FORMING COMPACT MASSIVE GALAXIES

PIETER G. VAN DOKKUM1, ERICA JUNE NELSON1, MARJIN FRANX2, PASCAL OESCH1, IVELINA MOMCHEVA1, GABRIEL BRAMMER3, NATASCHA M. FORSTER SCHREIBER1, ROSALIND E. SKELTON5, KATHERINE E. WHITAKER6, ARJEN VAN DER WEL7, RACHEL BEZANSON8, MATTIA FUMAGALLI9, GARTH D. ILLINGWORTH10, MARISKA KRIEK9, JOEL LEJA1, AND STIJN WUYTS4

1 Department of Astronomy, Yale University, New Haven, CT 06511, USA
2 Leiden Observatory, Leiden University, 2300-RA Leiden, The Netherlands
3 Space Telescope Science Institute, Baltimore, MD 21218, USA
4 Max-Planck-Institut für Extraterrestrische Physik, Giessenbachstrasse, D-85748 Garching, Germany
5 South African Astronomical Observatory, P.O. Box 9, Observatory, Cape Town 7935, South Africa
6 Astrophysics Science Division, Goddard Space Center, Greenbelt, MD 20771, USA
7 Max Planck Institute for Astronomy (MPIA), Königstuhl 17, D-69117 Heidelberg, Germany
8 Steward Observatory, University of Arizona, 933 North Cherry Avenue, Tucson, AZ 85721, USA
9 Department of Astronomy, University of California, Berkeley, CA 94720, USA
10 UCO/Lick Observatory, University of California, Santa Cruz, CA 95064, USA

Received 2015 June 9; accepted 2015 September 15; published 2015 October 22

ABSTRACT

In this paper we study a key phase in the formation of massive galaxies: the transition of star-forming galaxies into massive (\(M_{\text{stars}} \sim 10^{11}M_\odot\)), compact (\(r_e \sim 1\) kpc) quiescent galaxies, which takes place from \(z \sim 3\) to \(z \sim 1.5\). We use HST grism redshifts and extensive photometry in all five 3D-HST/CANDELS fields, more than doubling the area used previously for such studies, and combine these data with Keck MOSFIRE and NIRSPEC spectroscopy. We first confirm a population of massive, compact, star-forming galaxies exists at \(z \gtrsim 2\), using K-band spectroscopy of 25 of these objects at \(2.0 < z < 2.5\). They have a median [N II]/H\(\alpha\) ratio of 0.6, are highly obscured with SFR(\(\text{tot}\))/SFR(H\(\alpha\)) \(\sim 10\), and have a large range of observed line widths. We infer from the kinematics and spatial distribution of H\(\alpha\) that the galaxies have rotating disks of ionized gas that are a factor of \(\sim 2\) more extended than the stellar distribution. By combining measurements of individual galaxies, we find that the kinematics are consistent with a nearly Keplerian fall-off from \(V_{\text{rot}} \sim 500\) km s\(^{-1}\) at 1 kpc to \(V_{\text{rot}} \sim 250\) km s\(^{-1}\) at 7 kpc, and that the total mass out to this radius is dominated by the dense stellar component. Next, we study the size and mass evolution of the progenitors of compact massive galaxies. Even though individual galaxies may have had complex histories with periods of compaction and mergers, we show that the population of progenitors likely followed a simple inside-out growth track in the size–mass plane of \(\Delta \log r_e \sim 0.3\Delta \log M_{\text{stars}}\). This mode of growth gradually increases the stellar mass within a fixed physical radius, and galaxies quench when they reach a stellar density or velocity dispersion threshold. As shown in other studies, the mode of growth changes after quenching, as dry mergers take the galaxies on a relatively steep track in the size–mass plane.

Key words: galaxies: evolution – galaxies: structure

1. INTRODUCTION

Many studies have shown that massive galaxies with low star formation rates (SFRs) were remarkably compact at \(z \gtrsim 2\) (e.g., Daddi et al. 2005; Trujillo et al. 2006; van Dokkum et al. 2008; Damjanov et al. 2011; Conselice 2014). At fixed stellar mass of \(M_{\text{stars}} \approx 10^{11}M_\odot\), quiescent galaxies are a factor of \(\sim 4\) smaller at \(z = 2\) than at \(z = 0\) (e.g., van der Wel et al. 2014a). As the stellar mass of the galaxies also evolves, the inferred size growth of individual galaxies is even larger (van Dokkum et al. 2010; Patel et al. 2013). It is unlikely that all massive galaxies in the present-day universe had a compact progenitor (Franx et al. 2008; van Dokkum et al. 2008, 2014; Newman et al. 2012; Poggianti et al. 2013; Belli et al. 2014a); however, the vast majority of compact massive galaxies (CMGs) that are observed at \(z = 2\) ended up in the center of a much larger galaxy today (Belli et al. 2014a; van Dokkum et al. 2014). Their size growth after \(z = 2\) is probably dominated by minor mergers: such mergers are expected, and other mechanisms cannot easily produce the observed \(r_e/M_{\text{stars}} \approx 2\) scaling between size growth and mass growth (Bezanson et al. 2009; Naab et al. 2009; Hopkins et al. 2010; Trujillo et al. 2011; Hilz et al. 2013).

It is not yet clear how these massive, extremely compact galaxies were formed, and this question has significance well beyond the somewhat narrow context of the size evolution of quiescent galaxies. The dense centers of massive galaxies today are home to the most massive black holes in the universe (Magorrian et al. 1998); have an enrichment history that is very different from that of the Milky Way (Worthey et al. 1992); and probably had a bottom-heavy stellar initial mass function (IMF) (Conroy & van Dokkum 2012). All these characteristics are the product of processes that took place in the star-forming progenitors of \(z \sim 2\) massive quiescent galaxies. Furthermore, stars in very dense regions represent only a very small fraction (~0.1%) of the stellar mass in the universe today, but their contribution rises sharply with redshift: depending on the IMF, stars inside dense cores with \(M_{\text{stars}} < 1\text{kpc} > 3 \times 10^{10}M_\odot\) may contribute 10%–20% of the stellar mass density at \(z > 2\) (van Dokkum et al. 2014).

The formation of CMGs requires large amounts of gas to be funneled in a region that is only 1–2 kpc in diameter, while preventing significant star formation at larger radii. Galaxy formation models have been able to reproduce the broad characteristics of CMGs, either by mergers that are accompanied by a strong central star burst (e.g., Hopkins et al. 2009b;
Wuyts et al. 2010; Wellons et al. 2015), by in situ formation from highly efficient gas cooling (Naab et al. 2009; Wellons et al. 2015), or by contraction (“compaction”) of star-forming gas disks (Dekel & Burkert 2014; Zolotov et al. 2015). These scenarios have testable predictions: for example, if CMGs formed in mergers then they may be expected to show tidal features. Furthermore, the SFRs of galaxies, and their evolution in the size–mass plane, can be compared to observations.

Observationally, the challenge is to identify these star-forming progenitors of CMGs. Once they are found they can be studied, to measure the physical conditions inside them and to test proposed mechanisms for their formation (see Barro et al. 2013, 2014b; Nelson et al. 2014; Williams et al. 2014, 2015, for examples of such studies). The main observational complication is that typical quiescent galaxies at $z \gtrsim 2$ are structurally very different from typical star-forming galaxies (see, e.g., Franx et al. 2008). At fixed mass, star-forming galaxies are larger, have a lower Sérsic (1968) index and, as a result, a much lower central density (e.g., Franx et al. 2008; Kriek et al. 2009a; van der Wel et al. 2014b; van Dokkum et al. 2014). It may be that a subset of the star-forming galaxies decrease their size through mergers or “compaction,” but it would be difficult to pinpoint which among the many large, star-forming galaxies are destined to go through these phases. A similar problem arises when linking compact, quiescent descendants at $z = 2$ to (lower mass) star-forming galaxies at much higher redshift (Williams et al. 2014, 2015): although there may be progenitors of massive quiescent galaxies among small, blue, low mass star-forming galaxies at $z > 3$, most of those galaxies will likely follow different paths.

Barro et al. (2013, 2014b) and Nelson et al. (2014) use a relatively model-independent and straightforward way to identify plausible progenitors: they select massive star-forming galaxies at $z \gtrsim 2$ with the same small sizes as quiescent galaxies. These objects form the compact tail of the size distribution of star-forming galaxies: for every massive star-forming galaxy at $z = 2–2.5$ that is compact, there are several that are not (see Section 2.3, and van der Wel et al. 2014b).

It seems plausible that star-forming galaxies with the same structure as quiescent galaxies are the direct ancestors of these galaxies, and there may be physical reasons why the most compact star-forming galaxies are the most likely to shut off: many proposed quenching and maintenance mechanisms operate most effectively when a significant bulge (and associated black hole) has formed (Croton et al. 2006; Hopkins et al. 2008; Johansson et al. 2009; Conroy et al. 2015).

In this paper we build on previous studies by identifying a sample of massive, compact, star-forming galaxies at $z = 2–2.5$ in the 3D-HST survey (van Dokkum et al. 2011; Brammer et al. 2012b; Skelton et al. 2014). We study all five 3D-HST/CANDELS fields in a homogeneous way, providing improved measurements of the number density of candidate compact galaxies in formation. We present extensive Keck spectroscopy of a subset of these candidates, and measure redshifts, emission line widths, and emission line ratios. The Hα line profile and spatial extent is used to probe the potential beyond the stellar effective radius, allowing us to reconstruct the average rotation curve of this class of objects. In the second part of the paper we discuss a framework for the formation and evolution of massive galaxies that places the results of the Keck spectroscopy in context. We show that, even though individual galaxies likely have complex formation histories, the evolution of the population of massive galaxies can be described with a simple model in which galaxies follow parallel tracks in the size–mass plane. For consistency with previous studies we assume $\Omega_m = 0.3$, $\Omega_{\Lambda} = 0.7$, and $H_0 = 70 \text{km s}^{-1} \text{Mpc}^{-1}$.

2. COMPACT MASSIVE STAR-FORMING GALAXIES

2.1. Catalogs and Derived Parameters

We use data from the 3D-HST project (van Dokkum et al. 2011; Brammer et al. 2012b) to identify candidate CMGs. The 3D-HST catalogs (Skelton et al. 2014) provide multi-band photometry for objects in the five extra-galactic fields of the CANDELS survey (Grogin et al. 2011; Koekemoer et al. 2011). Objects were selected using a signal-to-noise ratio (S/N) optimized combination of the WFC3 $J_{125}$, $H_{140}$- and $H_{160}$ images. The catalogs encompass nearly all publicly available data in the CANDELS fields, including deep IRAC data, as well as medium-band imaging in the optical and the near-IR. Stars were excluded, as well as objects that have use$_{phot}=0$ (see Skelton et al. 2014).

The imaging data are combined with 3D-HST WFC3 G141 grism spectroscopy, which—together with data from program GO-11600—covers ~80% of the CANDELS photometric area (see Brammer et al. 2012b). The analysis of the combined photometric and spectroscopic dataset will be described in detail in I. Momcheva et al. (2015, in preparation). Briefly, the photometric data from Skelton et al. (2014) and the 2D grism data were fit simultaneously with a modified version of the EAZY code (Brammer et al. 2008) to measure redshifts, rest-frame colors, and the strengths of emission lines (Brammer et al. 2012a). If there are no significant emission or absorption features in the grism spectrum, or if no grism spectrum is available, the fit is similar to a standard photometric redshift analysis. In version 4.1.4 of our data release spectra are extracted only to $H_{160} < 24$ (and obviously only in the area covered by the grism observations).

In addition to the Skelton et al. photometric information and the grism spectroscopy we use Spitzer MIPS 24 µm data to estimate total IR luminosities and SFRs, as described in Whitaker et al. (2012, 2014). These IR luminosities and SFRs are consistent (within a factor of ~2) with those derived from the full mid- and far-IR spectral energy distributions (SEDs), at least for the IR-luminous galaxies that have reliable far-IR photometry (see, e.g., Muzzin et al. 2010; Elbaz et al. 2011; Wuets et al. 2011; Utomo et al. 2014).

Structural parameters of galaxies in the Skelton et al. catalogs were measured by van der Wel et al. (2014b), using the methodology described in van der Wel et al. (2012). Sizes, total luminosities, and ellipticities were measured from the WFC3 imaging using the GALAPAGOS implementation (Barden et al. 2012) of GALFIT (Peng et al. 2002). In Section 7.2 we show with a stacking analysis that the structural parameters in the van der Wel et al. (2014b) catalogs are reliable for the CMGs studied in this paper. The catalog contains a small number of “catastrophic” failures. To identify these, we compared the total galaxy fluxes from the GALFIT fit to the total fluxes in the Skelton et al. catalogs. Galaxies were excluded from the analysis if the absolute difference between these two measurements exceeds 0.5 mag. In this paper we use circularized half-light radii throughout, defined as

$$\log r_e = \log r_{e,a} + 0.5 \log q,$$

(1)
with $r_{e,a}$ as the half-light radius along the major axis and $q \equiv b/a$ as the axis ratio of the galaxy. The sizes are determined from data in the $H_{160}$ band, which corresponds to rest-frame $g$ at $z = 2.3$.

Finally, stellar masses were determined from fits of stellar population synthesis models to the $0.3–8\,\mu m$ photometry, as described in Skelton et al. (2014). The fits were done with the FAST code (Kriek et al. 2009b), using a Chabrier (2003) IMF, the Calzetti et al. (2000) attenuation law, and exponentially declining star formation histories. These parameters were chosen for consistency with previous studies; small changes such as using “delayed $\tau$” models do not change the masses significantly. In this paper we do not use the best-fitting SFRs, ages, or extinction from these fits, as they tend to be less robust than the stellar masses (see, e.g., Kriek et al. 2009b; Muzzin et al. 2009a).

A small (typically $\sim 5\%$) correction was applied to each galaxy to make its half-light radius and stellar mass self-consistent:

$$\log M_{\text{stars}} = \log M_{\text{stars,FAST}} + \log (L_G/L_{\text{tot}}),$$

with $L_G$ the total $H$ band luminosity as implied by the GALFIT fit and $L_{\text{tot}}$ the total $H$ band luminosity in the Skelton et al. catalog (see Taylor et al. 2010a; van Dokkum et al. 2014).

### 2.2. Selection of Star-forming Galaxies

In this paper we use the rest-frame colors of galaxies to separate (candidate) star-forming galaxies from quiescent galaxies. As shown by Labbé et al. (2005), Wuyts et al. (2007), Whitaker et al. (2011), and many others, galaxies occupy distinct regions in the space spanned by the rest-frame $U-V$ and $V-J$ colors, depending on their specific star formation rate (SSFR). The reason is that dust and age have a subtly different effect on the SEDs of galaxies: galaxies that are old and dust-free are red in $U-V$ but (relatively) blue in $V-J$. With high quality redshifts and photometry it has been demonstrated that there is a gap between the (age-) sequence of quiescent galaxies and the (dust-) sequence of star-forming galaxies in the $UVJ$ plane (Brammer et al. 2011; Whitaker et al. 2011), leading to a relatively unambiguous separation of the two galaxy classes.

The distribution of galaxies with $\log M_{\text{stars}} > 10.6$ and $2.0 < z < 2.5$ in the $UVJ$ plane is shown in Figure 1. The quiescent box is indicated with the black lines; galaxies inside this box satisfy the equations

$$V - J < 1.5,$$

$$U - V > 1.3,$$

$$U - V > 0.8(V - J) + 0.7. \quad (3)$$

Galaxies are color-coded by their specific star formation rates, defined as SSFR = SFR/$M_{\text{stars}}$, with SFR as the star formation rate derived from their UV+IR emission (see Whitaker et al. 2014, and references therein). As can be seen in Figure 1 the $UVJ$ selection corresponds very well to a selection on SSFR. This was expected from previous studies (e.g., Wuyts et al. 2011); nevertheless, the correspondence is striking, as the MIPS $24\,\mu m$ measurements (which dominate the SFRs in this stellar mass range) are entirely independent from the $U-V$ and $V-J$ colors.

We note that a subset of quiescent galaxies has high SSFRs in Figure 1; these are galaxies whose rest-frame optical/near-IR SEDs show no signs of star formation even though they have high MIPS $24\,\mu m$ fluxes. These galaxies are difficult to interpret: they may be quiescent galaxies with an active nucleus, or their star formation is so obscured that the young stars do not contribute significantly to the SED. Fumagalli et al. (2014) show that the optical/near-IR SEDs of these galaxies are very similar to the ones that have no MIPS detection. Approximately 20% of galaxies in the Barro et al. (2013) sample fall in this category.

Of 582 galaxies with $\log M_{\text{stars}} > 10.6$ and $2.0 < z < 2.5$, 185 (32%) are quiescent and 397 (68%) are star-forming. The total area of the five fields is 896 arcmin$^2$, and the number densities of massive quiescent galaxies and massive star-forming galaxies are $1.2 \times 10^{-4}$ Mpc$^{-3}$ and $2.7 \times 10^{-4}$ Mpc$^{-3}$ respectively. These numbers are consistent with previous measurements from other datasets (e.g., Marchesini et al. 2009; Brammer et al. 2011; Muzzin et al. 2013).

### 2.3. Selection of Compact Massive Star-forming Galaxies

The size–mass relation for galaxies in the 3D-HST survey with $2.0 < z < 2.5$ is shown in Figure 2. Quiescent and star-forming galaxies, identified using Equation (3), are indicated with red and blue points, respectively. As is well known, star-forming galaxies are larger than quiescent galaxies at fixed mass (e.g., Franx et al. 2008; Williams et al. 2010; van der Wel et al. 2014b). Note that the galaxy distribution in Figure 2 is displaced with respect to that in Figure 5 of van der Wel et al. (2014b), as we note circularized half-light radii and van der Wel et al. use half-light radii along the major axis.

CMGs are in the lower right portion of the size–mass diagram. Barro et al. (2013) use the criterion $\log r_e < (\log M_{\text{stars}} - 10.3)/1.5$ to isolate compact galaxies (dashed line in Figure 2). However, at masses of $\sim 10^{11}M_\odot$ this
Figure 2. Size–mass relation for galaxies with $2.0 < z < 2.5$. Sizes are circularized half-light radii. Red symbols are UVJ-selected quiescent galaxies, blue symbols are star-forming galaxies. The solid lines show our selection criteria for compact, massive galaxies: log $M_{\text{stars}} > 10.6$ and log $r_e < \log M_{\text{stars}} - 10.7$. This criterion is more restrictive than that used by Barro et al. (2013, 2014b) (dashed line); we did not use the Barro et al. criterion as 60% of star-forming galaxies with log $M_{\text{stars}} > 10.8$ fall below the dashed line, and their median size is significantly larger than that of massive quiescent galaxies.

As our goal is to select plausible progenitors of massive, compact quiescent galaxies we adopt a slightly more restrictive criterion:

$$\log r_e < \log M_{\text{stars}} - 10.7,$$

with $M_{\text{stars}}$ in units of $M_\odot$ and $r_e$ in units of kpc. This limit is indicated by the solid diagonal line in Figure 2. Thirty-nine percent of star-forming galaxies with log $M_{\text{stars}} > 10.8$ satisfy this criterion and their median size is $r_e = 1.8$ kpc. As we discuss below, the slope of unity of our compactness criterion can be readily interpreted in terms of a physical parameter, namely the velocity dispersion. The slope of 1/1.5 = 0.67 used by Barro et al. (2013) was chosen to be consistent with the slope of the size–mass relation of quiescent galaxies as found by Newman et al. (2012). We note that van der Wel et al. (2014b) find a slightly steeper slope than Newman et al. (2012) at $z \sim 2.3$ (0.76 ± 0.04 versus 0.69 ± 0.17).

In addition to their compactness criterion Barro et al. apply a mass limit of log $M_{\text{stars}} > 10$. This relatively low limit is also used for their comparison samples of quiescent galaxies and spatially extended star-forming galaxies. However, very few galaxies that have $M_{\text{stars}} \sim 10^{10} M_\odot$ at $z = 2$ will grow into $M_{\text{stars}} \sim 10^{11} M_\odot$ galaxies by $z = 0$ (e.g., van Dokkum et al. 2010; Behroozi et al. 2013; Leja et al. 2013a). We therefore apply a mass limit that is higher by a factor of 4: log $M_{\text{stars}} > 10.6$. This selection produces homogeneous samples of massive compact galaxies. Another consideration when choosing this mass limit is that sizes are uncertain when the effective radius is significantly smaller than the pixel size (the drizzled pixel size is $0''06$, corresponding to 0.5 kpc at $z = 2$).

In the remainder of the paper we will use “CMG,” for “Compact Massive Galaxy,” to denote objects with log $M_{\text{stars}} > 10.6$ and log $r_e < \log M_{\text{stars}} - 10.7$. Based on their location in the UVJ diagram we distinguish “qCMG,” for quiescent CMG, and “sCMG,” for star-forming compact galaxy. There are 112 sCMGs at $2.0 < z < 2.5$ in the five 3D-HST/CANDELS fields. Five of these have effective radii $r_e < 0.5$ kpc; when calculating dynamical masses and expected velocity dispersions of these galaxies we use 0.5 kpc instead of their best-fitting radius. It should be noted that many of the star-forming progenitors of $2 < z < 2.5$ qCMGs are expected to be at higher redshift than $z = 2.5$; we discuss the evolution of sCMGs and qCMGs in Sections 7 and 8.

2.4. Expected Galaxy-integrated Velocity Dispersions and Number Densities

We quantify the compactness of galaxies by their expected galaxy-integrated velocity dispersion, as this quantity follows directly from our size–mass selection and can be compared to observations (see Section 6.1). For simplicity, we use the following relation:

$$\log \sigma_{\text{pred}} = 0.5 (\log M_{\text{stars}} - \log r_e - 5.9),$$

with $\sigma_{\text{pred}}$ as the predicted velocity dispersion in km s$^{-1}$, $M_{\text{stars}}$ in units of $M_\odot$, and $r_e$ in units of kpc (Franx et al. 2008; van Dokkum et al. 2009). This relation has been shown to reasonably predict the observed stellar velocity dispersions of both quiescent galaxies and star-forming galaxies, at least in the regime where this has been tested: out to $z \sim 0.7$ for massive star-forming galaxies (Taylor et al. 2010a; Bezanson et al. 2015) and out to $z \sim 2$ for massive quiescent galaxies (Bezanson et al. 2013; van de Sande et al. 2013; Belli et al. 2014a).

Our compactness criterion (Equation 4) corresponds to log $\sigma_{\text{pred}} > 2.40$, or $\sigma_{\text{pred}} > 250$ km s$^{-1}$. The distributions of predicted dispersions of sCMGs and qCMGs are shown by the histograms in Figure 3. The median expected dispersions of the two populations are similar but not identical: $\sigma_{\text{pred}} = 324$ km s$^{-1}$ for quiescent galaxies and $\sigma_{\text{pred}} = 284$ km s$^{-1}$ for star-forming galaxies. The reason for this difference is that the size distribution of quiescent galaxies is different from that of star-forming galaxies. For star-forming galaxies we select the tail of the distribution, with the largest number of galaxies close to the compactness cutoff, whereas for quiescent galaxies we select the bulk of the population (see van der Wel et al. 2014b, for a discussion of the form of the size distributions of
quiescent and star-forming galaxies). Phrased differently, irrespective of the exact compactness criterion, the smallest galaxies tend to be quiescent. We will return to this in Section 8.1, where we define a “quenching line” just inside the CMG box.

As shown in Taylor et al. (2010a), the residuals between expected and observed dispersions correlate with the Sérsic index. The lines in Figure 3 show the distributions when the Sérsic index of the galaxies is taken into account. sCMGs have a medium predicted dispersion of 284 km s\(^{-1}\).

\[ \log \sigma_{\text{pred}} = 0.5(\log G + \log \beta(n) + \log M_{\text{stars}} - \log r_e), \]

with

\[ \beta(n) = 8.87 - 0.831n + 0.0241n^2 \]

(Cappellari et al. 2006). Here \( n \) is the Sérsic index and \( G = 4.31 \times 10^{-6} \) when \( M_{\text{stars}} \) is in units of \( M_\odot \), \( r_e \) is in kpc, and \( \sigma_{\text{pred}} \) is in km s\(^{-1}\). sCMGs have a slightly smaller median Sérsic index (\( (n) = 2.4 \)) than qCMGs (\( (n) = 2.9 \)). For quiescent galaxies the line and histogram are nearly the same, but for star-forming galaxies the Sérsic-dependent dispersions are on average \( \approx 10\% \) lower than those calculated with Equation (5).

The number density of qCMGs and sCMGs is the same, \( 0.8 \times 10^{-4} \) Mpc\(^{-3}\) (for reference, the number density of the full population of quiescent galaxies with \( \log M_{\text{stars}} > 10.6 \) is \( 1.2 \times 10^{-3} \) Mpc\(^{-3}\); see Section 2.2). This result is consistent with previous studies that noted the overlap of the compact tail of star-forming galaxies and the bulk of the quiescent population (Barro et al. 2013; van der Wel et al. 2014b). We therefore confirm that a population of star-forming galaxies can be identified at \( 2.0 < z < 2.5 \) that has a median mass, median size, and number density similar to the population of massive quiescent galaxies at the same redshifts. If all these compact star-forming galaxies quench in the near future, the number density of massive quiescent galaxies will increase by 70%, and the number density of qCMGs will double.

### 3. NEAR-IR SPECTROSCOPY

We observed candidate sCMGs with the near-IR spectrographs MOSFIRE (McLean et al. 2012) and NIRSPEC (McLean et al. 1998) on Keck in 2014 and 2015. The resulting spectra provide spectroscopic redshifts (measured from H\(\alpha\) and [N \(\text{II}\)] at \( 2.0 < z < 2.7 \)), which can be used to verify that a population of sCMGs exists at these redshifts. Furthermore, the spectroscopic observations provide galaxy-integrated kinematics of the ionized gas: if compact star-forming galaxies are in the process of forming the stars that are later in compact quiescent galaxies, their gas kinematics should be similar to the stellar kinematics of quiescent galaxies. In addition to redshifts and kinematics the spectra provide SFRs and strong line ratios; these are important for understanding the physical processes that take place in these galaxies, although their interpretation is often not unique.

#### 3.1. MOSFIRE

The MOSFIRE spectra were obtained in three separate observing runs: 2014 January 11, 12; 2014 April 18, 23, 25; and 2014 December 12, 13, 15. The January run suffered from clouds and poor seeing; conditions were generally good during the other two runs. Compact, massive star-forming galaxies were not always the main targets, and were not always selected using the criteria of Section 2.2. One target from the April run, a galaxy at \( z = 7.730 \), is described in Oesch et al. (2015). The December run gave higher priority to galaxies at \( 3.0 < z < 3.6 \) than to galaxies at lower redshift. In this paper we will limit the discussion to star-forming galaxies at \( 2 < z < 2.5 \) that satisfy the criteria of Section 2.3.

The observations were all taken in the \( K \)-band, using a standard ABAB dither pattern. The exposure times varied from \( \sim 1 \) to \( \sim 4 \) hr, depending on conditions and the requirements imposed by the primary targets in the masks. One of the slits in each mask was devoted to a relatively bright, relatively blue star. This has four important functions: the \( S/N \) of the star is used to weight individual exposures in the reduction; the \( y \)-position of the star is used to correct the data for small vertical drifts of the mask relative to the sky (see Kriek et al. 2015); the extracted spectrum is used to identify regions of strong sky absorption; and the width of the 2D stellar spectrum in the spatial direction provides us with a model of the point-spread function (PSF) that is otherwise very difficult to construct (see Section 6.2).

The data reduction used the standard MOSFIRE pipeline DRP,\(^{10}\) with small modifications (see Oesch et al. 2015). Individual sequences were reduced and shifted to a common reference frame before stacking. One-dimensional spectra were obtained from the 2D spectra by summing rows, as dictated by the observed spatial extent of the galaxies. For each mask an empirical noise spectrum was created by removing all rows with signal, and determining the width of the pixel distribution of the remaining rows for each pixel in the wavelength

---

\(^{10}\) https://code.google.com/p/mosfire/
direction. The width was measured by removing the lowest and highest 16% of values, and is therefore equivalent to the ±1σ width of a Gaussian. For each individual galaxy in a mask the noise spectrum was multiplied by the square root of the number of rows that was summed to create the 1D spectrum of that object.

3.2. NIRSPEC

The NIRSPEC data were obtained in two runs, 2014 January 10, 13, 14 and 2015 January 25, 26. Conditions were poor in the 2014 run and the only object in our final sample that came from it is GOODS-N_774, which was published in Nelson et al. (2014). Conditions in 2015 were excellent, with the seeing ranging from 0'3–0'76 during both nights. The selection for the NIRSPEC runs was very similar to that described in Section 2.3; within these criteria priority was generally given to galaxies with higher SFRs (and with good blind offset stars; see below).

We followed standard observing procedures for NIRSPEC spectroscopy of faint targets (see, e.g., Erb et al. 2003; van Dokkum et al. 2004). Target acquisition was done with blind offsets from nearby stars, as the galaxies are not detected in the SCAM slit-viewing camera. The N6 filter was used for GOODS-N_774; all data in the 2015 run were taken with the N7 filter. A typical observing sequence consisted of four 900 s exposures in an ABBA pattern with 7'' offsets between nods. The data were continuously inspected as objects sometimes drift out of the slit.

The data reduction followed standard procedures for near-IR, single slit data (see, e.g., van Dokkum et al. 2004). The data were initially reduced in pairs, using the sky of the A frame for the B frame and vice versa. This method yields relatively clean, photon noise-dominated spectra, at the expense of reducing the S/N in the final frames by \( \sqrt{2} \) (see, e.g., Kriek et al. 2015). Wavelength calibration was done using sky lines, which were also used to determine the spectral resolution of the data (see Section 3.4.1). The slit is not long enough to obtain an accurate noise spectrum from empty regions; therefore, we calculate the noise spectrum from the sky spectrum and the noise in the darks. An analysis of the residuals from fits to the emission lines shows that this is sufficient for our purposes (see Section 3.4.1).

3.3. Results and Comparison to Parent Sample

We identify the redshifted H\( \alpha \) and [N ii] emission lines in 20 out of 24 compact, massive star-forming galaxies with expected redshifts in the range 2.0 < \( z \) < 2.5. This success rate of 86% is encouraging,\(^{11}\) but it should be noted that our selection at the telescope was somewhat subjective, particularly in the NIRSPEC runs. As an example, if there were two plausible targets and one showed a hint of an H\( \alpha \) contribution to the broadband flux we would generally give it preference. Additionally, there are five non-overlapping galaxies in Barro et al. (2014b) that satisfy our criteria (see Section 3.5); the total sample of massive compact star-forming galaxies with H\( \alpha \) measurements is therefore 25 (Table 1).

The properties of the galaxies in the spectroscopic sample are compared to the parent sample in Figure 4. The median size and mass are \( r_e = 1.3 \) kpc and \( M_{\text{stars}} = 1.0 \times 10^{11} M_{\odot} \), respectively, close to the medians of the parent sample. The spread is somewhat smaller; 24 out of 25 galaxies are in the mass range 10.7 < \( \log M_{\text{stars}} < 11.3 \). The galaxies have bluer \( U - V \) colors and slightly higher UV+IR SFRs than the parent sample. This is by selection; galaxies with specific star formation rates SSFR < \( 10^{-7} \) yr\(^{-1} \) were given lower priority. Despite the lack of galaxies with low SFRs in the spectroscopic sample, the median SSFR is only 0.1 dex higher than that of the parent sample (log SSFR = −8.8 yr\(^{-1} \) compared to log SSFR = −8.9 yr\(^{-1} \) for the parent sample). Both medians are close to the Whitaker et al. (2014) main sequence for this redshift (dark gray line in Figure 4(c)). Panel (d) of Figure 4 shows the dust content of the galaxies, as parameterized by both the ratio of the IR and UV luminosities and the rest-frame \( V - J \) color. Galaxies in the upper right part of this panel are very dusty, with the re-radiated IR emission exceeding the UV emission by a factor of >100. The median \( L_{\text{IR}}/L_{\text{UV}} \) ratio of the parent sample is \( \langle L_{\text{IR}}/L_{\text{UV}} \rangle = 64 \). The median ratio for the galaxies in the spectroscopic sample is slightly lower, at 42. We only have a few spectroscopic objects in this part of the diagram, and all four spectroscopic failures are located here. We infer that the most likely explanation for the failures is that the H\( \alpha \) emission in these galaxies is too obscured for a detection in our current observations.

The Keck spectra of the 20 galaxies that we observed are shown in Figure 5. The galaxies are ordered by the measured velocity dispersion (see below). We include the five objects from Barro et al. (2014b) that satisfy our selection criteria; as we cannot show the spectra of these objects in Figure 5, we

---

\(^{11}\) Somewhat amazing really, particularly when considering that only a handful of these objects had a previously measured secure redshift from the ground or the grism.

---

Table 1

<table>
<thead>
<tr>
<th>ID*</th>
<th>R.A.</th>
<th>Decl.</th>
<th>( R_{500} )</th>
<th>( H_{100} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>AEGIS_9163</td>
<td>14°21'03.68</td>
<td>53°04'37.3</td>
<td>25.8</td>
<td>23.2</td>
</tr>
<tr>
<td>AEGIS_26952</td>
<td>19°20'09.81</td>
<td>53°04'51.9</td>
<td>25.2</td>
<td>22.2</td>
</tr>
<tr>
<td>AEGIS_41114</td>
<td>16°18'32.92</td>
<td>52°46'06.7</td>
<td>25.1</td>
<td>22.7</td>
</tr>
<tr>
<td>COSMOS_163</td>
<td>10°06'25.01</td>
<td>21°10'44.1</td>
<td>25.9</td>
<td>23.2</td>
</tr>
<tr>
<td>COSMOS_1014</td>
<td>10°00'35.92</td>
<td>21°11'27.8</td>
<td>23.1</td>
<td>21.5</td>
</tr>
<tr>
<td>COSMOS_11363</td>
<td>10°06'28.71</td>
<td>21°17'45.4</td>
<td>24.2</td>
<td>21.3</td>
</tr>
<tr>
<td>COSMOS_12020</td>
<td>10°17'19.1</td>
<td>21°18'07.2</td>
<td>25.8</td>
<td>22.0</td>
</tr>
<tr>
<td>COSMOS_22995</td>
<td>10°00'17.15</td>
<td>22°54'52.3</td>
<td>24.6</td>
<td>22.1</td>
</tr>
<tr>
<td>COSMOS_27289</td>
<td>10°00'41.58</td>
<td>22°37'51.5</td>
<td>22.1</td>
<td></td>
</tr>
<tr>
<td>GOODS-N_774</td>
<td>12°36'27.73</td>
<td>62°07'12.8</td>
<td>27.1</td>
<td>23.0</td>
</tr>
<tr>
<td>GOODS-N_2615*</td>
<td>12°36'06.86</td>
<td>62°10'21.4</td>
<td>25.2</td>
<td>21.5</td>
</tr>
<tr>
<td>GOODS-N_13616*</td>
<td>12°36'06.53</td>
<td>62°12'32.9</td>
<td>25.9</td>
<td>22.8</td>
</tr>
<tr>
<td>GOODS-N_14283*</td>
<td>12°37'02.60</td>
<td>62°12'44.0</td>
<td>25.0</td>
<td>22.9</td>
</tr>
<tr>
<td>GOODS-N_22548*</td>
<td>12°37'00.46</td>
<td>62°15'08.9</td>
<td>25.5</td>
<td>22.5</td>
</tr>
<tr>
<td>GOODS-S_5981</td>
<td>3°32'14.55</td>
<td>−27°52'56.5</td>
<td>24.9</td>
<td>22.4</td>
</tr>
<tr>
<td>GOODS-S_30274</td>
<td>3°32'31.46</td>
<td>−27°46'23.2</td>
<td>23.5</td>
<td>21.3</td>
</tr>
<tr>
<td>GOODS-S_37745</td>
<td>3°32'43.88</td>
<td>−27°44'05.7</td>
<td>24.1</td>
<td>22.0</td>
</tr>
<tr>
<td>GOODS-S_45068*</td>
<td>3°32'33.02</td>
<td>−27°42'00.4</td>
<td>25.0</td>
<td>22.5</td>
</tr>
<tr>
<td>GOODS-S_45188</td>
<td>3°32'15.18</td>
<td>−27°44'58.7</td>
<td>25.4</td>
<td>22.9</td>
</tr>
<tr>
<td>UDS_16442</td>
<td>21°17'20.80</td>
<td>−5°13'16.0</td>
<td>27.4</td>
<td>23.4</td>
</tr>
<tr>
<td>UDS_25893</td>
<td>21°16'02.97</td>
<td>−5°11'21.3</td>
<td>23.1</td>
<td></td>
</tr>
<tr>
<td>UDS_26012</td>
<td>21°17'03.66</td>
<td>−5°11'22.2</td>
<td>25.4</td>
<td>22.4</td>
</tr>
<tr>
<td>UDS_33334</td>
<td>21°16'55.10</td>
<td>−5°09'52.8</td>
<td>26.2</td>
<td>23.3</td>
</tr>
<tr>
<td>UDS_35673</td>
<td>21°17'05.33</td>
<td>−5°09'25.7</td>
<td>25.1</td>
<td>22.4</td>
</tr>
<tr>
<td>UDS_42571</td>
<td>21°17'43.95</td>
<td>−5°07'51.3</td>
<td>27.0</td>
<td>22.8</td>
</tr>
</tbody>
</table>

Notes.

* Id number in Skelton et al. (2014).

* Confirmation from Barro et al. (2014b); R.A., decl., \( R_{500} \) and \( H_{100} \) from Skelton et al. (2014).
instead show models that are based on their published best-fitting parameters.

Figures 6 and 7 show the HST images and the rest-frame UV–near-IR SEDs of the 25 galaxies of Figure 5. The H_{160} images are shown separately at high dynamic range in Appendix A. The SEDs range from relatively unobscured (COSMOS_1014) to extremely dusty (e.g., GOODS-N_774). Some have excess emission in the IRAC bands (UDS_42571; see, e.g., Mentuch et al. 2009). Two galaxies show clear signs of merging: COSMOS_11363 is an ongoing merger between two CMGs that are only 0.6 apart, and GOODS-S_30274 is probably a merger remnant (see Section 7.2). Interestingly, there is no clear relation between the measured velocity dispersion and either the morphology or the SED. Phrased differently, it is not possible to predict the Hα line width based on the information shown in Figures 6 and 7.

3.4. Redshifts, Fluxes, Line Widths, and Line Ratios

3.4.1. Fitting

The spectra were fitted with a model that has the redshift, the continuum level, the [N ii] and Hα line fluxes, and the line width as free parameters. The instrumental resolution is explicitly taken into account. The model has the following form:

$$ M(\lambda) = L(\lambda) \ast R(\lambda) + C, $$

with $L(\lambda)$ as the model for the line emission, $R(\lambda)$ as the instrumental resolution, $C$ as the continuum level, and $\ast$ denoting convolution. The instrumental resolution is modeled with a Gaussian:

$$ R(\lambda) = \frac{\Delta \lambda}{\sqrt{2 \pi} \sigma_{\text{instr}}} \exp \left( -0.5 \left( \frac{\lambda - \lambda_{\text{cen}}}{\sigma_{\text{instr}}} \right)^2 \right), $$

Figure 4. Comparison of objects with near-IR spectra to the parent population of compact, massive star-forming galaxies at 2.0 < z < 2.5. Panels show the size–mass relation (a), the UVJ diagram (b), the star formation–mass relation (with the Whitaker et al. 2014 “main sequence” indicated) (c), and the relation between $L_{IR}/L_{UV}$ to the rest-frame $V-J$ color (d). Solid blue symbols are objects in the sample described here. Open symbols are galaxies from Barro et al. (2014b) that fall in our selection box. Gray points are observed galaxies whose spectrum did not show any clear features.
with \( \sigma_{\text{inst}} \) measured from sky lines in the vicinity of the redshifted H\( \alpha \) line, \( \Delta \lambda \) as the pixel size in \( \text{Å} \), and \( \lambda_{\text{cen}} \) as the center of the fitting range. Expressed as a velocity, the resolution of the MOSFIRE spectra is \( \approx 35 \text{ km s}^{-1} \), and the resolution of the NIRSPEC data is \( \approx 80 \text{ km s}^{-1} \). The lines are parameterized as follows:

\[
L(\lambda) = f_{\text{H}\alpha} L_{6563}(\lambda) + f_{\text{[N II]}} L_{6584}(\lambda) + \frac{1}{3} L_{6584}(\lambda),
\]

with

\[
L_{\lambda_0}(\lambda) = \frac{\Delta \lambda}{\sqrt{2\pi} \sigma} \exp\left(-0.5 \left(\frac{\lambda - (1+z)\lambda_0}{\sigma}\right)^2\right). \tag{11}
\]

Here \( f \) is the line strength, \( \sigma \) is the galaxy-integrated line of sight velocity dispersion, \( \lambda_0 \) is the rest-frame wavelength of the line (with \( \lambda_0 = 6562.8 \) and \( \lambda_0 = 6548.1, 6583.6 \) for H\( \alpha \) and the two [N II] lines, respectively), and \( z \) is the redshift.
Some galaxies show evidence for multiple velocity components (e.g., COSMOS_1014). We do not attempt to separately fit broad and narrow velocity components to these galaxies (as was done by, e.g., Förster Schreiber et al. 2014). As discussed later, broad components could indicate the presence of winds but could also indicate rapidly rotating gas at small radii in the galaxies. In the absence of high spatial resolution data, it is difficult to distinguish these possibilities; we therefore simply interpret the Hα-luminosity-weighted velocity profiles in this paper. It should be noted that the formal uncertainties underestimate the error in the velocity dispersion if the velocity distribution is not Gaussian. This is particularly important for galaxies with a high S/N, such as COSMOS_12020.

The emcee MCMC algorithm (Foreman-Mackey et al. 2013) was used to fit this model to the galaxy spectra. The fit was done over the wavelength region \((1+z)\lambda_{6584} - 200 < \lambda < (1+z)\lambda_{6584} + 200\); the results are not dependent on the choice of fitting region as long as the continuum is reasonably well covered. Priors are top hats with boundaries...
that comfortably encompass the fitting results. That is, the Bayesian aspects of *emcee* were essentially turned off. We used 100 walkers and generated 500 chains in each fit. Burn-in was typically fast, but we removed the first 200 chains when calculating errors. For each fit parameter the best fit is defined as the median of the 300 remaining samples. Errors were determined from the 16th and 84th percentiles (see Foreman-Mackey et al. 2013, for details). The best fit models are shown by red lines in Figure 5. Residuals from the fits are shown in Figure 30. As discussed in Appendix B the residuals are consistent with the expected noise in almost all cases.

### 3.4.2. Calibration

The redshifts and velocity dispersions follow directly from the MCMC fit, but the line fluxes, equivalent widths, and line ratios need to be calibrated or corrected. The continuum is detected for every galaxy, which makes it possible to calculate equivalent widths directly from the spectra. The equivalent widths, in turn, enable us to calibrate the line fluxes using the

![Figure 7. Restframe UV to near-IR spectral energy distributions of the galaxies of Figure 5. The red spectra are the best-fitting EAZY (Brammer et al. 2008) models; open red circles show the model fluxes in the observed filters. The SEDs show a large variety, ranging from blue, relatively unobscured emission (COSMOS_1014) to very red SEDs with high inferred dust content (e.g., UDS_42571 and GOODS-N_774). As in Figure 6, there is no obvious relation between the SEDs of the galaxies and the measured velocity dispersions of their ionized gas.](image)
## Table 2
Properties of Star-forming Compact Massive Galaxies

<table>
<thead>
<tr>
<th>ID</th>
<th>z</th>
<th>$M_{\text{stars}}$ ($10^{11} M_\odot$)</th>
<th>$r_e$ (kpc)</th>
<th>$q$</th>
<th>SFR$^a$ ($M_\odot$ yr$^{-1}$)</th>
<th>log $\text{SFR} / \text{UV}$</th>
<th>X-ray</th>
<th>Instr</th>
<th>$F_{\text{H}}$ (10$^{-17}$ erg s$^{-1}$ cm$^{-2}$)</th>
<th>EW H$\alpha$ (Å)</th>
<th>$\sigma$ (km s$^{-1}$)</th>
<th>$[\text{N} \text{ i}/H\alpha]$</th>
</tr>
</thead>
<tbody>
<tr>
<td>AEGIS_9163</td>
<td>2.445</td>
<td>0.8</td>
<td>0.9</td>
<td>5.4</td>
<td>0.72</td>
<td>131</td>
<td>1.81</td>
<td>...</td>
<td>NIRS</td>
<td>6.6$^{+1.3}_{-1.3}$</td>
<td>74$^{+12}_{-12}$</td>
<td>92$^{+18}_{-18}$</td>
</tr>
<tr>
<td>AEGIS_26952</td>
<td>2.097</td>
<td>1.1</td>
<td>1.8</td>
<td>3.6</td>
<td>0.64</td>
<td>148</td>
<td>1.62</td>
<td>...</td>
<td>yes NIRS</td>
<td>18.4$^{+3.2}_{-3.2}$</td>
<td>95$^{+13}_{-13}$</td>
<td>446$^{+28}_{-28}$</td>
</tr>
<tr>
<td>AEGIS_41114</td>
<td>2.332</td>
<td>0.5</td>
<td>0.2</td>
<td>8.0</td>
<td>0.62</td>
<td>95</td>
<td>1.38</td>
<td>...</td>
<td>NIRS</td>
<td>3.2$^{+0.7}_{-0.7}$</td>
<td>30$^{+6}_{-6}$</td>
<td>176$^{+6}_{-6}$</td>
</tr>
<tr>
<td>COSMOS_163</td>
<td>2.312</td>
<td>0.8</td>
<td>1.1</td>
<td>2.5</td>
<td>0.60</td>
<td>336</td>
<td>2.25</td>
<td>...</td>
<td>yes MOSF</td>
<td>7.4$^{+2.3}_{-2.1}$</td>
<td>95$^{+27}_{-26}$</td>
<td>249$^{+45}_{-34}$</td>
</tr>
<tr>
<td>COSMOS_1014</td>
<td>2.100</td>
<td>0.5</td>
<td>0.7</td>
<td>8.0</td>
<td>0.79</td>
<td>150</td>
<td>0.93</td>
<td>...</td>
<td>NIRS</td>
<td>18.5$^{+2.3}_{-2.3}$</td>
<td>70$^{+6}_{-6}$</td>
<td>172$^{+13}_{-13}$</td>
</tr>
<tr>
<td>COSMOS_11363</td>
<td>2.096</td>
<td>1.1</td>
<td>2.1</td>
<td>5.2</td>
<td>0.76</td>
<td>169</td>
<td>1.31</td>
<td>...</td>
<td>yes MOSF</td>
<td>23.3$^{+4.4}_{-4.4}$</td>
<td>65$^{+3}_{-3}$</td>
<td>368$^{+12}_{-12}$</td>
</tr>
<tr>
<td>COSMOS_12020</td>
<td>2.094</td>
<td>2.0</td>
<td>2.1</td>
<td>5.7</td>
<td>0.57</td>
<td>185</td>
<td>1.96</td>
<td>...</td>
<td>yes MOSF</td>
<td>8.3$^{+1.4}_{-1.4}$</td>
<td>34$^{+5}_{-5}$</td>
<td>719$^{+14}_{-14}$</td>
</tr>
<tr>
<td>COSMOS_22995</td>
<td>2.469</td>
<td>1.2</td>
<td>1.1</td>
<td>2.8</td>
<td>0.67</td>
<td>188</td>
<td>1.41</td>
<td>...</td>
<td>yes MOSF</td>
<td>5.1$^{+0.7}_{-0.7}$</td>
<td>23$^{+2}_{-2}$</td>
<td>176$^{+18}_{-18}$</td>
</tr>
<tr>
<td>COSMOS_27289</td>
<td>2.234</td>
<td>1.3</td>
<td>2.3</td>
<td>3.3</td>
<td>0.81</td>
<td>398</td>
<td>2.02</td>
<td>...</td>
<td>NIRS</td>
<td>25.5$^{+10}_{-10}$</td>
<td>106$^{+13}_{-13}$</td>
<td>54$^{+11}_{-11}$</td>
</tr>
<tr>
<td>GOODS-N_774</td>
<td>2.301</td>
<td>1.0</td>
<td>1.0</td>
<td>2.9</td>
<td>0.59</td>
<td>150</td>
<td>2.07</td>
<td>...</td>
<td>NIRS</td>
<td>5.7$^{+0.8}_{-0.8}$</td>
<td>45$^{+4}_{-4}$</td>
<td>352$^{+36}_{-36}$</td>
</tr>
<tr>
<td>GOODS-N_6215</td>
<td>2.321</td>
<td>1.8</td>
<td>1.8</td>
<td>2.6</td>
<td>0.72</td>
<td>110</td>
<td>1.28</td>
<td>...</td>
<td>yes MOSF$^b$</td>
<td>...</td>
<td>...</td>
<td>406$^{+69}_{-69}$</td>
</tr>
<tr>
<td>GOODS-N_13616</td>
<td>2.487</td>
<td>1.1</td>
<td>1.9</td>
<td>5.6</td>
<td>0.97</td>
<td>130</td>
<td>1.79</td>
<td>...</td>
<td>MOSF$^b$</td>
<td>...</td>
<td>...</td>
<td>243$^{+30}_{-30}$</td>
</tr>
<tr>
<td>GOODS-N_14283</td>
<td>2.420</td>
<td>0.9</td>
<td>1.2</td>
<td>2.7</td>
<td>0.86</td>
<td>111</td>
<td>1.43</td>
<td>...</td>
<td>MOSF$^b$</td>
<td>...</td>
<td>...</td>
<td>156$^{+22}_{-22}$</td>
</tr>
<tr>
<td>GOODS-N_22548</td>
<td>2.330</td>
<td>1.0</td>
<td>1.7</td>
<td>5.9</td>
<td>0.78</td>
<td>120</td>
<td>1.53</td>
<td>...</td>
<td>MOSF$^b$</td>
<td>...</td>
<td>...</td>
<td>223$^{+26}_{-26}$</td>
</tr>
<tr>
<td>GOODS-S_5981</td>
<td>2.253</td>
<td>0.8</td>
<td>0.8</td>
<td>4.4</td>
<td>0.85</td>
<td>206</td>
<td>1.75</td>
<td>...</td>
<td>MOSF</td>
<td>8.0$^{+1.9}_{-1.9}$</td>
<td>54$^{+11}_{-11}$</td>
<td>110$^{+18}_{-18}$</td>
</tr>
<tr>
<td>GOODS-S_30274</td>
<td>2.226</td>
<td>1.4</td>
<td>2.5</td>
<td>8.0</td>
<td>0.46</td>
<td>404</td>
<td>1.47</td>
<td>...</td>
<td>MOSF</td>
<td>...</td>
<td>...</td>
<td>296$^{+19}_{-19}$</td>
</tr>
<tr>
<td>GOODS-S_37745</td>
<td>2.432</td>
<td>0.9</td>
<td>0.6</td>
<td>3.6</td>
<td>0.94</td>
<td>118</td>
<td>1.04</td>
<td>...</td>
<td>MOSF</td>
<td>11.7$^{+3.0}_{-3.0}$</td>
<td>59$^{+3}_{-3}$</td>
<td>165$^{+21}_{-21}$</td>
</tr>
<tr>
<td>GOODS-S_45068</td>
<td>2.453</td>
<td>1.1</td>
<td>1.3</td>
<td>4.9</td>
<td>0.97</td>
<td>139</td>
<td>1.57</td>
<td>...</td>
<td>MOSF$^b$</td>
<td>...</td>
<td>...</td>
<td>260$^{+14}_{-14}$</td>
</tr>
<tr>
<td>GOODS-S_45188</td>
<td>2.407</td>
<td>0.7</td>
<td>1.4</td>
<td>4.3</td>
<td>0.90</td>
<td>134</td>
<td>1.66</td>
<td>...</td>
<td>yes NIRS</td>
<td>8.0$^{+1.5}_{-1.6}$</td>
<td>72$^{+12}_{-12}$</td>
<td>49$^{+17}_{-17}$</td>
</tr>
<tr>
<td>UDS_16442</td>
<td>2.218</td>
<td>1.7</td>
<td>3.3</td>
<td>1.6</td>
<td>0.52</td>
<td>176</td>
<td>2.36</td>
<td>...</td>
<td>MOSF</td>
<td>15.9$^{+2.2}_{-2.2}$</td>
<td>145$^{+14}_{-14}$</td>
<td>210$^{+6}_{-6}$</td>
</tr>
<tr>
<td>UDS_25893</td>
<td>2.304</td>
<td>0.6</td>
<td>0.2</td>
<td>8.0</td>
<td>0.92</td>
<td>73</td>
<td>1.88</td>
<td>yes</td>
<td>MOSF</td>
<td>4.5$^{+4.3}_{-4.1}$</td>
<td>54$^{+36}_{-34}$</td>
<td>213$^{+29}_{-29}$</td>
</tr>
<tr>
<td>UDS_26012</td>
<td>2.321</td>
<td>1.3</td>
<td>2.6</td>
<td>3.5</td>
<td>0.73</td>
<td>109</td>
<td>1.47</td>
<td>...</td>
<td>MOSF</td>
<td>11.3$^{+1.4}_{-1.4}$</td>
<td>65$^{+5}_{-5}$</td>
<td>209$^{+4}_{-4}$</td>
</tr>
<tr>
<td>UDS_33334</td>
<td>2.290</td>
<td>0.7</td>
<td>1.4</td>
<td>2.4</td>
<td>0.56</td>
<td>13</td>
<td>1.01</td>
<td>...</td>
<td>MOSF</td>
<td>6.6$^{+4.4}_{-4.4}$</td>
<td>74$^{+3}_{-3}$</td>
<td>161$^{+16}_{-16}$</td>
</tr>
<tr>
<td>UDS_35673</td>
<td>2.182</td>
<td>0.9</td>
<td>0.7</td>
<td>6.4</td>
<td>0.75</td>
<td>492</td>
<td>2.18</td>
<td>...</td>
<td>MOSF</td>
<td>24.7$^{+7.7}_{-7.6}$</td>
<td>136$^{+5}_{-5}$</td>
<td>267$^{+6}_{-6}$</td>
</tr>
<tr>
<td>UDS_42571</td>
<td>2.292</td>
<td>1.6</td>
<td>2.3</td>
<td>1.9</td>
<td>0.82</td>
<td>388</td>
<td>2.39</td>
<td>yes</td>
<td>NIRS</td>
<td>7.1$^{+1.1}_{-1.1}$</td>
<td>46$^{+6}_{-6}$</td>
<td>198$^{+25}_{-25}$</td>
</tr>
</tbody>
</table>

Notes.

$^a$ Uncertainties do not include possible effects of non-Gaussian velocity distributions.

$^b$ Id number in Skelton et al. (2014).

$^c$ Star formation rate from UV+IR emission.

$^d$ Velocity dispersion and $[\text{N} \text{ i}/H\alpha]$ from Barro et al. (2014b).
known K-band magnitudes of the galaxies. The equivalent width of H\(\alpha\) in the observed frame is given by

\[
EW_{H\alpha} = \Delta \lambda \frac{f_{H\alpha}}{C} + EW_{H\alpha,\text{abs}}(1 + z).
\]  

(12)

The second term is a correction for the underlying stellar continuum absorption, which has a non-negligible effect on the measured equivalent widths and line ratios in our sample. We adopt \(EW_{H\alpha,\text{abs}} = 3\) Å (Moustakas & Kennicutt 2006; Alonso-Herrero et al. 2010). The relation between rest-frame equivalent width and the observed equivalent width is \(EW^0_{H\alpha} = EW_{H\alpha}/(1 + z)\). The mean rest-frame equivalent width in our sample is \(\langle EW^0_{H\alpha} \rangle = 71\) Å, consistent with the general population of (detected) massive star-forming galaxies at these redshifts (Fumagalli et al. 2012). The \([N\,\text{II}]/H\alpha\) ratio, corrected for absorption, is

\[
\frac{[N\,\text{II}]}{H\alpha} = \frac{f_{[N\,\text{II}]}^{H\alpha}}{f_{H\alpha}^{H\alpha}} \times \frac{EW^0_{H\alpha} - EW^0_{H\alpha,\text{abs}}}{EW^0_{H\alpha}},
\]  

(13)

with \(f\) taken from the MCMC fit. Note that we use positive values for both absorption equivalent widths and emission equivalent widths in these expressions, as “absorption” here is more accurately described as “emission that is filling in the underlying absorption line.”

The line flux is calculated from the observed equivalent width and the \(K\) magnitude using

\[
F_{H\alpha} = 1.02 \times 10^{-15} \times \frac{EW_{H\alpha}}{2730} \times 10^{(K - 22)/2.5},
\]  

(14)

with \(K\) as the AB magnitude of the object and \(F\) in units of erg s\(^{-1}\) cm\(^{-2}\). This expression ignores small differences between the filters used in each field as well as the detailed shape of the continuum within the \(K\) filter. We verified that the transmission at the observed wavelengths of the lines is within \(\sim 5\%\) of the central transmission of the filter in all cases. Finally, the line luminosity is calculated using

\[
L_{H\alpha} = 1.20 \times 10^{50} \times D^2 F_{H\alpha},
\]  

(15)

with \(D\) as the luminosity distance in Mpc and \(L\) in erg s\(^{-1}\). The results for all galaxies are listed in Table 2. The error bars reflect the (propagated) MCMC errors; no additional calibration uncertainty was included in the error budget.

3.5. Comparison to Barro et al.

There are seven galaxies in the Barro et al. (2014b) sample that satisfy our more restrictive selection criteria. Two of these seven galaxies, COSMOS_12020 and GOODS-S_37745, are also in our sample: COSMOS_12020 was observed with NIRSPEC and GOODS-S_37745 with MOSFIRE. For COSMOS_12020 we find \(\sigma = 719^{+30}_{-14}\) km s\(^{-1}\) and \([N\,\text{II}]/H\alpha = 1.39 \pm 0.23\), whereas Barro et al. have \(\sigma = 352 \pm 213\) km s\(^{-1}\) and \([N\,\text{II}]/H\alpha = 0.25 \pm 0.25\). The kinematics of this galaxy are very complex, and a Gaussian is a poor fit (see Figure 5, and Section 9.2); this probably explains the differences between the two measurements and the large uncertainty in the Barro et al. values. As noted in Section 3.4.1 the formal uncertainty in our measurement of this galaxy is smaller than the true uncertainty, as it does not take deviations from a Gaussian into account. Given that a Gaussian is clearly a poor fit, the velocity dispersion of this galaxy is not well determined. For GOODS-S_37745 we find \(\sigma = 163^{+27}_{-31}\) km s\(^{-1}\) and \([N\,\text{II}]/H\alpha = 0.65 \pm 0.23\), compared to \(\sigma = 197 \pm 37\) km s\(^{-1}\) and \([N\,\text{II}]/H\alpha = 0.77 \pm 0.30\) in Barro et al. (2014b). These values are in agreement within the (relatively large) 1σ uncertainties.

For the two galaxies that overlap we use our own measurements. The other five galaxies from Barro et al. are added to our sample (see Tables 1 and 2). We do not have measurements of the line flux or spatial extent of the emission line gas for these objects, but they are included in the analysis whenever only the redshift, velocity dispersion, or line ratio are needed. They are shown in Figure 5 by their best-fitting models. The total number of sCMGs at \(2.0 < z < 2.5\) that are studied in this paper is 25.

4. INTERPRETATION OF THE LINE RATIOS AND LUMINOSITIES

4.1. Line Ratios

Considering that the 25 sCMGs of Figure 5 were selected in a very restricted region of parameter space, their emission lines show a surprisingly large range of properties. The velocity dispersions range from \(50\) to \(>500\) km s\(^{-1}\), the \([N\,\text{II}]/H\alpha\) ratios from \(0.2\) to \(>2\), and the \(H\alpha\) line luminosities from \(1.3 \times 10^{42} L_{\odot}\) to \(1.2 \times 10^{43} L_{\odot}\). Two of these parameters, the \([N\,\text{II}]/H\alpha\) ratio and the velocity dispersion, show a significant correlation: as shown in Figure 8, galaxies with the highest velocity dispersions tend to have the highest line ratios. The correlation has a formal significance of \(>99\%\). The broken line
is the best fit relation, which has the form
\[
\log \left( \frac{[N \text{ II}]}{H\alpha} \right) = (-0.51 \pm 0.08) + (1.0 \pm 0.2) \log \left( \frac{\sigma_{\text{gas}}}{100} \right).
\]

The canonical high-metallicity saturation value for \([N \text{ II}]/H\alpha\) in low redshift star-forming galaxies is \(\sim 0.4\) (e.g., Baldwin et al. 1981; Denicoló et al. 2002; Pettini & Pagel 2004; Kewley et al. 2013). Although this limit is observed to be higher at \(z > 2\) (e.g., Brinchmann et al. 2008; Steidel et al. 2014; Shapley et al. 2015), values of \([N \text{ II}]/H\alpha > 1\) are extreme at any redshift (see, e.g., Leja et al. 2013b; Shapley et al. 2015). A likely explanation for the highest \(\sigma\), highest \([N \text{ II}]/H\alpha\) galaxies in Figure 8 is that shocks (Dopita & Sutherland 1995) and/or emission from active galactic nuclei (AGNs) (Kewley et al. 2013) are responsible for the line ratios.

This is supported by the X-ray luminosities of the objects, obtained from all public catalogs in the CANDELS fields.12 Twelve of the 25 sCMGs (48%) have \(L_X > 10^{43}\) erg s\(^{-1}\) and are classified as AGNs. The X-ray luminosities range from \(L_X = 1.4 \times 10^{43}\) erg s\(^{-1}\) for GOODS-S S_30274 to \(L_X = 6 \times 10^{44}\) erg s\(^{-1}\) for COSMOS-11363. This high AGN fraction is consistent with previous studies of massive star-forming galaxies at these redshifts (e.g., Papovich et al. 2006; Daddi et al. 2007; Kriek et al. 2007; Barro et al. 2013; Förster Schreiber et al. 2014). The four galaxies with the highest velocity dispersions are all classified as X-ray AGNs.13 Their kinematics are complex (see Figure 5), and their \([N \text{ II}]/H\alpha\) ratios range from 0.8 to 2.2. It is likely that the observed emission line properties of these galaxies are affected by the presence of the AGN, either directly through emission from the broad line region or indirectly through AGN-driven winds (see Förster Schreiber et al. 2014; Genzel et al. 2014b).

However, it is not clear whether AGNs or winds dominate the observed, galaxy-integrated kinematics, even for these four objects—and whether the presence of a central point source influenced their selection as apparently compact, apparently massive galaxies. As shown in Figure 7 the UV–near-IR SEDs of all galaxies are well fit by stars-only models. Most galaxies have strong Balmer breaks (including the most powerful X-ray source in the sample, COSMOS-11363), and as discussed in Kriek et al. (2007) and later studies (e.g., Marsan et al. 2015) this strongly constrains the contribution of continuum emission from an AGN at \(\lambda_{\text{rest}} \sim 4000\) Å. As we show below and in the following section, the properties of most of the galaxies can be understood in a model where AGNs are present but do not dominate the kinematics, line ratios, line luminosities, or morphology.

4.2. Star Formation Rates

The \(H\alpha\) luminosities can be converted to SFRs if it is assumed that the \(H\alpha\) emission largely originates in \(\text{H} \alpha\) regions. By comparing these SFRs to those derived from the UV and bolometric UV+IR luminosities we can assess whether this assumption is reasonable, and also constrain the amount of obscuration in the galaxies. The \(H\alpha\) SFRs were determined using the Kennicutt (1998) relation, converted to a Chabrier (2003) IMF.14 The UV luminosities come from the best-fitting Brammer et al. (2008) models at \(\lambda_{\text{rest}} = 2500\) Å, and the IR luminosities are converted Spitzer/MIPS 24 μm fluxes (see Whitaker et al. 2012 and Section 2.1).

The relation between the UV/UV+IR SFRs and the \(H\alpha\) SFR is shown in Figure 9. Only the 20 galaxies from our own spectroscopy are considered here, as we do not have self-consistent measurements of \(L(H\alpha)\) for the five objects from Barro et al. (2014b). The \(H\alpha\) SFRs range from \(6 M_\odot\) yr\(^{-1}\) to \(58 M_\odot\) yr\(^{-1}\). They correlate with the UV SFRs (98% significance) and with the UV+IR SFRs, which are dominated by the IR (96% significance). The mean offset between SFR(H\(\alpha\)) and SFR(UV) is 0.47 ± 0.06 dex, with an rms scatter of 0.22 dex. The offset between SFR(H\(\alpha\)) and SFR(UV+IR) is −1.00 ± 0.09 dex, with a scatter of 0.27 dex. The implication is that the \(H\alpha\) emission misses ∼90% of the star formation, and the UV misses ∼97%. The ratios between the three indicators are broadly consistent with expectations from a Calzetti et al. (2000) reddening curve, if there is ∼50% more dust toward nebular emission line gas than toward the UV continuum.15

The X-ray AGNs are indicated by orange points in Figure 9. Remarkably, they are indistinguishable from the other objects: they span the same range in \(H\alpha\) luminosity, and they follow the same relations with the UV and UV+IR luminosities. The offsets between the AGN and non-AGN are consistent with

---

12 The catalogs were searched using the tools of the NASA High Energy Astrophysics Science Archive Research Center (http://heasarc.gsfc.nasa.gov/). We note, however, that the X-ray coverage in the CANDELS fields is not uniform.

13 The correlation between \([N \text{ II}]/H\alpha\) and \(\sigma\) is no longer significant when these four objects are removed.

14 For consistency with previous studies we use a Chabrier (2003) IMF as the default, even though these galaxies may have a more bottom-heavy IMF (see, e.g., Conroy & van Dokkum 2012).

15 We refer to other studies for more detailed analysis of the attenuation toward \(\text{H} \alpha\) regions (e.g., Price et al. 2014; Reddy et al. 2015).
These are the 25 sCMGs; orange centers indicate galaxies with X-ray AGN. The gas in sCMGs does not have the same distribution and the dynamical masses often appear to be lower than the stellar masses. The gas in sCMGs does not have the same distribution and/or kinematics as the stars in qCMGs.

5. INTERPRETATION OF THE VELOCITY DISPERSIONS

5.1. Are the Gas Dynamics Similar to the Stellar Dynamics of Compact Quiescent Galaxies?

The velocity dispersions we measure come from Gaussian fits to the galaxy-integrated, luminosity-weighted Hα line profile and are equivalent to the second moment of the velocity distribution of the gas. They should not be confused with the rotation-corrected gas dispersions within spatially resolved disks, such as discussed by e.g., Kassin et al. (2012) and Förster Schreiber et al. (2014). The measured dispersions are a complex function of the dynamics and gas distribution in the galaxies:

\[ \sigma_{\text{gas}}^2 \sim \alpha^2 v_{\text{rot}}^2 \sin^2(i) + \sigma_{\text{ISM}}^2 + w^2(i)\sigma_{\text{wind}}^2, \]  

with \( \alpha \sim 0.8 \) (Franx 1993; Rix et al. 1997; Weiner et al. 2006; see also Appendix C), \( i \) as the inclination of the galaxy (\( i = 0^\circ \) is face-on, and \( i = 90^\circ \) is edge-on), \( \sigma_{\text{ISM}} \) as the galaxy-integrated dispersion within the gas clouds, and \( w^2(i)\sigma_{\text{wind}} \) as an inclination-dependent term that takes non-gravitational motions into account. A further complication is that Equation (17) is the result of an integral over the area of the galaxy that falls within the slit, weighted by the spatially varying luminosity of the Hα line.

We first assume that the gas in the sCMGs “behaves” in a similar way as the stars in qCMGs. That is, we assume that the stars in qCMGs were formed directly out of the (detected) gas in sCMGs, such that they have the same distribution and kinematics. This has been assumed in previous studies of the kinematics of compact massive star-forming galaxies (Barro et al. 2014b; Nelson et al. 2014) and it may be reasonable if many compact, massive quiescent galaxies are direct descendants of the sCMGs. As discussed in Section 2.4 the stellar velocity dispersions of quiescent galaxies can be predicted from their stellar masses and effective radii (e.g., Taylor et al. 2010a; Bezanson et al. 2011; Belli et al. 2014b). Figure 10(a) shows the relation between \( \sigma_{\text{gas}} \) and the predicted velocity dispersion. The predicted dispersions were calculated using the Sérsic-dependent relation Equation (6).

There is no significant correlation between \( \sigma_{\text{gas}} \) and \( \sigma_{\text{pred}} \) for either the full sample or the sample with the X-ray AGN removed. The rms scatter in \( \sigma_{\text{gas}}/\sigma_{\text{pred}} \) is 0.26 dex. Given that we are ignoring the effects of non-gravitational motions, it is striking that many galaxies have lower velocity dispersions than the expectations. The mean offset is \(-0.08\) dex for the full sample, and \(-0.16\) dex when the AGN are excluded. These results stand in sharp contrast to the stellar velocity dispersions of quiescent galaxies. Red squares are seven galaxies with \( 2 < z < 2.5 \) and measured \( \sigma_{\text{stars}} = r_{\text{e}}, n \) and \( M_{\text{star}} \) from van Dokkum et al. (2009), van de Sande et al. (2013), and Belli et al. (2014b). They have a mean offset in \( \sigma_{\text{stars}}/\sigma_{\text{pred}} \) of \(+0.05\) dex and an rms scatter of only 0.03 dex.

As dynamical mass is proportional to \( \sigma^2 \), the offsets of the sCMGs are even more dramatic in Figure 10(b), which shows the relation between dynamical mass and stellar mass. Here dynamical mass was calculated using

\[ M_{\text{dyn}}^\beta = \frac{\beta(n)\sigma_{\text{obs}}^2r_e}{G}, \]  

as derived by Cappellari et al. (2006) and following studies of quiescent galaxies at high redshift (e.g., van de Sande et al. 2013). For sCMGs \( \sigma_{\text{obs}} = \sigma_{\text{gas}} \) and for quiescent galaxies \( \sigma_{\text{obs}} = \sigma_{\text{stars}} \). Note that, given our definition of \( \sigma_{\text{pred}} \) (see Equation (6)), panels (a) and (b) of Figure 10 are two different ways of presenting the same information. The mean mass offset of the sCMGs is \(-0.16\) dex for the full sample, and
−0.32 dex for the sample with the AGN removed. That is, the dynamical masses of the non-AGN galaxies are on average a factor of two lower than the stellar masses. Several of the galaxies have apparent dynamical masses that are a factor of \( \gtrsim 10 \) lower than their stellar masses. Again, the quiescent galaxies show a tight relation in Figure 10(b), with a mean offset of +0.1 dex.

We conclude that the gas dynamics of sCMGs are not similar to the stellar dynamics of quiescent galaxies in the same mass and redshift range. The stellar masses and sizes are not useful indicators of the observed gas velocity dispersions; in fact, the observed [N II]/H\( \alpha \) ratio is a better predictor of the observed H\( \alpha \) line width of a galaxy than its compactness is. There are many ways to increase the velocity dispersion of a galaxy so it falls above the lines of equality in the two panels of Figure 10: the broad line region of an AGN, AGN-induced winds, and supernova-driven winds can all lead to broad H\( \alpha \) lines (e.g., Westmoquette et al. 2009; Le Tiran et al. 2011; Förster Schreiber et al. 2014; Banerji et al. 2015). This is likely the case for several galaxies in the sample: the four galaxies with the largest dynamical masses are all X-ray AGN with [N II]/H\( \alpha \) ratios in the range 0.8–2.2. However, it is difficult to decrease the observed dispersion. Setting aside the possibility that the stellar masses of some galaxies could be in error by a factor of \( \sim 10 \), this is only possible if the detected ionized gas is sCMGs distributed very differently from the stars in quiescent galaxies. As we show below, there is strong evidence that this is indeed the case.

5.2. Evidence for Rotating Gas Disks

A possible interpretation of the large range of velocity dispersions is that the dynamics are dominated by rotation, and we are seeing disks under a large range of viewing angles. In Figure 11(a) we show the distribution of projected axis ratios \( q = b/a \) in our sample, as determined from the \( H_{160} \) data (see van der Wel et al. 2014b). The axis ratios of the 25 galaxies are inconsistent with a uniform distribution, which would be expected for thin, randomly oriented disks. We find no galaxies with \( q < 0.4 \) and the distribution peaks at \( q \sim 0.75 \). The distribution is consistent with that observed for qCMGs, shown by the red line in Figure 11(a): according to the Kolgomorov–Smirnov test the probability that both samples were drawn from the same distribution of axis ratios is 27%. The distributions are also consistent with results for the general population of massive galaxies at \( z \sim 2 \) (Chang et al. 2013; van der Wel et al. 2014a). We note that we do not detect a significant wavelength dependence of the mean axis ratio of the 25 sCMGs: we find \( \langle q \rangle = 0.76 \pm 0.03 \) in \( J_{125} \) and \( \langle q \rangle = 0.74 \pm 0.03 \) in \( H_{160} \).

Even though the stars are not in thin disks, the gas can be. If the gas is in rotationally supported disks that are aligned with the stellar distribution, the measured velocity dispersions are expected to show an anti-correlation with the observed axis ratios of the galaxies. As shown in Figure 12(a) we see precisely this effect: there is an anti-correlation, with a correlation coefficient of −0.38 and a significance of 94%. This is strong evidence that the gas is in disks and that the measured dispersions are dominated by gravitational motions.\(^{16}\) This anti-correlation is not consistent with M82-

\[^{16}\text{The correlation between }\sigma/\sqrt{M}\text{ and }q\text{ has slightly less scatter, and equal significance.}\]

Figure 11. (a) Distribution of axis ratios among the 25 sCMGs at \( 2 < z < 2.5 \). The distribution is not uniform, and is inconsistent with thin disks under random viewing angles. The axis ratio distribution of qCMGs in the same redshift range is shown in red. The orange line is a model for randomly oriented oblate objects with intrinsic thickness \( q_0 = C/A = 0.4–0.75 \). (b) The relation between median inclination and observed axis ratio in this model. Dotted lines indicate the ±1σ spread. (c) Inclination correction as a function of observed axis ratio.

\[^{17}\text{It is well known that the axis ratio distribution by itself is insufficient to constrain all three axes }A, B,\text{ and }C\text{ (see, e.g., Franx et al. 1991). Although there is some evidence that the stellar distribution of compact }z \sim 2\text{ galaxies is oblate or disk-like rather than triaxial (e.g., van der Wel et al. 2014a; Zolotov et al. 2015), in our paper this is an assumption, not a result.}\]
thinner disks, and all we assume is that the gas disks of the galaxies are aligned with their stellar distributions.

For galaxies with intrinsic thickness $q_0$ the relation between the inclination and the observed axis ratio is given by

$$i = q_0 \cos \left( \frac{1}{2} \right) \left( q - q_0 \right) \left( \frac{1}{2} \right) \left( q - q_0 \right).$$

As $q_0$ is not a constant in our model the relation between $i$ and $q$ is not single-valued. The solid line in Figure 11(b) shows the median relation, and the broken lines indicate the 1σ scatter. Figure 11(c) shows the inclination correction $\sin^{-1}(i)$ as a function of $q$.

The inclination-corrected rotation velocities are shown in Figure 12(b). They are derived from the gas velocity dispersions and the observed axis ratios of the galaxies using the average relation in 11(c) and assuming $\alpha = 0.8 \pm 0.2$ (see Rix et al. 1997; Weiner et al. 2006). In Appendix C we show that this value is a reasonable approximation for the geometries of both the mass and the ionized gas that we derive in this paper. The large uncertainty reflects the fact that the conversion of dispersion to rotation velocity depends on the spatial distribution of the gas, and the underlying velocity field (see Appendix C). Data of much higher spatial resolution and S/N are needed to measure $\alpha$ directly for these extremely compact galaxies. The uncertainty in $\alpha$ and 50% of the (logarithmic) inclination correction were added in quadrature to the error budget. The median rotation velocity for the full sample is $V_{\text{rot}} = 338 \text{ km s}^{-1}$ for the full sample and $271 \text{ km s}^{-1}$ when AGN are excluded.

Figure 12. (a) Observed relation between the Hα velocity dispersion and the H160 axis ratio. Orange centers indicate X-ray AGNs. There is a significant (anti-)correlation between $\sigma_{\text{gas}}$ and $q$, as expected if there is a significant contribution from rotation to $\sigma_{\text{gas}}$ and the Hα disks are aligned with the stellar distribution. The gray line indicates the expected trend for rotating disks (Figure 11(c)). (b) Inferred rotation velocity vs. axis ratio. The rotation velocities were corrected for inclination using the observed axis ratios (see the text). The median rotation velocity is 338 km s$^{-1}$ for the full sample and 271 km s$^{-1}$ when AGN are excluded.

Figure 13. Relation between dynamical mass and stellar mass, with dynamical masses calculated from the inclination-corrected rotation velocities and the stellar half-light radii. Most galaxies fall below the line of equality.

If it is assumed that $r_e$ is not only the half-light radius in the H160 band but also the half-light radius of the Hα emission, we can define the dynamical mass as

$$M_{\text{dyn}}^V = \frac{2V_{\text{rot}}^2 r_e}{G}.$$  

18 Although the gas disks likely have lower C/A than the stellar distribution, they are probably not as thin as disks in the local universe (see, e.g., Cresci et al. 2009).

19 For completeness, we note the interesting possibility that the two peaks in the spectra may not be Hα and [N ii] but two narrow peaks in a "double-horned" Hα profile that happen to have exactly the separation of Hα and [N ii]λ6584. This may happen when the Hα emission originates from a narrow ring rather than a disk. In most cases that interpretation can readily be ruled out, from the spatially resolved line profile (see Section 6.2) or from the detection of the [N ii]λ6548 line, but in a few cases (e.g., AEGIS_41114) it is difficult to exclude this possibility without observing other emission lines.
This is not a true total mass but simply twice the enclosed mass within the half-light radius. In Figure 13 this dynamical mass is compared to the stellar mass. Although the inclination corrections have lessened the offsets of the most extreme outliers, it is clear that orientation effects are not sufficient to explain the relatively low velocities that have been measured for a large fraction of the sample. The mean offset for the whole sample is $-0.19$ dex, and the scatter is $0.55$ dex. In the next section we show that variation in the spatial extent of the ionized gas with respect to that of the stars is a likely source of both the offset and scatter in Figure 13.

6. SPATIALLY EXTENDED GAS DISKS

6.1. Inferred Sizes of Gas Disks

In the previous section we showed that many galaxies have galaxy-integrated velocity dispersions that are much smaller than expected from their stellar masses and sizes. As demonstrated in Section 5.2 this is partly caused by the $\sin(i)$ reduction of the velocity of rotating disks. However, even after correcting the observed dispersions to inclination-corrected rotation velocities the dynamical masses are typically lower than the stellar masses, particularly for galaxies that do not host an X-ray AGN.

So far we have assumed that the spatial extent of the gas is similar to that of the stars, that is, $r_{\text{gas}} \sim r_{\text{stars}} = r_e$, where $r_{\text{gas}}$ is the half-light radius of the measured H$\alpha$ distribution. There is no a priori reason why this should be the case; e.g., in the models of Zolotov et al. (2015) compact galaxies often have rings of gas and young stars around their dense centers, which originate from ongoing accretion from the halo. Furthermore, as shown earlier $\sim$90% of the star formation in sCMGs is obscured, and the extinction is expected to be particularly high toward the central regions (e.g., Gilli et al. 2014; Nelson et al. 2014). The distribution of detected H$\alpha$ emission may therefore be less centrally concentrated than the distribution of star formation.

The radius of the gas disks can be inferred from $V_{\text{rot}}$ if we assume that the observed velocity is the circular velocity of the stellar body at the radius of the gas. The gas radius then depends on $V_{\text{rot}}$, the stellar mass, and the structural parameters of the galaxy:

$$r_{\text{gas}} \sim \frac{G}{V_{\text{rot}}^2} f(r_{\text{gas}}) M_{\text{stars}}, \quad (22)$$

with $V_{\text{rot}}$ as the inclination-corrected rotation velocity and $f(r_{\text{gas}})$ as a function that depends on the mass distribution of the galaxies:

$$f(r_{\text{gas}}) = \int_0^{r_{\text{gas}}} \frac{I(r)}{2\pi r} dr \int_0^{\infty} \frac{I(r)}{2\pi r} dr. \quad (23)$$

Here $I(r)$ is the best-fitting Sérsic profile to the light distribution. For $r_{\text{gas}} = r_{\text{stars}} (\approx r_e)$, $f(r_{\text{gas}}) = 0.5$ and Equation (22) is equivalent to Equation (21) with $M_{\text{dyn}} = M_{\text{stars}}$. These expressions ignore the fact that the 2D radii are not identical to the 3D radii, assume that the stellar mass distribution can be approximated by the $H_{160}$ luminosity distribution, and assume that the contributions of gas and dark matter to the total mass can be neglected on the scales that are probed by the H$\alpha$ emission.

Solving Equation (22) numerically, we find that the inferred gas disk sizes range from $\sim 0.2$ to $\geq 10$ kpc. This large range is not surprising, as it is effectively an interpretation of the large variation that is seen in Figure 13. Figure 14 shows the relation between inferred $r_{\text{gas}}$ and the stellar effective radius. The gas radii are typically larger than the stellar radii, particularly for the galaxies that do not have an X-ray AGN (black points). The ratio between the gas radius and the stellar radius is shown explicitly in the bottom panel of Figure 14. The mean ratio,

$$r_e = r_{\text{star}} \quad (\text{kpc})$$

Figure 14. Relation between inferred radius of the gas distribution and the stellar half-light radius. Orange points indicate galaxies with X-ray AGNs. The gas radii were determined from the stellar masses and the inclination-corrected rotation velocities. There is a large scatter, reflecting the large scatter in Figure 13. The ratio between the gas size and the stellar size is shown in the bottom panel. Non-AGN (black) and AGN (orange) are shown separately. The galaxies with AGNs have, on average, compact inferred gas distributions. For the non-AGN (black histogram) the average spatial extent of the gas is $\sim 2.3 \times$ larger than that of the stars.

$^{20}$ That is, the distribution of the ionized gas, with no extinction corrections applied. Measuring the true $r_{\text{gas}}$ requires molecular line measurements with high spatial resolution.

$^{21}$ We note that there are two solutions to Equation (22), as the gas could in principle also be located in the inner $\lesssim 50$ pc where the rotation curve is still rising (see, e.g., Figure 18). This is unlikely given that the galaxies have, by selection, star-forming SEDs with a spatial extent of $\sim 1$ kpc. Furthermore, as we show later, the large radius solutions are corroborated by the measured spatial extent of the H$\alpha$ emission.
calculated with the biweight statistic (Beers et al. 1990), is
\[ \log r_{\text{gas}} - \log r_{\text{stars}} = 0.18 \pm 0.10 \] for the full sample. Excluding
galaxies with an AGN, we find \( \log r_{\text{gas}} - \log r_{\text{stars}} = 0.37 \pm 0.14 \). That is, the
gas disks are a factor of \( \sim 2.3 \) more extended than the stellar distribution. This is strictly a lower
limit, as it is assumed that only stars contribute to the stellar mass, the galaxies have a relatively “light” Chabrier (2003)
IMF, and there are no contributions from non-gravitational motions to the measured velocity dispersions.

6.2. Measured Sizes of Gas Disks

We can test directly whether the sCMGs are embedded in large gas disks by examining the observed spatial extent of
the emission lines. Even though the galaxies were selected to be extremely compact, the inferred spatial extent of the emission
line gas is so large that it should (just) be detectable in ground-based, seeing-limited observations. The 2D spectra are shown
in Figure 15; they cover a rest-frame wavelength range from 6551 to 6596 A and a spatial extent along the slit of \( \pm 15'5 \).
The five empty panels are the sCMGs from Barro et al. (2014b).

Remarkably, about 1/3 of the galaxies show velocity gradients. They are most prominent in UDS_33334, UDS_26012, and UDS_16442, but also visible in GOODS-S_5981, UDS_42571, and UDS_35673. The seeing ranged
from 0.6 to 1.0, and the stellar half-light radii of the galaxies are typically 0.1. Therefore, the fact that we spatially resolve
the H\( \alpha \) emission immediately demonstrates that the ionized gas extends to larger radii than the stars in these galaxies. We emphasize here that we do not attempt to measure rotation
curves directly from these velocity gradients, as this can only be done reliably when the sizes of galaxies are similar to, or
larger than, the spatial resolution of the data (see, e.g., Vogt et al. 1996; Miller et al. 2011; Newman et al. 2013).

For the nine galaxies that were observed with MOSFIRE we can measure the spatial extent of the H\( \alpha \) emission. As discussed in Section 3.1 a bright star was included in all MOSFIRE masks, and the profile of this star in the spatial
direction can be used to approximate the PSF. We extracted spatial profiles of the combined H\( \alpha \) and [N\( \text{II} \)] emission for
the nine galaxies by averaging the data in the wavelength direction. Each column was weighted by the inverse of the noise (which
is dominated by sky emission lines); we did not weight by the signal as this would bias the profile toward the central regions.
The spatial profiles are shown in Figure 15 (black points with error bars). Each panel also shows the profile of the star that
was observed in that particular mask (orange points); the FWHM of this profile is also indicated.

The profiles were fit by a model to determine the half-light radii of the ionized gas. The model has the form
\[ M(r) = \Sigma(r) \ast P(r), \]
with \( r \) as the position along the slit, \( \Sigma(r) \) as the model for the one-dimensional surface brightness profile of H\( \alpha \) along the slit,
\( P(r) \) as a Gaussian fit to the profile of the star, and \( \ast \) denoting a convolution. The Gaussian fits to the stellar profiles are shown
by orange lines in Figure 15. Parameterizing \( P(r) \) with the sum of two Gaussians does not improve the fit to the stellar profile
or change the results. It is not possible to constrain the functional form of the surface brightness profile with our data.
Instead, we assume that the H\( \alpha \) is in an exponential disk (see

Nelson et al. 2013):
\[ \Sigma(r) = \Sigma(0) \exp \left( -\frac{1.678 |r - r_{\text{cen}}|}{r_{\text{gas}}} \right). \]

Here \( \Sigma(0) \) is a normalization factor, \( r_{\text{cen}} \) is the center of the profile, and \( r_{\text{gas}} \) is the half-light radius of the ionized gas.

We fitted this model to the data using the emcee code, as described for the fits in the wavelength direction in Section 3.4.1. Again, the priors are top hats with bounds that do not constrain the fits or the error bars. Rather than \( r_{\text{gas}} \) itself we fit \( \log r_{\text{gas}} \); the error distribution of \( r_{\text{gas}} \) is highly asymmetric, which means that the peak of the distribution of samples does not coincide with its 50th percentile. The distribution of the \( \log r_{\text{gas}} \) samples is symmetric. The resulting measured gas radii, converted to kpc, are listed in the panels of Figure 15. For
seven out of nine galaxies the value of \( r_{\text{gas}} \) is different from zero with \( >2\sigma \) significance.

A geometric correction needs to be applied to the measured values of \( r_{\text{gas}} \) to account for the fact that the slit is typically not
aligned with the major axis of the gas disk. This correction depends on the orientation of the slit and on the inclination of the
gas disk:
\[ r_{\text{gas}} \approx \left[ \cos^2(i) + \cos^2(\text{PA}_{\text{slit}} - \text{PA}_{\text{gal}}) \right]^{-\frac{1}{2}} r_{\text{gas}} \]

with \( i \) as the inclination (as derived in Section 5.2), \( \text{PA}_{\text{slit}} \) as the position angle of the slitmask, and \( \text{PA}_{\text{gal}} \) as the orientation of
the galaxy on the sky (as determined with GALFIT). Note that the corrected \( r_{\text{gas}} \) is measured along the major axis (and is not a circularized radius), consistent with our interpretation that the gas is in thin, rotating disks. The median correction is small at
9%. For GOODS-S_30274 we use the median correction of the other eight galaxies, as its PA mostly reflects the orientation of
its tidal tail. We use the corrected radii when comparing the measured radii to predicted radii and when deriving the rotation
curve of the galaxies in Section 6.4.

For three galaxies, UDS_35673, GOODS-S_30274, and GOODS-N_6215, we obtained an independent measurement of the extent of the emission line gas from their WFC3/G141 grism spectra. These are the only galaxies in the sample of 25 that have grism spectra covering the redshifted [O\( \text{III} \)] \( \lambda4959,5007 \) lines and a detection of these lines with \( >5\sigma \)
significance. As shown in Nelson et al. (2012) emission line spectra in grism spectra are images of the galaxy in the light of that line, providing direct information on the distribution of ionized gas at \( 0.014 \) resolution. The interpretation of the [O\( \text{III} \)] lines is complicated by the fact that the two lines are very close
together on the detector. We fit the lines simultaneously with
GALFIT (Peng et al. 2002), keeping their relative location and flux rate fixed and using a PSF generated with Tiny Tim
(Krist 1995). Two of the three galaxies (UDS_35673 and GOODS-S_30274) are also in the MOSFIRE sample. The best-fit
G141 [O\( \text{III} \)] radii of these objects are 1.6 \( \pm 0.3 \) kpc and 5.1 \( \pm 1.5 \) kpc, in excellent agreement with the MOSFIRE H\( \alpha \)
values (1.3 \( \pm 0.2 \) kpc and 3.9 \( \pm 1.4 \) kpc, respectively). The third galaxy, GOODS-N_6215, has a G141 [O\( \text{III} \)] radius of 3.0 \( \pm 1.0 \) kpc. In the following, we show all 12 measurements in
figures (nine from MOSFIRE, three from HST), with lines
connecting the two independent measurements for UDS_35673 and GOODS-S_30274.

6.3. Comparison of Inferred and Measured Sizes

For the 10 galaxies with gas size measurements we can directly compare the inferred sizes to the measured ones. The results are shown in Figure 16. There is a clear correlation, with a significance of >99%. Furthermore, the offset between the two sets of radii is small. Giving equal weight to all 12 measurements we find a difference of only $-0.09 \pm 0.07$ dex. This excellent agreement between inferred and measured radii provides support to our modeling of the observed kinematics of sCMGs.

Figure 15. Two-dimensional MOSFIRE and NIRSPEC spectra centered on the redshifted Hα and [N II] lines. The galaxies are ordered by their observed galaxy-integrated velocity dispersion, as in Figures 5–7. The inclination-corrected rotation velocity $V_{rot}$ (in km s$^{-1}$) is indicated in each panel. At least 1/3 of the galaxies show velocity gradients, demonstrating that their ionized gas distributions are spatially resolved in these ground-based, seeing-limited data. For the nine galaxies observed with MOSFIRE the spatial extent of the gas can be measured, using the profile of a star (orange). Black curves are the best fitting exponential profiles convolved with the PSF. The measured half-light radii of the Hα emission ($r_{halo}$ in kpc) are indicated.
the galaxies; this is consistent with disks under a range of viewing angles and difficult to reconcile with M82-style galactic winds (Figure 12(a)). (3) Nearly all galaxies with spatially resolved gas distributions show velocity gradients\(^\text{22}\) (Figure 15). (4) Inferring the sizes of the gas disks from the inclination-corrected rotation velocities, we find good agreement between the inferred sizes and the measured sizes (Figure 16).

### 6.4. Keplerian Rotation out to 7 kpc

The measured kinematics can be used to constrain the total mass within ~7 kpc. We can derive a spatially resolved rotation curve by making use of the fact that the measured spatial extent of the gas varies by a factor of 10 (see Figure 16), under the assumption that the galaxies have similar inclination-corrected dynamics after scaling them to a common mass. The validity of this approach is demonstrated in Appendix C, where we calculate the relation between the observed galaxy-integrated line widths and the actual rotation velocity at \( r = r_{\text{gas}} \). To bring all galaxies to the same normalization, we first define the scaled rotation velocity as

\[
V^2_{\text{rot}} = \frac{V_{\text{rot}}}{\overline{M_{\text{stars}}}/\overline{M_{\text{stars}}}},
\]

with \( \bar{M}_{\text{stars}} = 1.0 \times 10^{11} M_\odot \) the median stellar mass of the full sample of 25 sCMGs. We note that this scaling does not change the velocities by a large amount, as the galaxies in our sample span a small mass range.

In Figure 18 the scaled velocities are plotted as a function of the measured gas half-light radius \( r_{\text{gas}} \) (corrected for slit orientation) for the 10 galaxies that have this measurement. The rotation curve declines: in galaxies where H\(\alpha\) is measured at a larger distance from the center, the inclination-corrected rotation velocity is lower. The decline has a formal significance >99%. Falling rotation curves have been seen previously in some individual (large, non-compact) \( z \sim 2 \) galaxies (e.g., the galaxies D3a6397 and zC400690 in Genzel et al.\(^{2014}a\)). The solid line is the predicted rotation curve for an \( M = 10^{11} M_\odot \) galaxy with the median effective radius (\( r_e = 1.3 \) kpc) and median Sérsic index \( (n = 4) \) of the sCMGs, calculated with Equation (22). This model is a good description of the data: \( \chi^2 = 6.5 \) with 12 degrees of freedom. The gray line is a model with two mass components: in addition to the stellar component this model has a gas component with the same mass as the stars (i.e., the gas fraction in this model is \( f_{\text{gas}} \equiv M_{\text{gas}}/(M_{\text{stars}} + M_{\text{gas}}) = 0.5 \)). For consistency with the previous sections, the spatial distribution of the gas is assumed to be exponential with \( r_{\text{gas}} = 2.5 \times r_e \). The gray line overpredicts the observed velocities: with \( \chi^2 = 30.0 \) this model can be ruled out with 99% confidence.

We can derive an upper limit to the gas mass within 7 kpc by assuming that the uncertainty in the stellar mass is small and allowing the mass in the gas component to vary. The 95% confidence upper limit to the gas mass is \( M_{\text{gas}} < 0.6 \times 10^{11} M_\odot \), corresponding to a limit on the gas fraction of \( f_{\text{gas}} < 0.4 \). It appears that the gas is mostly a tracer of, rather than a contributor to, the kinematics. Finally, we derive the best fitting mass within \( r = 7 \) kpc by assuming that \( f_{\text{gas}} = 0 \) and allowing \( M_{\text{stars}} \) to vary: \( \overline{M_{\text{fit}}} = 0.8^{+0.6}_{-0.4} \times 10^{11} M_\odot \), where the error bars are 95% confidence limits. Although this estimate assumes that mass follows light, we verified that the results are very similar

---

\(^{22}\) There are indications that the presence of velocity gradients anti-correlates with the axis ratio, as expected in the rotating disk interpretation, but larger samples with higher spatial resolution are needed to confirm this.
for more extended mass distributions. We conclude that the dynamical mass within $r \sim 7$ kpc is fully consistent with the stellar mass that is implied by the stellar population fit; and that there is little room for additional stars, gas, or dark matter inside this radius.

7. ARE STAR-FORMING COMPACT GALAXIES THE MAIN PROGENITORS OF QUIESCENT COMPACT GALAXIES?

In the previous sections we have shown that a population of star-forming galaxies exists at $z \gtrsim 2$ whose dynamical mass within $\sim 7$ kpc is dominated by a massive, compact, stellar component. We now ask whether these galaxies can be progenitors of the population of massive, compact, quiescent galaxies, by considering their number densities, morphologies, and SFRs. This question has been discussed before by, e.g., Williams et al. (2014, 2015), Bruce et al. (2014), Nelson et al. (2014), Dekel & Burkert (2014), Zolotov et al. (2015). Arguably the most extensive observational study is a series of papers by Barro et al. (2013, 2014a, 2014b), using data over two (Barro et al. 2013, 2014b) or one (Barro et al. 2014a) of the five fields that we study here. Using our larger data set and more restrictive selection we find broadly similar results.

7.1. Number Density Evolution

A star-forming CMG will resemble a quiescent CMG if star formation stops (quenching). However, the opposite is also true: a quiescent compact galaxy that starts forming stars due to the accretion of new gas (see, e.g., Graham et al. 2015; Zolotov et al. 2015) could resemble a star-forming compact galaxy (rejuvenation). We can determine whether quenching or rejuvenation dominates by measuring the number density of sCMGs and qCMGs as a function of redshift. The selection criteria of Section 2.3 were applied in small redshift bins, and the number density was determined by dividing the number of galaxies in the bin by its volume. The result is shown in Figure 19 (filled points and solid curves).

At $2.0 < z < 2.5$ the number densities of the two populations are very similar, as already noted in Section 2.4. However, at higher and lower redshifts the number densities are different: the sCMGs have a roughly constant number density from...
galaxies grow in size due to mergers at $z < 1.5$. This implies that only about half of the star-forming galaxies disappear from one redshift bin to the next, and that the average quenching timescale is roughly equal to the time interval between the redshift bins: $\tau_c \sim 0.5$ Gyr. This is the average lifetime of star-forming galaxies in the “compact massive” selection box, assuming that they all turn into quiescent galaxies. It is slightly lower than the value of $\sim 0.8$ Gyr derived by Barro et al. (2013), but judging from their Figure 5 the two studies are broadly consistent.

Although somewhat outside of the scope of this paper, we briefly discuss the number density evolution at lower redshift. The number density of sCMGs drops precipitously after $z \sim 1.8$. This drop leads to a plateau in the number density of qCMGs: as the number of star-forming progenitors decreases, no new quiescent galaxies are added to the sample. At the lowest redshifts the number density of compact quiescent galaxies decreases (as was also found by Taylor et al. 2010b; van der Wel et al. 2014b, and van Dokkum et al. 2014, among others), while the number density of all massive quiescent galaxies rises steeply (dashed red curve). The likely explanation is that the compact galaxies accrete extended envelopes through merging from $z \sim 1.5$ to the present day (e.g., Bezanson et al. 2009; Naab et al. 2009; van Dokkum et al. 2010, 2014; Newman et al. 2012; Hilz et al. 2013).

Finally, we note that Figure 19 is not new: the peak in the number density of compact, massive quiescent galaxies was also shown in Cassata et al. (2011, 2013), Barro et al. (2013), and van der Wel et al. (2014). Barro et al. (2013) derive a similar lifetime for star-forming galaxies in the compact selection region. Although uncertainties remain (particularly at low redshift; see, e.g., Carollo et al. 2013), it is encouraging that these largely independent samples give similar results.

7.2. Morphologies and Radial Surface Brightness Profile

The large spatial extent of the ionized gas raises the question whether the stellar half-light radii and masses of the compact star-forming galaxies have been underestimated: although it is difficult to bias GALFIT measurements in this direction (see, e.g., Davari et al. 2014), it is possible that the galaxies have extended low surface brightness envelopes (see, e.g., Hopkins et al. 2009a). If such envelopes exist this would call into question whether sCMGs can be direct progenitors of compact quiescent galaxies with the same apparent mass and half-light radius.

Images of the galaxies are shown in Figure 6 and in Figure 29 (see Section 3.3). Visually, most of the objects have a compact luminosity distribution and no spiral arms, clumps, star-forming complexes, or other features outside of the dense center. Several of the reddest galaxies do not appear to be very compact: for example, UDS_42571 and, in particular, UDS_16442 are faint and fuzzy rather than bright and compact. The reason for their relatively low surface brightness is that dust obscuration has dramatically lowered their luminosity: as galaxies can have high mass-to-light ratios, compact in mass does not necessarily imply compact in light.

Two objects show unambiguous evidence for ongoing or past mergers: GOODS_S_30274 has an asymmetric feature resembling a tidal tail, and COSMOS_11363 is one component of a spectacular merger between two compact galaxies with a projected separation of $0.76$ (5 kpc). The companion of

---

**Figure 19.** Evolution of the number density of sCMGs (blue solid line) and of qCMGs (red solid line). The number density of all star-forming and quiescent galaxies with log($M_{\text{star}}$/sun) > 10.6 is also shown (dashed lines). The data suggest that compact star-forming galaxies continuously enter the selection region from $z \gtrsim 2.8$ to $z \sim 1.8$ and quench, leading to a strong increase in the number of compact quiescent galaxies. When the number of sCMGs begins to decrease at $z < 1.8$, the number of qCMGs first plateaus and then drops, as quiescent galaxies grow in size due to mergers at $0.5 < z < 1.5$.

$z \sim 2.8$ to $z \sim 1.8$, whereas the number density of qCMGs increases by an order of magnitude over that same redshift range. A straightforward interpretation is that star-forming galaxies continuously enter the “compact massive” selection box (because of a decrease in their size and/or an increase in their mass), and quench shortly after. This continuous quenching then leads to a rapid build-up of the number of quiescent galaxies in the compact/massive selection region. We conclude that quenching likely dominates over rejuvenation: if rejuvenation dominated, we would have expected to see quiescent galaxies disappear as their star formation (re-)started, unless there are other channels to create quiescent compact galaxies. We note that the evolution of the number densities of the two populations is qualitatively similar to the simulations of Zolotov et al. (2015).

It is difficult to determine how long it takes before a compact star-forming galaxy turns into a quiescent galaxy, as this depends on the rate with which new galaxies enter the sample. The number density of sCMGs is constant from $z \sim 2.8$ to $z \sim 1.8$, which means that new sCMGs enter the sample at approximately the same rate as existing ones quench. We can obtain a very rough estimate of the “compact life time” of star-forming galaxies $\tau_c$ by adding the number densities of the sCMGs in the three redshift bins that cover this period: if the average quenching time is much shorter than the time interval between redshift bins, all galaxies in each bin are new arrivals and should be added to the sample of progenitors of quiescent galaxies. The combined number density in these bins (which are of nearly equal volume) is $2.0 \times 10^{-4}$ Mpc$^{-3}$, higher than the increase in the number density of the qCMGs over this period ($1.3 \times 10^{-4}$ Mpc$^{-3}$). This implies that only about half of the star-forming galaxies disappear from one redshift bin to the next, and that the average quenching timescale is roughly equal to the time interval between the redshift bins: $\tau_c \sim 0.5$ Gyr. The likely lifetime of star-forming galaxies in the “compact massive” selection box, assuming that they all turn into quiescent galaxies. It is slightly lower than the value of $\sim 0.8$ Gyr derived by Barro et al. (2013), but judging from their Figure 5 the two studies are broadly consistent.

Although somewhat outside of the scope of this paper, we briefly discuss the number density evolution at lower redshift. The number density of sCMGs drops precipitously after $z \sim 1.8$. This drop leads to a plateau in the number density of qCMGs: as the number of star-forming progenitors decreases, no new quiescent galaxies are added to the sample. At the lowest redshifts the number density of compact quiescent galaxies decreases (as was also found by Taylor et al. 2010b; van der Wel et al. 2014b, and van Dokkum et al. 2014, among others), while the number density of all massive quiescent galaxies rises steeply (dashed red curve). The likely explanation is that the compact galaxies accrete extended envelopes through merging from $z \sim 1.5$ to the present day (e.g., Bezanson et al. 2009; Naab et al. 2009; van Dokkum et al. 2010, 2014; Newman et al. 2012; Hilz et al. 2013).

Finally, we note that Figure 19 is not new: the peak in the number density of compact, massive quiescent galaxies was also shown in Cassata et al. (2011, 2013), Barro et al. (2013), and van der Wel et al. (2014b). Barro et al. (2013) derive a similar lifetime for star-forming galaxies in the compact selection region. Although uncertainties remain (particularly at low redshift; see, e.g., Carollo et al. 2013), it is encouraging that these largely independent samples give similar results.

---

23 The evolution of compact quiescent galaxies may become more gradual at $z > 3$: Straatman et al. (2015) recently reported the existence of a sizeable population of compact, massive quiescent galaxies at $z \sim 4$, based on medium-band near-IR photometry.
COSMOS_11363 is COSMOS_11337 in the Skelton et al. (2014) catalog. Our Keck/NIRSPEC and HST/WFC3 spectroscopy confirms that they are at the same redshift. With $r_e = 1.0$ kpc and $M_{\text{stars}} = 1.7 \times 10^{11} M_\odot$, COSMOS_11337 is actually significantly more compact than COSMOS_11363. Its rest-frame UVJ colors (just) give it a quiescent classification. This merging pair seems to suggest that CMGs can form in mergers (Hopkins et al. 2009b), but that is not the right interpretation: as both galaxies already fall in the “compact massive” selection region, this particular type of merger actually decreases their number. Even if the result of the merger falls in the selection region, there will be one less CMG. Interestingly, several other galaxies show evidence for distorted outer isophotes in Figure 29. This could indicate interactions are common for these galaxies, but the evidence is not conclusive at the depth of the CANDELS imaging.

To quantify the stellar emission on scales $\gg 1$ kpc we stacked the $H_{160}$ images of the 25 sCMGs and measured their averaged radial surface brightness profile to faint levels. Each galaxy was normalized by its total $H_{160}$ flux prior to stacking, so that the stack is not dominated by a few bright objects. Neighboring objects, identified from the SExtractor segmentation map (see Bertin & Arnouts 1996; Skelton et al. 2014), were masked. The resulting surface brightness profile is shown in the top panel of Figure 20 (blue points). We fit the stack with a PSF-convolved Sérsic profile to determine whether there is evidence for an additional component at large radii. This fit, done with GALFIT (Peng et al. 2002), is shown by the blue line. It is an excellent description of the data out to 15 kpc ($> 10 r_e$): there is no excess light beyond a single Sérsic profile. Furthermore, the best-fitting effective radius ($r_e = 1.3$ kpc) and Sérsic index ($n = 3.6$) are similar to the median values of the 25 galaxies that went into the stack: $(r_e) = 1.4$ kpc and $(n) = 4.3$.

The stacked sCMG profile is compared to a stacked qCMG profile, shown in red in Figure 20. The qCMGs in this Figure are a subset of the full population: they were selected in narrow bins of mass and effective radius, centered on the median values of the 25 sCMGs. This ensures that any differences between the stacks are not caused by a difference in the mean size or mass of the samples. The quiescent profile is virtually indistinguishable from that of the star-forming galaxies. Finally, $J_{25} - H_{160}$ color profiles of both stacks are shown in the bottom panel of Figure 20. Both stacks are bluer at larger radii and the gradients are small, qualitatively consistent with previous work (Szomoru et al. 2012). The negative color gradients imply that the galaxies are even more compact in mass than in light, and that any stellar emission at $r > r_e$ is not missed because it is enshrouded in dust.

We conclude that the morphologies of the sCMGs are consistent with being direct progenitors of qCMGs. When selected to have the same mass and effective radius, their surface brightness profiles are indistinguishable out to at least 15 kpc. We find a relatively high Sérsic index for both populations. Such high values (and the relatively round 3D morphologies; see Section 5.2) are consistent with violent relaxation following a merger, but also with composite structures, such as envelopes of material around extremely compact exponential disks.

$\frac{M_c}{M_{\text{stars}}} \sim \text{SSFR} \times w \times \tau_c,$ (29)

with SSFR as the specific star formation rate, $w$ as a correction for mass loss due to stellar winds, and $\tau_c$ as the average life time of star-forming galaxies in the compact, massive selection region. The median SSFR of the sCMGs is $\text{SSFR} = 1.2 \times 10^{-9}$ yr$^{-1}$, and for $w \sim 0.6$ (Chabrier 2003) and $\tau_c \sim 0.5$ Gyr (Section 7.1) we find $M_c \sim 0.4 M_{\text{stars}}$. As they are, on average, observed halfway through their lifetime in the compact selection region, their final mass before quenching will be

---

24 We note that the rest-frame $J$ magnitudes of these objects are somewhat uncertain as they rely on accurate deblending of the IRAC fluxes; it may well be that both galaxies are sCMGs.
Figure 21. Relation between specific star formation rate and compactness ($\alpha M_{stars}/\sigma_c$), for galaxies in the “massive, compact” selection box at $2 < z < 2.5$. Red points are UVJ quiescent galaxies; blue points are UVJ star-forming galaxies. Within the sample of massive compact galaxies, the specific star formation rate, and the fraction of UVJ star-forming galaxies, declines with the degree of compactness. The right axis is the fraction of mass that will be added to the galaxies in 0.5 Gyr, which is the estimated average lifetime of star-forming galaxies in the massive, compact region. About 1/3 of the mass of compact quiescent galaxies was formed in the compact phase.

$M_{stars,final} = M_{stars} + 0.5M_c \sim 1.2M_{stars}$, and the fraction of $M_{stars,final}$ that is formed in the compact phase is then $\sim 1/3$. We conclude that sCMGs are responsible for forming a significant fraction of the stars that are present in compact quiescent galaxies.

An implication of this result is that the spatial distribution of the H$\alpha$ emission in sCMGs is probably more extended than the spatial distribution of star formation in these galaxies. This is qualitatively similar to results for galaxies at $z \sim 1$ (Nelson et al. 2012, 2015), and may indicate that star formation has ceased in the inner regions of the galaxies (e.g., Genzel et al. 2014a;Tacchella et al. 2015). However, as discussed in Section 4.2 most of the star formation in sCMGs is obscured, and the observed H$\alpha$ emission accounts for only $\sim 10\%$ of the total star formation. As the column density is a very strong function of radius in these compact galaxies (see, e.g., Gilli et al. 2014; Nelson et al. 2014), the obscuration-corrected distribution of star formation is almost certainly much more compact than the observed distribution of H$\alpha$ emission—at least for the galaxies with low observed velocity dispersions.

A somewhat puzzling aspect of the sCMGs is that they have very high SSFRs even though their observed kinematics leave little room for a large gas reservoir (see Section 6.4). Many studies have found that the molecular gas and dust content of galaxies increases with redshift, and reaches $>50\%$ of the total baryonic mass for $z \sim 2$ galaxies with the highest SFRs (e.g., Daddi et al. 2010; Tacconi et al. 2010; Genzel et al. 2015; Scoville et al. 2015). Using the scaling relations derived in Genzel et al. (2015), the expected gas fraction for the galaxies in our sample is $\sim 60\%$. One possible explanation for their relatively low gas fraction is that the galaxies have nearly exhausted their reservoir and are about to quench. If the galaxies typically build $\sim 40\%$ of their mass inside the compact, massive selection region, the average sCMG should have $\sim 30\%$ of their mass in gas (for $w \sim 0.6$); this is just consistent with the 95% confidence upper limit on the gas fraction of 40% that we derived in Section 6.4. Another explanation is that newly accreted gas is continuously and efficiently funneled into the central regions, and the SFRs are “accretion throttled” (Dekel et al. 2009); in that case the gas depletion time can be shorter than the actual duration of star formation (see, e.g., Genzel et al. 2010). Direct observations of the dust and molecular gas in sCMGs, at $\sim 1$ kpc resolution, are needed to address these questions.

Finally, we note that star-forming galaxies tend to be less compact than quiescent galaxies even _within_ the population of CMGs at $2 < z < 2.5$ (see Figure 21). As discussed earlier in the context of the sample selection (Section 2.4), star-forming galaxies are always less compact than quiescent galaxies, irrespective of the precise criteria for their selection. In the next section we interpret the distribution of galaxies in the size–mass plane in the context of a simple model, in which star-forming galaxies become gradually more compact and the probability of quenching rises smoothly as their compactness increases.

8. FORMATION OF STAR-FORMING COMPACT GALAXIES

8.1. A Simple Model for Building Massive Galaxies

In this section we turn to the formation of compact, massive star-forming galaxies. Several distinct mechanisms have been discussed in the literature, including mergers of gas-rich galaxies (Tacconi et al. 2008; Hammer et al. 2009; Hopkins et al. 2009b; Wellons et al. 2015), in situ, inside-out growth of even more compact progenitors (Oser et al. 2010; Johansson et al. 2012; Nelson et al. 2014; Williams et al. 2014; Wellons et al. 2015), “compaction” of the gas in star-forming galaxies due to disk instabilities (Dekel & Burkert 2014), and hybrid models that include several of these effects (Zolotov et al. 2015).

Although individual massive galaxies likely have complex formation histories, including periods of compaction, mergers, and star bursts, the _population_ of massive galaxies should follow a particular track in the size–mass plane that is determined by the dominant mode of growth when the evolution of many galaxies is averaged. Tracks derived from observations and simulations are shown in Figure 22. The blue and red tracks show the evolution of galaxies matched by their cumulative number density, for (relatively) low mass galaxies (van Dokkum et al. 2013, blue) and high mass galaxies (Patel et al. 2013, red). The solid parts of the curves are for $1.5 < z < 3$ and the dotted parts are for $0 < z < 1.5$. Low mass galaxies evolve along a single track with a slope of $\sim 0.3$. High mass galaxies evolve along a similar track from $z \sim 3$ to $z \sim 1.5$ but then turn “upward,” around the time when star
formation ceases and the growth becomes dominated by dry mergers (see Section 9.1).

Magenta, orange, and black curves are from simulations. The magenta tracks are the wind models shown in Figure 10 of Hirschmann et al. (2013), for two different mass ranges. These models are the same as those in Genel et al. (2012), and are updated versions of the momentum-driven wind models of Oppenheimer & Davé (2006) in cosmological simulations. They include both winds and metal enrichment; as shown in Hirschmann et al. (2013) models without winds predict somewhat steeper relations between size growth and mass growth. The orange curve is the track of galaxies in the Illustris project (Vogelsberger et al. 2014), as shown in Figure 5 of Wellons et al. (2015). This is the average track of all galaxies with a stellar mass in the range \((1-3) \times 10^{11} M_\odot\) at \(z = 2\). The thin black curves show the evolution from \(z = 3\) to \(z = 1.5\) of individual galaxies in the simulations of Zolotov et al. (2015). We include all 34 simulations, irrespective of whether they have a “compaction” phase. The thick dashed curve was created by averaging the evolution in these simulations. The number density-matched observational samples and the simulations all suggest that the ensemble-averaged evolution of star-forming galaxies in the size–mass plane is well approximated by

\[
\Delta \log r_e = 0.3 \Delta \log M_{\text{stars}},
\]

that is, galaxies increase their size by a factor of 2 for every factor of 10 evolution in their mass. This simple inside-out growth model is qualitatively consistent with a host of other data and theory, including the expected growth of disks in

\[\sigma_{\text{core}} [\text{km s}^{-1}]\]

\[P_0 (\text{quenching probability})\]

\[
\log M_{\text{stars}} - \log r_e [M_\odot \text{kpc}^{-1}]\]

\[\rho_0 (\text{quenching probability})\]

Figure 22. Tracks of galaxies in the size–mass plane in different studies. The solid blue and red curves show the evolution from \(z \sim 3\) to \(z = 1.5\) of number density-matched samples of low mass (van Dokkum et al. 2013) and high mass (Patel et al. 2015) galaxies. Broken curves show the evolution at \(z < 1.5\). Magenta tracks are the wind models of Hirschmann et al. (2013), for two different mass ranges and \(1.5 < z < 2.5\). The orange curve is the evolution of the full sample of massive Illustris galaxies from \(z = 3\) to \(z = 1.5\) in Wellons et al. (2015). Thin black curves are individual simulated galaxies in Zolotov et al. (2015), from \(z = 3\) to \(z = 1.5\). The mean Zolotov evolution is indicated by the thick black dashes. The green arrow is a good match to the mean growth of galaxies in all these studies: \(\Delta \log r_e \sim 0.3 \Delta \log M_{\text{stars}}\).

Figure 23. Parameterization of quenching. No galaxies with low velocity dispersions are quenched, and all galaxies with high velocity dispersions are quenched. The quenching probability begins to increase at \(\log M_{\text{stars}} - \log r_e = 10.6\). This threshold is held fixed in this paper, but is in fact redshift dependent.

\[P_q = 0 \quad (x < 10.6)\]

\[= \frac{x - 10.6}{0.3} \quad (10.6 \leq x \leq 10.9)\]

\[= 1 \quad (x > 10.9),\]

with \(x \equiv \log M_{\text{stars}} - \log r_e\) (see Figure 23). Galaxies begin to quench at \(\log M_{\text{stars}} - \log r_e > 10.6\), or \(\sigma_q = 225 \text{ km s}^{-1}\) (Equation (5)). As we show below this particular choice of \(\sigma_q\) provides a reasonably good fit to the data over the redshift range \(1.5 < z < 3.0\). We use a single value in this paper, but we note that the threshold is a function of redshift: low redshift galaxies quench at a lower density or dispersion than high redshift galaxies (Franx et al. 2008).

The average mass growth of the population is assumed to be a simple function of the SFR, modified by the quenching
the number of galaxies and the color indicating the fraction of quiescent galaxies along with possible effects of mergers, and the well-documented offset from the sequence.

Figure 24: Illustration of the “parallel track” model of massive galaxy evolution. The blue and red squares show the distribution of galaxies in the size–mass plane at 1.5 < z < 2.25, with the size of the square proportional to the number of galaxies and the color indicating the fraction of quiescent galaxies. Galaxies move along parallel tracks in the size–mass plane, with ∆ log r_e ∼ 0.3∆ log M_{stars}, until they cross the yellow quenching line of constant σ_y ∼ 225 km s^{-1}.

The parameter β encompasses mass loss due to stellar winds, possible effects of mergers, and the well-documented offset between the evolution of the star-forming sequence and the evolution of the stellar mass function (see Leja et al. 2015; Papovich et al. 2015, and references therein). We adopt β = 0.45; values of 0.4 < β < 0.5 produce very similar results. A pure mass loss model would have β = w ≈ 0.6 for a Chabrier (2003) IMF. The SFR is given by the star-forming “main sequence.” We adopt the mass-dependent parameterization of Whitaker et al. (2014):

\[ \Delta \log M_{\text{stars}} = \beta \Delta t \times \text{SFR} \times \left(1 - P_e\right). \]  (32)

The observed distribution of galaxies at 1.5 < z < 2.25 is shown in Figure 25(c). In panel (d) this observed distribution is multiplied by a weight mask, to account for the artificial fall-off at low masses in panel (b). The weight mask was constructed by evolving a galaxy population with a uniform density distribution in the size–mass plane and a cutoff at M_{stars} < 10^{10}M_\odot forward in time (in the same way as described above). The distribution in Figure 25(d) is remarkably similar to that in Figure 25(b). Furthermore, the total number density of galaxies in the two panels is almost identical; panel (d) has 7% less galaxies than panel (b).

In Figure 26 the color-coding reflects the SSFRs of the galaxies, with redder squares indicating a lower SSFR. The figure looks very similar when the fraction of quiescent galaxies is used for the color coding instead of the SSFR. The sizes of the squares are proportional to the number of galaxies. The model naturally produces a population of quiescent galaxies with M_{stars} ∼ 10^{11}M_\odot and r_e ∼ 1 kpc. In our model, the progenitors of these galaxies have masses of ∼3 × 10^{10}M_\odot and sizes of ∼0.7 kpc at z ∼ 3. The model does not produce the right fraction of quiescent galaxies at the highest masses and largest sizes: many of these galaxies are forming stars at z ∼ 1.9 even though they have high galaxy-averaged velocity dispersions. This suggests that our quenching prescription is too simplistic in this regime (see Section 8.3).

We compare the predicted to the observed number densities explicitly in Figure 27. This figure highlights the excellent match of our model to the size distribution of all galaxies over the entire mass range 10.5 < log M_{stars} < 11.5: it not only reproduces the peak in the distribution at r_e ∼ 2.5 kpc but also the “shoulder” of compact quiescent galaxies. It also demonstrates that the modeling of quenching is too simplistic for large galaxies, as was already clear from the comparison of panels (b) and (d) of Figure 26. In particular, nearly 100% of galaxies with r_e > 2 kpc are forming stars in the model, whereas the observed star-forming fraction is only ∼85%.

We test the model in the following way. We first quantify the distribution of galaxies in the size–mass plane at 2.25 < z < 3.0, by measuring the number of galaxies in bins of 0.1 dex × 0.1 dex (see Figure 25(a)). Next, we evolve this distribution forward in time, using timesteps of δt = 100 Myr. For each combination of (M_{stars}, r_e) we can calculate the SFR from Equation (33), P_e from Equation (31), the change in mass from Equation (32), and the corresponding change in size from Equation (30).

The evolved distribution after 10 timesteps (i.e., 1 Gyr) is shown in Figure 25(b), with a small (4%) correction to account for the volume difference between 2.25 < z < 3.0 and 1.50 < z < 2.25. As expected, the galaxies have shifted to larger masses and to slightly larger radii in the size–mass plane. The distribution artificially falls off at low masses due to the M_{stars} = 10^{10}M_\odot limit in Figure 25(a). This limit was chosen to ensure that the galaxies with the lowest masses and highest redshifts have robust size measurements: the median brightness of the 28 galaxies with 10.0 < log M_{stars} < 10.1 and 2.9 < z < 3.0 is (H_{160}) = 23.9, well within the regime where size measurements are reliable (see van der Wel et al. 2014b).
In summary, we have shown that the population of CMGs at $z \sim 2$ can be explained by a model in which galaxies form stars at a rate that is dictated by the star-forming sequence, experience a modest increase in size for a given increase in mass, and quench after passing a velocity dispersion threshold. This was demonstrated by evolving the observed galaxy population at $z \sim 2.6$ forward by 1 Gyr to $1.50 < z < 2.25$. Panel (b) shows the observed number density of galaxies at $1.50 < z < 2.25$. Panel (d) is identical to panel (c), but is weighted to account for the edge effect at low masses in the model prediction of panel (b). The distribution of galaxies in panel (d) is remarkably similar to that in panel (b), demonstrating that compact massive galaxies at $z \sim 2$ can be formed by simple mass growth of galaxies at higher redshift.

8.3. Summary of the Modeling

In summary, we have shown that the population of CMGs at $z \sim 2$ can be explained by a model in which galaxies form stars at a rate that is dictated by the star-forming sequence, experience a modest increase in size for a given increase in mass, and quench after passing a velocity dispersion threshold. This was demonstrated by evolving the observed galaxy population at $z \sim 2.6$ forward by 1 Gyr to $z \sim 1.9$. This is a critical period, as the number density of qCMGs increases by an order of magnitude over that redshift range.

Although it is beyond the scope of this paper, we note that the modeling can easily be extended. In particular, it would be straightforward to fit for the two tunable parameters (the quenching dispersion $\sigma_q$ and the parameter $\beta$, which relates the mass growth to the SFR). Furthermore, our quenching description is inadequate in the high mass/large size regime; the yellow line in Figure 24 is somewhat too steep. A possible explanation is that quenching depends on the galaxy properties in the central $\sim 1$ kpc, and the simple $M_{\text{stars}}/r_e$ criterion no longer “works” in a regime where $r_e \gg 1$ kpc. Some evidence for this comes from a study of the mass in the central $r_{3D} < 1$ kpc of galaxies (van Dokkum et al. 2014); as we showed in Figure 9 of that paper the mass inside of 1 kpc is an excellent predictor of quiescence at all redshifts. Finally, the modeling can be extended to lower redshifts, taking evolution in $\sigma_q$ into account (see Section 9.1).
9. DISCUSSION

9.1. The Formation of Today’s Massive Galaxies

In the preceding sections we discussed a simple model for the evolution of massive galaxies at $2 < z < 3$: they grow inside-out with $\Delta \log r_e \sim 0.3 \Delta \log M_{\text{stars}}$ (Equation (30)) while they are forming stars, and quench when they reach a density or velocity dispersion threshold. This model provides an explanation for the fact that large galaxies have younger stellar populations than small galaxies at fixed mass (e.g., Franx et al. 2008), as only the smallest galaxies have reached the quenching threshold. Galaxies enter the massive, compact selection region in the size–mass plane “from the left,” that is, by increasing their masses. This seems different from models in which large, massive galaxies enter this region “from above,” that is, by decreasing their sizes through mergers (e.g., Hopkins et al. 2009b) or by gas “compaction” followed by star formation (Dekel & Burkert 2014). This apparent difference may reflect a difference in approach: in this paper we are concerned with the average evolution of the population of massive galaxies, whereas simulations such as those of Zolotov et al. (2015) are able to follow the tracks of individual galaxies in the size–mass plane. Judging from the Zolotov et al. (2015) tracks, Equation (30) may simply be the time- and population average of periods of proportional size and mass growth ($\Delta \log r_e \sim \Delta \log M_{\text{stars}}$), periods of compaction, and the effects of mergers.25

At lower redshifts massive galaxies evolve along a markedly different track in the size–mass plane: van Dokkum et al. (2010), Patel et al. (2013), and others find that the size and mass evolution of massive galaxies are related through $\Delta \log r_e \sim 2 \Delta \log M_{\text{stars}}$ at $0 < z < 2$ (as indicated by the dotted section of the red curve in Figure 22). This evolution can be explained by minor, gas-poor mergers building up the outer

25 Note that the term “compaction” refers to the gas, not the stars; in the Zolotov et al. models the (indirect) effect on the stellar effective radius is generally much smaller than that on the gas radius.
envelopes of galaxies (Bezanson et al. 2009; Naab et al. 2009; Hopkins et al. 2010; Hilz et al. 2013). In van Dokkum et al. (2010) we showed that any physical process that deposits mass at \( r > r_e \) leads to a steep track in the size–mass plane, due to the definition of the effective radius.

A schematic of the growth of massive galaxies from \( z \sim 3 \) to \( z \sim 0 \) is shown in Figure 28. After galaxies quench, their mass growth per unit time is reduced, but their effective radii continue to increase. This figure suggests that there are multiple paths leading to large, massive, quiescent galaxies in the local universe, as was also noted in, e.g., Cappellari et al. (2013) and Barro et al. (2014a). Their \( z \sim 2 \) progenitors can be large star-forming (disk) galaxies, such as those studied extensively by, e.g., Genzel et al. (2008) and Förster Schreiber et al. (2011), or compact, massive, quiescent galaxies that have grown through mergers (e.g., Trujillo et al. 2011; Patel et al. 2013; Ownsworth et al. 2014). As shown in Figure 2 of van Dokkum et al. (2014) massive \( z = 0 \) galaxies have a large range of central densities at fixed total mass, as expected in such scenarios. It is possible that massive S0 galaxies formed from large star-forming galaxies and massive elliptical galaxies formed from compact star-forming galaxies, although it remains to be seen whether the stellar populations of massive early-type galaxies are sufficiently diverse to accommodate a large range in formation histories (Gallazzi et al. 2005; van Dokkum & van der Marel 2007).

In this paper we mostly ignored the effects of AGN, despite the fact that nearly half of the 25 galaxies with Keck spectra have X-ray luminosities above the canonical AGN limit of \( L_X > 10^{43} \text{ erg s}^{-1} \). The reason is that these effects are difficult to constrain and quantify. Barro et al. (2013) discuss the high occurrence rate of AGN in compact star-forming galaxies extensively, and argue that they are the agent of quenching. This may be true: in many galaxy formation models AGNs play a crucial role in quenching star formation precisely in this mass and redshift range (e.g., Croton et al. 2006; Hopkins et al. 2008). However, the SFRs of the sCMGs are (still) high and consistent with the \( z \sim 2.3 \) star-forming sequence (Whitaker et al. 2014), and there is no evidence for a direct effect of the AGNs on star formation. Turning this around, it is obviously the case that the black holes are growing in these galaxies, and that they are growing at a time when the dense stellar centers are also growing. This is not surprising, as it is difficult to see how to avoid a high accretion rate onto the central object in these extremely dense, highly star-forming galaxies.

An obvious point of concern is that the presence of AGNs causes errors in the derived physical parameters of the galaxies. In principle, an AGN in a relatively low mass, relatively large, and relatively quiescent galaxy could push the galaxy in the sCMG category: the extra light of the AGN could be mistaken for star light, increasing the mass; the combination of a point source with a normal galaxy could be mistaken for a compact bulge-dominated object; and the hot IR flux from the AGN could be mistaken for polycyclic aromatic hydrocarbon features from star formation. This can only be addressed properly with data of much higher spatial resolution than are available today, but we

\[ 26 \text{ The number of galaxies with active nuclei could be even higher, as the X-ray selection is biased against Compton-thick AGN (see, e.g., Fiore et al. 2008).} \]
note here that the galaxies with AGNs do not stand out in any of the figures. The only exception is that the four galaxies with the highest measured velocity dispersions all have X-ray AGNs, and also [N II]/Hα ratios of ~1. We have treated these four galaxies in the same way as the others.

A related issue is the almost-certain presence of galactic-scale winds and outflows. Such winds can be driven by star formation (e.g., Heckman et al. 1987) and/or AGNs (e.g., Proga et al. 2000) and are ubiquitous in star-forming galaxies at high redshifts (Franx et al. 1997; Pettini et al. 1998; Förster Schreiber et al. 2014; Genzel et al. 2014b). Galactic superwinds can create bubbles and shock fronts whose kinematics, spatial extent, and emission line ratios are very similar to what we observe. In at least one of the galaxies in our sample, COSMOS_1014, there is evidence for a broad Hα line in addition to a narrow component, similar to IRAS 11095–0238 (Soto & Martin 2012) and galaxies in Förster Schreiber et al. (2014). Furthermore, four of the galaxies in our sample are part of the sample of massive galaxies of Genzel et al. (2014b) (COSMOS_11363, GOODS-S_30274, GOODS-S_37745, and GOODS-S_45068), and they find broad nuclear velocity components in two of them (COSMOS_11363 and GOODS-S_30274). A detailed study of the kinematics and line ratios of GOODS-S_30274 was also done by van Dokkum et al. (2005).

Although winds are almost certainly present, two results suggest that they are not dominating the galaxy-integrated emission line widths. First, winds tend to escape in a direction perpendicular to the plane of the galaxy (Heckman et al. 1990), which is difficult to reconcile with the observed anti-correlation between velocity dispersion and axis ratio (Figure 12). Second, the observed kinematics are fully explained by the stellar mass, leaving little room for additional broadening due to winds. In fact, broad components in the velocity profiles are expected just from rotating gas at small radii: as shown in Figure 18 gas at ~1 kpc should have FWHM ≈ 1000 km s⁻¹ even in the absence of winds. Judging from other z ~ 2 galaxies the disks are also likely to be highly turbulent, with a relatively high internal dispersion (see, e.g., Cresci et al. 2009; Förster Schreiber et al. 2009). The gaseous environments of sCMGs may be similar to those of ULIRGs, which are highly complex: as shown in Soto & Martin (2012) they can have rotating, large-scale disks in addition to outflows and shocks.

Finally, we note that the presence of spatially extended gas disks in these galaxies had been predicted by Zolotov et al. (2015). They also predicted that the gas dispersions are, on average, lower than the stellar dispersions (Figure 10(a), as the gas is in disks which are sometimes seen face-on. Interestingly, Zolotov et al. (2015) also find that the gas constitutes only a small fraction of the total baryonic mass of the simulated compact massive star-forming galaxies, although they note that this result is sensitive to the feedback prescription. Similarly, Johansson et al. (2012) predicted that CMGs are stellar mass-dominated and have Keplerian rotation curves; the model rotation curves in their Figure 7 are remarkably similar to the inferred rotation curve shown in our Figure 18.

9.3. Submillimeter Galaxies, Far-IR Selected Galaxies, and Quasars

This study begins with an HST/WFC3-selected sample in a total area of ~0.25 square degrees. Many other studies have found extreme star-forming galaxies by selecting them on the basis of their far-infrared, submillimeter, or radio emission instead (e.g., Kormendy & Sanders 1992; Sanders & Mirabel 1996; Barger et al. 1998; Smail et al. 2000; Barger et al. 2001; Casey et al. 2012). These extreme galaxies are plausible ancestors of early-type galaxies; as an example, Tacconi et al. (2008), Toft et al. (2014), and Simpson et al. (2015) have suggested that many submillimeter galaxies could be direct progenitors of compact quiescent galaxies at z ~ 2.

We do not select against such objects, and our sample should include the proper number of submillimeter galaxies, radio galaxies, and other extreme objects. However, there are (at least) two possible reasons why galaxies selected at other wavelengths could be underrepresented in our sample: some fraction may be too faint in the near-IR to be included (or to be properly characterized) in the Skelton et al. (2014) catalogs, and some may be too rare to be represented in the 3D-HST/CANDELS area. sCMGs have such high column densities in the central regions that some may be entirely obscured at rest-frame optical wavelengths (Gilli et al. 2014; Nelson et al. 2014). Wang et al. (2012) and Caputi et al. (2014) show that objects exist that are relatively bright in the IRAC bands but that are undetected in deep near-IR data. It is obviously difficult to measure the redshifts and masses of these objects with traditional means, but it may be possible using molecular lines (see Walter et al. 2012; Riechers et al. 2013). In the context of the study presented here the question is not whether any massive, compact, “optically dark” galaxies were missed, but what fraction of mass and star formation is in such objects.

The second class of potentially missed objects are extremely rare, extremely luminous galaxies. The median SFRs of sCMGs in our study is (SFR) = 134 M⊙ yr⁻¹, and we have 112 such objects at 2 < z < 5. Therefore, objects that are so rare that they are only a few (or zero) in our survey volume must have SFRs ≥ 5000 M⊙ yr⁻¹ to have a significant impact on our results. This seems extreme, but such objects probably exist: the most extreme Herschel-selected galaxies at 2 < z < 5 have estimated SFRs up to ~9000 M⊙ yr⁻¹ (Casey et al. 2012). Furthermore, recently identified highly obscured quasars have bolometric luminosities of Lbol ~ 10¹⁵ erg s⁻¹ (Banerji et al. 2012, 2015), and it seems likely that the growth of the black holes in these objects is accompanied by prodigious star formation. It remains to be seen whether such objects are sufficiently common (or rather, long-lived) to impact results derived from CANDELS-sized areas.

Finally, we note that we do not find a correlation between size and IR luminosity at fixed stellar mass, that is, an IR selection does not preferentially select compact galaxies but objects with a wide range of rest-frame optical sizes (see also Wiklind et al. 2014; Simpson et al. 2015). As an IR selection is effectively a star formation selection at high masses (see, e.g., Whitaker et al. 2012; Rodighiero et al. 2014), this is perhaps not surprising.

10. SUMMARY AND CONCLUSIONS

In this paper we have identified a population of star-forming CMGs in the five fields of the CANDELS and 3D-HST surveys. Such objects have been studied previously by Barro et al. (2013, 2014a, 2014b) and Nelson et al. (2014), and we build on their results. Compared to the Barro et al. studies, our selection is more restrictive, focusing only on the most massive and most compact galaxies; we study an area that is ~2.5 times larger; and our redshift catalogs make use of the 3D-HST grism spectra for all objects brighter than H₁₆₀ < 24.
We first confirm the redshifts and masses of the galaxies using Keck MOSFIRE and NIRSPEC spectroscopy of 25 compact massive star-forming galaxies at $2 < z < 2.5$. The gas dynamics suggest that the galaxies are embedded in spatially extended rotating disks; this explains the low measured dispersions of a large fraction of the sample and the observed anti-correlation between the dispersion and the axis ratio of the galaxies. Support for this interpretation comes from direct measurements of the sizes of the Hα disks for 10 galaxies; the fact that this is possible at all from ground-based, seeing-limited data already shows that the gas extends to scales $\gg 1$ kpc. The derived sizes of the gas disks, and the fall-off of the rotation curve that we construct for the galaxies, are in very good agreement with recent models for the formation of massive galaxies (Johansson et al. 2012; Zolotov et al. 2015).

It is important to note that, in our interpretation, the measured gas velocity dispersions of the galaxies generally do not reflect the true $V_{\text{rot}}$ in the stellar body. We predict that the (inclination-corrected) velocities at $r \lesssim 1$ kpc are 400–500 km s$^{-1}$ for all galaxies. This can be tested with adaptive optics-assisted observations of the Hα line. There is evidence for broad components in several of the velocity profiles (see Section 9.2), and these complex profiles may reflect the combined effect of high rotation velocities at small radii and lower velocities at larger radii. A more direct measurement could come from CO line widths, as these likely probe much smaller radii than the Hα emission (see, e.g., Downes & Solomon 1998).

Next, we interpret the existence of star-forming, compact galaxies at $2 < z < 2.5$ in the context of a simple model for the evolution of galaxies in the size–mass plane. We describe the average evolution of star-forming galaxies by the simple relation $\Delta \log r_e \sim 0.2 \Delta \log M_{\text{stars}}$, with the mass evolution proportional to the main sequence SFR. We show that this evolution is a consistent feature in galaxy formation models of Hirschmann et al. (2013), Wellons et al. (2015), and Zolotov et al. (2015), and is also seen in observations of number density-matched samples of galaxies (Patel et al. 2013; van Dokkum et al. 2013; Ownsworth et al. 2014).

As galaxies move along this track their average 3D density within $r_e$ remains approximately constant (as $\rho(r_e) \propto M / r_e^3$, it follows that $r_e \propto M^{1/3}$ if the density is constant). However, their density within a fixed physical radius increases, as does their projected (2D) density and their velocity dispersion. Following many other studies (e.g., Franx et al. 2008; Bell et al. 2012), we assume that quenching occurs when galaxies reach a threshold in either velocity dispersion or physical density. We show that this model explains the evolution of the distribution of galaxies in the size–mass plane from $z \sim 2.6$ to $z \sim 1.9$, the redshift range when the number density of massive compact quiescent galaxies increases by nearly an order of magnitude. In the context of this straightforward model, the progenitors of compact massive star-forming galaxies at $z \sim 2.5$ were simply somewhat less massive and slightly smaller galaxies at $z \gtrsim 3$.

Our study has several important systematic uncertainties. First, the stellar masses of the galaxies are derived from fitting stellar population synthesis models to the photometry, and these models have not been tested for the extreme galaxies that are under discussion in this paper. Such tests are urgently needed but they are difficult, even for quiescent galaxies and for “normal” star-forming galaxies in the local universe (Muzzin et al. 2009b; Conroy 2013). One interpretation of Figure 10(b) is that the stellar masses are off by factors up to $\sim 10$; however, as we show in the remainder of Section 5 the dynamical masses and stellar masses are consistent with each other once orientation effects and the spatial extent of the gas are taken into account. Our final dynamical result ($M_{\text{dyn}} = 0.8^{+0.6}_{-0.4} \times M_{\text{stars}}$; Section 6.4) suggests that the contributions of dark matter and gas to the mass within $\sim$7 kpc are small. We have assumed a relatively bottom-light Chabrier (2003) IMF when deriving stellar masses; if we assume a Salpeter (1955) IMF instead (see, e.g., van Dokkum & Conroy 2010; Cappellari et al. 2012; Conroy & van Dokkum 2012) we find $M_{\text{dyn}} = 0.5^{+0.4}_{-0.2} \times M_{\text{stars}}$, and even tighter constraints on the amount of gas and dark matter. We emphasize, however, that the conversion of light to stellar mass for these dusty, compact star-forming galaxies is highly uncertain. We also note here that the stellar masses are not corrected for the contribution of emission lines to the SEDs. These corrections are generally small ($\sim 10\%$).

Second, the role of winds and active nuclei in these galaxies is not well understood (Section 9.2). They almost certainly influence the measured dynamics and line ratios, but without spatially resolved data it is very difficult to disentangle the effects of winds, a falling rotation curve, and the spatial distribution of the ionized gas. Third, the fact that the galaxies are all very dusty may imply that we are missing part of the population due to selection effects (Section 9.3). We could be missing galaxies outright (see Figure 3 in Nelson et al. 2014), or they could be misclassified as less compact, lower mass galaxies if only their outer edges are detected in the currently available data. Another potential effect of the dust is that the stellar population modeling may produce incorrect stellar masses: the modeling uses a screen approximation for dust, whereas in reality the dust and stars are almost certainly mixed.

Fortunately, the prospects for addressing these uncertainties are excellent. Adaptive optics-assisted spectroscopic observations with integral field units on 8–10 m telescopes can be used to measure kinematics and line ratios on $\lesssim 1$ kpc scales (e.g., Newman et al. 2013). The morphology of the dust and molecular gas emission can be studied with interferometers such as the Very Large Array, the Plateau de Bure Interferometer, and the Atacama Large Millimeter Array (see, e.g., Simpson et al. 2015, for impressive early ALMA results on submillimeter-selected galaxies). These instruments can also measure the kinematics of the molecular gas (e.g., Tacconi et al. 2008). On a longer timescale, the James Webb Space Telescope can measure the stellar kinematics of the galaxies, as well as identify and characterize compact galaxies that are entirely obscured in the $K$ band (Wang et al. 2012). Finally, the upcoming generation of extremely large ground-based optical/near-IR telescopes is needed to spatially resolve these CMGs within their effective radius.

We thank Adi Zolotov for providing model tracks of galaxies in digital form, and Thorsten Naab and Peter Johansson for pointing us to the key figures that show model tracks in their simulations. The comments from the anonymous referee improved the manuscript, and prompted us to add the three appendices. Support from STScI grant GO-12177 is
gratefully acknowledged. The data presented here were obtained at the W. M. Keck Observatory, which is operated as a scientific partnership among the California Institute of Technology, the University of California and the National Aeronautics and Space Administration. The Observatory was made possible by the generous financial support of the W. M. Keck Foundation. The authors recognize and acknowledge the very significant cultural role and reverence that the summit of Mauna Kea has always had within the indigenous Hawaiian community. We are most fortunate to have the opportunity to conduct observations from this mountain.

**APPENDIX A**

$H_{160}$ IMAGES

In the main text we show color images of the 25 star-forming CMGs, created from the $J_{125}$ and $H_{160}$ CANDELS data (Figure 6). In Figure 29 we show the $H_{160}$ images separately, with a higher dynamic range than in Figure 6. The tidal features around GOODS-S_30274 and COSMOS_11363 are very clear, and several other galaxies also show structure at faint surface brightness. We fit all galaxies with a single Sérsic profile, which is an excellent approximation of the average surface brightness profile of the full sample (see Section 7.2); however,
it is clear that these fits do not capture the full information in the HST images.

APPENDIX B
EXPECTED AND OBSERVED UNCERTAINTIES IN THE SPECTRA

As described in Section 3.4.1 we fit Gaussian models to the emission lines. The fits are done with the *emcee* code, with the observed 1D spectrum and a noise model as inputs for each galaxy. Here we briefly analyze the residuals from these fits to determine the accuracy of the noise models.

In Figure 30 we show the spectra of the 20 galaxies that were observed by us. For convenience, the figure has the same format as Figures 5–7, and 15 in the main text, except that the five galaxies from Barro et al. (2014a) are left blank. For each galaxy, the top panel shows the spectrum and the best-fitting model; the middle panel shows the expected noise (see Sections 3.1 and 3.2); and the bottom panel shows the difference between the observed spectrum and the best-fitting model divided by the expected noise. The width of the distribution of these residuals is ~1 in nearly all cases.

**Figure 30.** Analysis of the noise in the NIRSPEC and MOSFIRE spectra. The galaxies have the same order as in Figure 5; panels for objects taken from Barro et al. (2014a) are left blank. For each galaxy, the top panel shows the spectrum and the best-fitting model; the middle panel shows the expected noise; and the bottom panel shows the difference between the observed spectrum and the best-fitting model divided by the expected noise. The width of the distribution of these residuals is ~1 in nearly all cases.
Sections 3.1 and 3.2). The bottom subpanel is the residual from the fit divided by the noise model. The residuals are well-behaved, and generally exhibit no indications of poorly subtracted sky lines or other irregularities. We quantified this by calculating the biweight scatter $\sigma_{\text{BI}}$ (see Beers et al. 1990) in the distribution of residuals. The value of $\sigma_{\text{BI}}$ deviates by more than $\sim 30\%$ from unity in only two cases, UDS_35673 and COSMOS_11363. Both galaxies have very high S/N spectra, and the higher than expected residuals are not caused by errors in the noise spectra but by the fact that the velocity distributions are not exactly Gaussian. The average scatter of the remaining 18 galaxies is $1.09$, which means that the noise models that we use are accurate to $\sim 10\%$.

APPENDIX C

CONVERTING GALAXY-AVERAGED VELOCITY DISPERSIONS TO A ROTATION CURVE

C.1 Motivation

In Section 6.4 we construct the average rotation curve for star-forming CMGs. This is done by combining information for 10 different galaxies: all galaxies have approximately the same stellar masses and $H_{160}$ half-light radii, but they have a wide range of $H_\alpha$ effective radii. For each galaxy we measure the galaxy-integrated velocity dispersion and the inclination, and convert these to an inclination-corrected rotation velocity at $r = r_{\text{gas}}$, where $r_{\text{gas}}$ is the half-light radius of the $H_\alpha$ emission. The rotation velocities of the galaxies are then plotted versus $r_{\text{gas}}$ in Figure 18, and the resulting relation is interpreted as a rotation curve.

Here we test whether this method is viable, that is, whether the actual rotation curve of a model galaxy can be reconstructed in this way. We also test whether we are using the correct conversion constant to go from a galaxy-integrated velocity dispersion to a rotation velocity at the half-light radius of $H_\alpha$. This constant, together with an inclination correction, relates the velocity dispersion $\sigma$ to the rotation velocity $V_{\text{rot}}$:

$$\alpha = \frac{\sigma_{\text{gas}}}{V_{\text{rot}} \sin^{-1}(i)}$$

(see Equations (17) and (19)). In the main text we use $\alpha = 0.8 \pm 0.2$, based on previous studies (see Section 5.1). However, these studies did not consider the specific model of a compact,
A $r^{1/4}$-law mass distribution combined with an extended, exponential gas distribution.

C.2 Modeling Velocity Profiles

We simulated the observations in the following way. We constructed a model mass distribution that follows a Sérsic surface density profile. This mass distribution is characterized by three parameters: the Sérsic index $n$, the effective radius $r_{\text{mass}}$ (this parameter is equivalent to both $r_{\text{stars}}$ and $r_e$ in the main text), and the total mass $M$. We fixed $r_{\text{mass}} = 1$ kpc and $M = 1.0 \times 10^{11} M_\odot$, and for the initial model we set $n = 4$. Apart from a slight rescaling of the effective radius, this model closely matches the actual average stellar mass distribution of the sCMGs, if mass traces the $H_{160}$ light. The model is shown in Figure 31(a) by the gray line.

Next, we constructed 10 model galaxies, each with the same mass distribution but with different distributions of the Hα emission. The ionized gas is in thin exponential disks, with effective radii ranging from $r_{\text{H\alpha}} = 0.5$ kpc (and hence $r_{\text{H\alpha}} = 0.5 r_{\text{mass}}$) to $r_{\text{H\alpha}} = 5$ kpc. Four of these model gas distributions are shown by the black lines in Figure 31(a). The gas disks mimic the derived extended ionized gas of sCMGs, with $r_{\text{H\alpha}}$ equivalent to the parameter $r_{\text{gas}}$ in the main text. Galaxy-integrated velocity profiles were created by integrating the projected velocities along the line of sight and over the full spatial extent of the model galaxies. The velocities were calculated from the mass profile shown in Figure 31(a) and weighted by the Hα flux. In order to model the observed profiles as closely as possible, we used an inclination of 60° (where 90° is edge-on) and an instrumental resolution of 60 km s$^{-1}$ (in between the MOSFIRE and NIRSPEC resolution).

The velocity profiles of the four model galaxies are shown in panels (c)–(f) of Figure 31. As expected they have the classic “double-horned” form that is characteristic of rotating disks. The profile is not the same for all four models even though the mass distribution, and hence the underlying velocity field, is identical in all cases. The more extended the Hα distribution is with respect to the mass, the narrower the profile becomes, and the more closely it resembles a Gaussian. The reason for this behavior is that the Hα emission is more weighted toward larger radii, where the rotation velocity is lower. Velocities in excess of $\sim 350$ km s$^{-1}$ are still sampled, but they have relatively low weight and are responsible for the high velocity tails of the profile.

C.3 Relation between Global Dispersion and Rotation Velocity at $r = r_{\text{H\alpha}}$

We fitted Gaussian models to the line profiles, just as we do in the data analysis described in the main text. These Gaussian fits are shown by the red curves in panels (c)–(f) of Figure 31. The width of these Gaussians decreases with increasing $r_{\text{H\alpha}}/r_{\text{mass}}$, as discussed above. We note here that the actual profile shape is not very well approximated by a Gaussian, particularly in panels (c) and (d). Interestingly, we see hints of double-horned profiles in the data for some of the galaxies (e.g., UDS_16442 and, particularly, GOODS-N_774, which was published in Nelson et al. 2014), although the S/N is not high enough to quantify this.

In Figure 32(a) these measured galaxy-integrated velocity dispersions are plotted versus the half-light radii of the Hα disks, after correcting for inclination and instrumental broadening (open squares). All ten galaxy models are shown, with Hα effective radii ranging from $0.5 \times r_{\text{mass}}$ to $5 \times r_{\text{mass}}$. For comparison, the black curve shows the actual rotation curve of the galaxies. The squares show the same fall-off as the actual rotation curve, with a roughly constant multiplicative offset. The solid squares are obtained by dividing the measured dispersions by 0.8, which is the value of $\alpha = \sigma/V_{\text{rot}}$ that we used in the analysis of Section 6.4. They are in almost perfect agreement with the black curve, demonstrating that it is

---

**Figure 32.** (a) Rotation curve of the model in Figure 31 (black line), compared to the inclination-corrected, galaxy-integrated velocity dispersion $\sigma$ for 10 different Hα distributions (open red squares). The half-light radius of the Hα emission ranges from $0.5 \times r_{\text{mass}}$ to $5 \times r_{\text{mass}}$. Solid red squares are corrected for the parameter $\alpha = \sigma/V_{\text{rot}} = 0.8$. (b) Derived values of $\alpha$ from our model (black lines). The value $\alpha = 0.8 \pm 0.2$ that is used in the main text is shown by the orange line. Different line types indicate results for different Sérsic indices $n$ of the mass distribution; the value of $\alpha$ is nearly independent of $n$.!
possible to reconstruct the average rotation curve of sCMGs with our method.

The analysis is generalized in Figure 3(b), where we show the value of $\alpha$ as a function of the ratio of the effective radius of $H_0$ and the effective radius of the mass. We repeated the analysis for different assumed mass profiles, ranging from exponential ($n = 1$; dotted) to an $r^{1/4}$ law ($n = 4$; solid). The ratio between dispersion and rotation velocity at $r = r_{\text{H}_0}/r_{\text{mass}}$ is remarkably constant: it does not vary appreciably either with $r$ or with $n$. We conclude that the assumed value of $\alpha = 0.8 \pm 0.2$ is reasonable for the mass and $H_0$ profiles discussed in this paper.

REFERENCES


Bersier, D., and the Effective Radius of the Mass. We repeated the analysis for different assumed mass profiles, ranging from exponential ($n = 1$; dotted) to an $r^{1/4}$ law ($n = 4$; solid). The ratio between dispersion and rotation velocity at $r = r_{\text{H}_0}/r_{\text{mass}}$ is remarkably constant: it does not vary appreciably either with $r$ or with $n$. We conclude that the assumed value of $\alpha = 0.8 \pm 0.2$ is reasonable for the mass and $H_0$ profiles discussed in this paper.

REFERENCES


Bersier, D., and the Effective Radius of the Mass. We repeated the analysis for different assumed mass profiles, ranging from exponential ($n = 1$; dotted) to an $r^{1/4}$ law ($n = 4$; solid). The ratio between dispersion and rotation velocity at $r = r_{\text{H}_0}/r_{\text{mass}}$ is remarkably constant: it does not vary appreciably either with $r$ or with $n$. We conclude that the assumed value of $\alpha = 0.8 \pm 0.2$ is reasonable for the mass and $H_0$ profiles discussed in this paper.

REFERENCES


Bersier, D., and the Effective Radius of the Mass. We repeated the analysis for different assumed mass profiles, ranging from exponential ($n = 1$; dotted) to an $r^{1/4}$ law ($n = 4$; solid). The ratio between dispersion and rotation velocity at $r = r_{\text{H}_0}/r_{\text{mass}}$ is remarkably constant: it does not vary appreciably either with $r$ or with $n$. We conclude that the assumed value of $\alpha = 0.8 \pm 0.2$ is reasonable for the mass and $H_0$ profiles discussed in this paper.

REFERENCES


Bersier, D., and the Effective Radius of the Mass. We repeated the analysis for different assumed mass profiles, ranging from exponential ($n = 1$; dotted) to an $r^{1/4}$ law ($n = 4$; solid). The ratio between dispersion and rotation velocity at $r = r_{\text{H}_0}/r_{\text{mass}}$ is remarkably constant: it does not vary appreciably either with $r$ or with $n$. We conclude that the assumed value of $\alpha = 0.8 \pm 0.2$ is reasonable for the mass and $H_0$ profiles discussed in this paper.

REFERENCES


Bersier, D., and the Effective Radius of the Mass. We repeated the analysis for different assumed mass profiles, ranging from exponential ($n = 1$; dotted) to an $r^{1/4}$ law ($n = 4$; solid). The ratio between dispersion and rotation velocity at $r = r_{\text{H}_0}/r_{\text{mass}}$ is remarkably constant: it does not vary appreciably either with $r$ or with $n$. We conclude that the assumed value of $\alpha = 0.8 \pm 0.2$ is reasonable for the mass and $H_0$ profiles discussed in this paper.

REFERENCES


Bersier, D., and the Effective Radius of the Mass. We repeated the analysis for different assumed mass profiles, ranging from exponential ($n = 1$; dotted) to an $r^{1/4}$ law ($n = 4$; solid). The ratio between dispersion and rotation velocity at $r = r_{\text{H}_0}/r_{\text{mass}}$ is remarkably constant: it does not vary appreciably either with $r$ or with $n$. We conclude that the assumed value of $\alpha = 0.8 \pm 0.2$ is reasonable for the mass and $H_0$ profiles discussed in this paper.