sum_j \hat{n}_j (A_1 q_j + A_2 q_j^2 + \cdots) + \sum_j \hat{n}_j \hat{n}_j (B_1 q_j + B_2 q_j^2 + \cdots). \tag{2}
\end{equation}

Since the molecule is centrosymmetric and the vibrational mode is of odd symmetry, the terms linear in $q_j$ [19,20], which dominate the coupling for all even modes, vanish ($A_1 = B_1 = 0$). As the vibrational mode’s natural frequency is $\Omega_{\text{IR}}$, every molecule is coherently driven by the laser pulse with its coordinate in time $\tau$ described as $q_j(\tau) = q_{\text{IR}}(\tau) = C \sin(\Omega_{\text{IR}} \tau)$, where $C$ is the driving amplitude. This implies that the $A_2$ term $\propto q_{\text{IR}}^2(\tau) \sum_j \hat{n}_j$ couples to the total density, resulting in an irrelevant global phase shift. We are, therefore, left with a quadratic coupling to the on-site interaction of the form $\hat{H}_\text{vib} = B_2 q_{\text{IR}}^2(\tau) \hat{n}_j \hat{n}_j = (C/2) B_2 (1 - \cos(2 \Omega_{\text{IR}} \tau)) \hat{n}_j \hat{n}_j$. Importantly, the coefficient $B_2 < 0$ because the vibration will, in general, cause the valence orbital to spatially expand.

Thus, two effects are expected as long as an odd molecular mode is driven: a time-averaged reduction of the on-site repulsion together with its modulation at $2 \Omega_{\text{IR}}$.

These predictions can be tested only by exciting vibrational oscillations by midinfrared pump pulses with a stable carrier-envelope phase (CEP), in which the temporal offset between the electric field and the intensity envelope is constant and locked over consecutive laser shots. Hence, every laser pulse drives the molecule with identical phase and allows measurements performed with subcycle resolution over many pump pulses. The evolution of these oscillations is then monitored by a delayed probe pulse. The time resolution of this experiment is given by the probe-pulse duration, which should be of the order of one-half of the vibrational period to resolve effects at $\Omega_{\text{IR}}$ and one-quarter to observe oscillations at $2 \Omega_{\text{IR}}$. In the experiments on ET-F$_2$TCNQ discussed here, a 10 $\mu$m vibrational mode with a period of 33 fs is excited, requiring probe pulses of approximately 8 fs duration, tuned to the 700 meV charge transfer resonance. Note that this pulse duration corresponds to less than two optical cycles at the corresponding probe wavelength of 1.7 $\mu$m.

In order to generate the required ultrashort probe pulses, the following system was developed. Midinfrared optical pulses with locked carrier-envelope phase were obtained by difference frequency generation from two near-infrared (NIR) optical parametric amplifiers (OPAs) driven by an amplified Ti:sapphire laser operating at 800 nm wavelength and at 1 kHz repetition rate. The two OPAs were seeded by replicas of a single white-light continuum to preserve their relative phase; difference frequency mixing between the two NIR-amplified sources occurring in a GaSe crystal generated passively CEP-stable 130 fs pulses tunable in the midinfrared region [21]. To compensate for slow thermal drifts, these pulses were actively stabilized in phase [22] and used to drive the infrared-active molecular mode of ET-F$_2$TCNQ at 10 $\mu$m wavelength (30 THz frequency), perpendicular to the a axis [see Fig. 3(a)]. The system was probed by 700 meV pulses derived from a third near-infrared OPA pumped by another portion of the 800 nm Ti:sapphire laser source. The broadband probe pulses, an order of magnitude weaker than the pump pulse, covered the spectral region between 570 and 980 meV and were performed at room temperature.

Figure 3(c) reports the spectrally integrated time-resolved reflectivity changes $\Delta R/R$ in ET-F$_2$TCNQ for a

FIG. 1 (color online). (a) The crystal structure of one-dimensional organic salt ET-F$_2$TCNQ (yellow, ET; blue, F$_2$TCNQ). (b) Static reflectivity of the compound with electric field parallel to crystallographic a axis (along the ET chain).
oscillations of about the same amplitude as the overall reducing their amplitude. In the same figure, we also probe pulse, longer than their 8 fs half-period, thus, oscillations are convolved with the 10 fs duration of the were observed, with an amplitude of 0.7%. Note that these
slow decay is attributed to the direct relaxation of the driven vibrational mode. The slower response is attributed to lattice thermalization. Crucially, fast oscillations at approximately 70 THz were observed, with an amplitude of 0.7%. Note that these oscillations are convolved with the 10 fs duration of the probe pulse, longer than their 8 fs half-period, thus, reducing their amplitude. In the same figure, we also show the response after deconvolution, now exhibiting oscillations of about the same amplitude as the overall reduced reflectivity [gray trace in Fig. 3(c)].

The microscopic origin of these dynamics appears to follow qualitatively the response discussed above for quadratic coupling of the type $\hat{H}_{\text{elec}} = (C/2)B_0^2\sum_i[1 - \cos(2\Omega_0 t)]\hat{n}_{i\uparrow}\hat{n}_{i\downarrow}$. For a 1D system, any change in filling will bring the system into a metallic state [24]. Since no metallic Drude response is observed in the terahertz regime [11], we can rule out a transient deviation from the average band filling as the origin of the experimentally observed oscillations. Further insight was possible by performing a spectrally resolved pump-probe measurement using a gated spectrometer for the detection of the probe. The time-dependent reflectivity spectrum is shown in Fig. 4(a), evidencing a reduction in the total reflectivity (from a peak value of 0.4 to 0.33), a red shift of the reflectivity peak (by $\sim70$ cm$^{-1}$), and oscillations with the same 70 THz frequency detected in the spectrally integrated measurements of Fig. 3(c). The observed reflectivity change in Fig. 4(a) is consistent with the spectrally integrated data in Fig. 3(c) when integrating the spectral changes over the weighted probe spectral content. From this reflectivity spectrum, the optical conductivity was calculated at each time delay by a Kramers-Kronig (KK) consistent variational dielectric function [25]. The results are reported in Fig. 4(b), clearly showing oscillations of the conductivity spectrum.

We next analyze the measured response by fitting these transient conductivity spectra. As discussed in Refs. [26–28], the charge transfer band of ET-F$_2$TCNQ in equilibrium is described by two dominant contributions to the optical conductivity [see Fig. 4(c)]. The rather strong peak at lower frequency is related to holon-doublon (HD) pair excitations, that is, the transfer of charges between pump fluence of 0.9 mJ/cm$^2$ obtained by detecting the energy of the reflected probe pulses with a photodiode using the lock-in technique. The reflectivity was observed to reduce by 4% during the pump pulse, recovering in 45 fs along the trailing edge of the pump pulse and followed by a slower exponential decay of 500 fs. The fast decay is attributed to the direct relaxation of the driven vibrational mode. The slower response is attributed to lattice thermalization. Crucially, fast oscillations at approximately 70 THz were observed, with an amplitude of 0.7%. Note that these oscillations are convolved with the 10 fs duration of the probe pulse, longer than their 8 fs half-period, thus, reducing their amplitude. In the same figure, we also show the response after deconvolution, now exhibiting oscillations of about the same amplitude as the overall reduced reflectivity [gray trace in Fig. 3(c)].
neighboring ET sites. As this holon-doublon exciton is bound by the intersite Coulomb correlation $V$, its energy
is centered at $U - V - 4t^2/V$ [28]. A second weaker
contribution to the conductivity spectrum results from the
excitation of delocalized holon-doublon pairs not bound
by the intersite Coulomb energy $V$ [15], which form a
particle-hole (PH) continuum described by a band of width 8$t$
centered at $U$ [27].

Figure 4(c) reports the fit results of the optical conduc-
tivity in which individually normalized contributions from
bound HD pairs and PH continuum are displayed in intervals of $\frac{1}{4}$ of the time period of the pump electric
field. We find that the peak positions of both HD and PH
oscillate at 70 THz frequency, synchronized with the
molecular mode. We extract $U$ and $V$, fitting the optical
conductivity along the lines described in Ref. [27], as a
function of pump-probe delay time. Assuming that the
hopping amplitude does not oscillate with the driven local
vibrational motion [29], this procedure yields the effective
correlation term $U/t$ and $V/t$. Crucially, the overall
reduction of $U/t$ is superimposed by a response at
frequency $2\Omega_{\text{IR}}$, consistent with a quadratic coupling of
$U$ to the vibrational degree of freedom (see Fig. 5(a)).
$V/t$ also shows a prominent reduction contributing to the
transient changes (Fig. 5(c)) but does not show oscillatory
behavior. Note that as for the spectrally integrated measure-
ments, the spectral shifts [35 cm$^{-1}$ (4 meV) and 93 cm$^{-1}$
(12 meV) wavenumbers for HD and PH features, respec-
tively] and the corresponding estimate of the $U/t$ modu-
lations are strongly underestimated because our probe beam
is longer than the limit of 8 fs. No attempt to deconvolve this
resolution factor was made for the $U/t$ parameter, although
the response is likely to be 1 order of magnitude larger than
estimated here. Note also that the absolute changes induced
by the pump in $U$ and $V$ are of comparable magnitude, 7 and
14 meV, respectively. Finally, we observe that the 70 THz
oscillations are at slightly higher frequency than twice the
excitation frequency (60 THz). This effect is likely related
to the precision of our measurement. However, we cannot
exclude that second-order effects may be taking place,
beyond the considerations discussed in Eq. (2). No attempt
was made to analyze these possible effects, which may
involve, for example, a change in frequency of the vibrations
by fourth-order coupling, potentially squeezing the vibra-
tion [30,31].

Additional theoretical analysis further substantiates the
coherent modulation of the Hubbard $U$ parameter. An
effective model describing electronic excitations above the
insulating ground state in the strong-coupling limit was
used (see the Supplemental Material [32]), allowing for a
numerical computation of the optical conductivity from the
nonequilibrium two-time current-current correlation func-
tion $\chi_{JJ}(\tau, \tau') = \langle 0 | \hat{U}^\dagger(\tau + \tau') \hat{U}(\tau + \tau') \hat{U}(\tau') \hat{U}(\tau) \rangle | 0 \rangle$
[33–35]. In this expression, $\hat{U}(\tau)$ is the time-evolution
operator of the system up to time $\tau$ including time
dependence caused by the driving, and $\hat{J}$ is the current
operator. We assumed that $U$ varies in time as a Gaussian
pulse envelope superimposed with the $q_R^2(\tau)$ oscillation
as $U(\tau) = U \{ 1 - A_U e^{-(\tau - \tau_p)^2/2T_p^2} \} \hat{J} \hat{U}(\tau) \},$ where $\tau_p$
and $T_p$ are the center and width of the pulse taken from the
experiment, and $A_U$ quantifies the overall reduction of $U$
seen from the equilibrium fitting in Fig. 5(a). Only the
parameter $P_0$ giving the amplitude of the oscillations
around the envelope was fitted, giving a profile shown in
Fig. 5(b). We assumed that $V$ varies only with the
envelope [Fig. 5(d)]. The computed $\chi_{JJ}(\tau, \tau')$ was then
transformed into the simulated reflectivity and simulated
conductivity shown in Figs. 5(e) and 5(f) and is seen to give
an excellent reproduction of measured reflectivity and
conductivity shown in Figs. 4(a) and 4(b). In order to rule
out a modulation of the nearest-neighbor interaction, we
repeated these calculations also under the assumption of
an oscillatory $V/t$ ratio. The calculated optical properties

FIG. 5 (color online). (a), (c) Time dependence of effective
Hubbard correlation term $U/t$ and $V/t$, respectively, extracted
from fits. (b) and (d) Assumed $U/t$ and $V/t$ variation, respec-
tively, over time for numerical simulation, similar to one obtained
experimentally. (e) Simulated reflectivity obtained via two-time
current-current correlation function calculations of an effective
strong-coupling model. (f) Corresponding simulated conductivity
from the calculations.
(reported in Fig. 3 of the Supplemental Material [32]) differ significantly from the experimental observations, further supporting the claim that the on-site $U$ modulation is the dominant effect behind the oscillatory behavior.

In summary, the time-dependent reflectivity of the molecular Mott insulator ET-$F_2$TCNQ shows a coherent modulation of the correlation gap following phase-stable vibrational excitation. The nonlinear characteristic of the coupling is evidenced by the response, which occurs at approximately twice the frequency of the driving pulse. Fitting of the time-dependent optical conductivity reveals that the on-site Hubbard $U$ parameter is being directly modulated by the excitation of the local molecular vibration. This is in contrast to what was discussed to date for the excitation of collective phonon modes. Vibrational control may be combined with midinfrared pulse-shaping techniques [36], well established in the visible spectral range [37,38], and open up new avenues to coherently control vibrational excitation of collective phonon modes. Vibrational control may be combined with midinfrared pulse-shaping techniques [36], well established in the visible spectral range [37,38], and open up new avenues to coherently control interactions in a many-body system, a task to date only possible with cold-atom optical lattices via the Feshbach resonance [35].

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[18] This assumption is justified since the strongly coupled local molecular vibrations are well separated (≈400–1600 cm$^{-1}$) from the weakly coupled lattice phonons of the comparably heavy molecular sites (below 200 cm$^{-1}$).
[23] D. Brida, G. Cirmi, C. Manzoni, S. Bonora, P. Villoresi, S. De Silvestri, and G. Cerullo, Sub-two-cycle light pulses...


[29] Note that the bandwidth t = 40 meV corresponds to a hopping time scale of 10 THz and, therefore, cannot follow a fast oscillatory modulation at 70 THz.


