Polymorphism of the azobenzene dye compound methyl yellow†

Dyanne L. Cruickshank,*a Christopher H. Hendon,*b Matthew J. R. Verbeek,a Aron Walshc and Chick C. Wilsoncd

The crystal structure and polymorphism of the well-known aminoazobenzene, N,N-dimethyl-4-aminoazobenzene (DAB) are studied; a second polymorph of DAB reported and the relationship between the two polymorphs studied using differential scanning calorimetry and by evaluating their lattice energies and absorption spectra. Without significantly strong intermolecular interactions present in the two forms of DAB, a balance between conformational strain and a cumulative π-orbital overlapping effect results in the existence of the enantiotropically related polymorphs and their alternative packing arrangements. The UV/vis spectra of the two polymorphs are different, thus illustrating the significance of small structural changes on the colour of a material, which could behave differently under particular sensing conditions. DAB has been used primarily as an acid/base indicator solution and a dye molecule and the implications of the polymorphic relationships established here are discussed with respect to the range of applications this molecule finds as a sensor and for its incorporation into various functional films and devices.

1. Introduction

Molecules containing an azo chromophore have a long-standing reputation as excellent dyes. \((E)-N,N\)-Dimethyl-4-aminoazobenzene (DAB) more commonly known as methyl yellow, is one of the most successful azo dyes that found a wide range of applications initially, especially in the food and textile industries.1 After being reported as a carcinogen in the mid-1900's2 and discontinued as a food additive, DAB found standing reputation as excellent dyes. (E)-N,N-Dimethyl-4-aminoazobenzene (DAB) are studied; a second polymorph of DAB reported and the relationship between the two polymorphs studied using differential scanning calorimetry and by evaluating their lattice energies and absorption spectra. Without significantly strong intermolecular interactions present in the two forms of DAB, a balance between conformational strain and a cumulative π-orbital overlapping effect results in the existence of the enantiotropically related polymorphs and their alternative packing arrangements. The UV/vis spectra of the two polymorphs are different, thus illustrating the significance of small structural changes on the colour of a material, which could behave differently under particular sensing conditions. DAB has been used primarily as an acid/base indicator solution and a dye molecule and the implications of the polymorphic relationships established here are discussed with respect to the range of applications this molecule finds as a sensor and for its incorporation into various functional films and devices.

1. Introduction

Molecules containing an azo chromophore have a long-standing reputation as excellent dyes. \((E)-N,N\)-Dimethyl-4-aminoazobenzene (DAB) more commonly known as methyl yellow, is one of the most successful azo dyes that found a wide range of applications initially, especially in the food and textile industries.1 After being reported as a carcinogen in the mid-1900's2 and discontinued as a food additive, DAB found standing reputation as excellent dyes. (E)-N,N-Dimethyl-4-aminoazobenzene (DAB) are studied; a second polymorph of DAB reported and the relationship between the two polymorphs studied using differential scanning calorimetry and by evaluating their lattice energies and absorption spectra. Without significantly strong intermolecular interactions present in the two forms of DAB, a balance between conformational strain and a cumulative π-orbital overlapping effect results in the existence of the enantiotropically related polymorphs and their alternative packing arrangements. The UV/vis spectra of the two polymorphs are different, thus illustrating the significance of small structural changes on the colour of a material, which could behave differently under particular sensing conditions. DAB has been used primarily as an acid/base indicator solution and a dye molecule and the implications of the polymorphic relationships established here are discussed with respect to the range of applications this molecule finds as a sensor and for its incorporation into various functional films and devices.

1. Introduction

Molecules containing an azo chromophore have a long-standing reputation as excellent dyes. \((E)-N,N\)-Dimethyl-4-aminoazobenzene (DAB) more commonly known as methyl yellow, is one of the most successful azo dyes that found a wide range of applications initially, especially in the food and textile industries.1 After being reported as a carcinogen in the mid-1900's2 and discontinued as a food additive, DAB found standing reputation as excellent dyes. (E)-N,N-Dimethyl-4-aminoazobenzene (DAB) are studied; a second polymorph of DAB reported and the relationship between the two polymorphs studied using differential scanning calorimetry and by evaluating their lattice energies and absorption spectra. Without significantly strong intermolecular interactions present in the two forms of DAB, a balance between conformational strain and a cumulative π-orbital overlapping effect results in the existence of the enantiotropically related polymorphs and their alternative packing arrangements. The UV/vis spectra of the two polymorphs are different, thus illustrating the significance of small structural changes on the colour of a material, which could behave differently under particular sensing conditions. DAB has been used primarily as an acid/base indicator solution and a dye molecule and the implications of the polymorphic relationships established here are discussed with respect to the range of applications this molecule finds as a sensor and for its incorporation into various functional films and devices.

1. Introduction

Molecules containing an azo chromophore have a long-standing reputation as excellent dyes. \((E)-N,N\)-Dimethyl-4-aminoazobenzene (DAB) more commonly known as methyl yellow, is one of the most successful azo dyes that found a wide range of applications initially, especially in the food and textile industries.1 After being reported as a carcinogen in the mid-1900's2 and discontinued as a food additive, DAB found standing reputation as excellent dyes. (E)-N,N-Dimethyl-4-aminoazobenzene (DAB) are studied; a second polymorph of DAB reported and the relationship between the two polymorphs studied using differential scanning calorimetry and by evaluating their lattice energies and absorption spectra. Without significantly strong intermolecular interactions present in the two forms of DAB, a balance between conformational strain and a cumulative π-orbital overlapping effect results in the existence of the enantiotropically related polymorphs and their alternative packing arrangements. The UV/vis spectra of the two polymorphs are different, thus illustrating the significance of small structural changes on the colour of a material, which could behave differently under particular sensing conditions. DAB has been used primarily as an acid/base indicator solution and a dye molecule and the implications of the polymorphic relationships established here are discussed with respect to the range of applications this molecule finds as a sensor and for its incorporation into various functional films and devices.

1. Introduction

Molecules containing an azo chromophore have a long-standing reputation as excellent dyes. \((E)-N,N\)-Dimethyl-4-aminoazobenzene (DAB) more commonly known as methyl yellow, is one of the most successful azo dyes that found a wide range of applications initially, especially in the food and textile industries.1 After being reported as a carcinogen in the mid-1900's2 and discontinued as a food additive, DAB found standing reputation as excellent dyes. (E)-N,N-Dimethyl-4-aminoazobenzene (DAB) are studied; a second polymorph of DAB reported and the relationship between the two polymorphs studied using differential scanning calorimetry and by evaluating their lattice energies and absorption spectra. Without significantly strong intermolecular interactions present in the two forms of DAB, a balance between conformational strain and a cumulative π-orbital overlapping effect results in the existence of the enantiotropically related polymorphs and their alternative packing arrangements. The UV/vis spectra of the two polymorphs are different, thus illustrating the significance of small structural changes on the colour of a material, which could behave differently under particular sensing conditions. DAB has been used primarily as an acid/base indicator solution and a dye molecule and the implications of the polymorphic relationships established here are discussed with respect to the range of applications this molecule finds as a sensor and for its incorporation into various functional films and devices.

1. Introduction

Molecules containing an azo chromophore have a long-standing reputation as excellent dyes. \((E)-N,N\)-Dimethyl-4-aminoazobenzene (DAB) more commonly known as methyl yellow, is one of the most successful azo dyes that found a wide range of applications initially, especially in the food and textile industries.1 After being reported as a carcinogen in the mid-1900's2 and discontinued as a food additive, DAB found standing reputation as excellent dyes. (E)-N,N-Dimethyl-4-aminoazobenzene (DAB) are studied; a second polymorph of DAB reported and the relationship between the two polymorphs studied using differential scanning calorimetry and by evaluating their lattice energies and absorption spectra. Without significantly strong intermolecular interactions present in the two forms of DAB, a balance between conformational strain and a cumulative π-orbital overlapping effect results in the existence of the enantiotropically related polymorphs and their alternative packing arrangements. The UV/vis spectra of the two polymorphs are different, thus illustrating the significance of small structural changes on the colour of a material, which could behave differently under particular sensing conditions. DAB has been used primarily as an acid/base indicator solution and a dye molecule and the implications of the polymorphic relationships established here are discussed with respect to the range of applications this molecule finds as a sensor and for its incorporation into various functional films and devices.

1. Introduction

Molecules containing an azo chromophore have a long-standing reputation as excellent dyes. \((E)-N,N\)-Dimethyl-4-aminoazobenzene (DAB) more commonly known as methyl yellow, is one of the most successful azo dyes that found a wide range of applications initially, especially in the food and textile industries.1 After being reported as a carcinogen in the mid-1900's2 and discontinued as a food additive, DAB found standing reputation as excellent dyes. (E)-N,N-Dimethyl-4-aminoazobenzene (DAB) are studied; a second polymorph of DAB reported and the relationship between the two polymorphs studied using differential scanning calorimetry and by evaluating their lattice energies and absorption spectra. Without significantly strong intermolecular interactions present in the two forms of DAB, a balance between conformational strain and a cumulative π-orbital overlapping effect results in the existence of the enantiotropically related polymorphs and their alternative packing arrangements. The UV/vis spectra of the two polymorphs are different, thus illustrating the significance of small structural changes on the colour of a material, which could behave differently under particular sensing conditions. DAB has been used primarily as an acid/base indicator solution and a dye molecule and the implications of the polymorphic relationships established here are discussed with respect to the range of applications this molecule finds as a sensor and for its incorporation into various functional films and devices.
metastable, despite each DAB molecule occupying the more favourable planar molecular geometry. We can attribute the increase in stability of DAB form II to better π-orbital overlapping effects and thus we are able to present both a novel polymorph of DAB and an energetic basis for its formation. We anticipate that the results presented here may be used when rationalising and designing future materials that contain DAB as a key sensor molecule.

2. Experimental

2.1 Materials and preparation of polymorphs

DAB was purchased from Sigma Aldrich on two separate occasions (batch numbers 077K1187 and BCBM8998V). Solvent grade ethanol and acetonitrile were used for the recrystallisation of DAB form I and II respectively.

2.2 Characterisation methods

Single crystal X-ray diffraction. X-ray diffraction data for form II of DAB were collected on an Agilent Gemini A-Ultra X-ray diffractometer using MoKα (\(\lambda = 0.71069 \text{ Å}\)) radiation. The crystal was cooled to 150 (2) K using an Agilent Cryojet. The redetermination of the X-ray crystal structure of DAB was carried out using a Mettler Toledo FP82 hot stage equipped with a Leica DM1000 microscope. Both crystals were subjected to a programmed temperature regime using the FP90 Central Processor. The crystals were filtered using an Infinity 2 microscopy camera.

DFT calculations. All solid-state calculations were performed within the Kohn–Sham DFT construct as implemented in the Vienna \textit{ab initio} simulation package (VASP).\textsuperscript{15} Starting with the experimentally determined crystal structures, the lattice parameters and atomic positions were allowed to relax to their equilibrium geometries using the PBEsol functional,\textsuperscript{16–18} a 500 eV plane wave cutoff and a 4 \(\times\) 4 \(\times\) 2 k-point grid for form I and form II, respectively. These parameters converged the total energy to within 0.001 eV per atom and the lattice parameters within 0.1\% of the experimentally determined values. The hybrid HSE06 screened-exchange functional\textsuperscript{19} was then used to recover more accurate electronic properties, including the prediction of the UV-vis absorption spectra within the single-particle approximation. The same basis set and k-grid were used in these calculations. In principle other hybrid functionals could also be employed (\textit{i.e.} PBE0\textsuperscript{20} or B3LYP\textsuperscript{21}) to examine similar problems. We have elected to use the same functional as the entirety of our previous work,\textsuperscript{22,23} as HSE06 performs reliably over a broad range of chemical functionalities.

3. Results and discussion

3.1 Polymorph discovery

DAB was purchased from Sigma Aldrich on two separate occasions (the as-purchased PXRD patterns are shown in Fig. 1). The calculated PXRD pattern for form I, the only reported crystal structure, did not show perfect agreement with PXRD patterns of the samples as purchased, from which it was clear that there were at least two crystalline phases in the samples. Through targeted growth of form I and the solid form that emerged as the new form II, we were able to

<table>
<thead>
<tr>
<th>C_{14}H_{15}N_{3} (DAB)</th>
<th>Form I</th>
<th>Form II</th>
</tr>
</thead>
<tbody>
<tr>
<td>Crystal system</td>
<td>Orthorhombic</td>
<td>Monoclinic</td>
</tr>
<tr>
<td>Crystal colour and habit</td>
<td>Yellow plate</td>
<td>Orange plate</td>
</tr>
<tr>
<td>Crystal dimensions (mm)</td>
<td>0.20 × 0.18 × 0.02</td>
<td>0.20 × 0.11 × 0.08</td>
</tr>
<tr>
<td>Space group</td>
<td>P2₁2₁2₁, P2₁/c</td>
<td>P2₁/c</td>
</tr>
<tr>
<td>a (Å)</td>
<td>6.021(2)</td>
<td>6.2362(2)</td>
</tr>
<tr>
<td>b (Å)/β (°)</td>
<td>7.287(3)</td>
<td>16.4475(6), 93.457(4)</td>
</tr>
<tr>
<td>c (Å)</td>
<td>27.27(1)</td>
<td>11.5774(5)</td>
</tr>
<tr>
<td>Volume (Å(^3))</td>
<td>1196.6, 4</td>
<td>1185.3, 4</td>
</tr>
<tr>
<td>(\rho_{\text{calc}}) (g cm(^{-3}))</td>
<td>1.251</td>
<td>1.262</td>
</tr>
<tr>
<td>(\mu) (mm(^{-1}))</td>
<td>0.077</td>
<td>0.077</td>
</tr>
<tr>
<td>F(000)</td>
<td>480</td>
<td>480</td>
</tr>
<tr>
<td>(\theta) range for data collection (°)</td>
<td>2.9–25.7</td>
<td>3.0–29.6</td>
</tr>
<tr>
<td>Miller index ranges</td>
<td>–7 ≤ h ≤ 3</td>
<td>–8 ≤ h ≤ 8</td>
</tr>
<tr>
<td></td>
<td>–6 ≤ k ≤ 8</td>
<td>–22 ≤ k ≤ 22</td>
</tr>
<tr>
<td></td>
<td>–32 ≤ l ≤ 33</td>
<td>–15 ≤ l ≤ 14</td>
</tr>
<tr>
<td>Reflections collected</td>
<td>2253</td>
<td>2951</td>
</tr>
<tr>
<td>Independent reflections</td>
<td>1775</td>
<td>1988</td>
</tr>
<tr>
<td>Final R indices ([l &gt; 2\sigma(l)])</td>
<td>(R_1 = 0.0436, wR_2 = 0.0992)</td>
<td>(R_1 = 0.0519, wR_2 = 0.1046)</td>
</tr>
<tr>
<td>R indices (all data)</td>
<td>(R_1 = 0.0637, wR_2 = 0.1083)</td>
<td>(R_1 = 0.0892, wR_2 = 0.1221)</td>
</tr>
<tr>
<td>Largest diff. peak and hole (e Å(^{-3}))</td>
<td>0.15, –0.17</td>
<td>0.21, –0.22</td>
</tr>
<tr>
<td>CCDC deposition no.</td>
<td>1443009</td>
<td>1443008</td>
</tr>
</tbody>
</table>
deconvolute the PXRD patterns. For rapid analysis, the forms can be identified by the low angle reflections, i.e. the presence of a reflection at a 2θ angle of 7° is indicative of form I.

Form I is readily crystallised through the evaporation of a solution of DAB from a variety of solvents (including mixed solvent systems, see ESI† Table S1 for details). Form II was obtained by dissolving 10 mg of DAB in acetonitrile and placing it into a fridge (4 °C). Seven months later form II appears as a dark orange crystalline material.

Full data collections were performed on the single crystals of DAB forms I and II and their X-ray structures determined. The single crystal X-ray structure of form I was redetermined, as the current structure on the Cambridge Structural Database (CSD) has poor hydrogen placement.

3.2 X-ray analysis

DAB form I displays a planar structure with torsion angles about the azo bond of less than one degree. Form II, however, displays a noticeable out-of-plane bend (torsion angle N10–N11–C12–C13 = 20°). This is the main conformational difference between the two polymorphs as they both maintain the trans conformation about the azo bond. These differences are shown by overlaying a representative DAB molecule from each structure, Fig. 2. From both simple Hückel theory, and expanded descriptions of complex π-systems, it is clear that the extent of orbital overlap determines the electronic structure of the system. From molecular arguments alone we anticipate that polymorphs form I and II should be electronically dissimilar.

As well as the molecular differences, the intermolecular packing arrangements of the two polymorphs are significantly different (Fig. 3), with form I exhibiting a pseudo-layered arrangement of the molecules along the [0 1 0] plane. In these layers DAB molecules position themselves in a head-to-tail, zig-zag arrangement. The packing arrangement of form II, on the other hand, contains DAB molecules arranged in centrosymmetric pairs with centroid to centroid distances measuring over 4.7 Å. There are two noteworthy intermolecular interactions that occur between the DAB pairs that are positioned perpendicularly one another in the herringbone formation shown in Fig. 3(b). A C–H⋯π (C3⋯Cg8, 3.76 Å, 157° a: −x, y − 1/2, −z − 1/2 and C–H⋯N (C15⋯N11b, 3.316(2) Å; H15⋯N11b, 2.53 Å; 140°, b: x, 3/2 − y, 1/2 + z) interaction on either side of each DAB pair weakly binds the perpendicular neighbours to one another. These intermolecular interactions for DAB form II are evident on the Hirshfeld fingerprint plots (Fig. 3), which are different for the two polymorphs.† Form II contains two long and sharp lateral spikes with a minimum d_min + d_max ≈ 2.5 Å which corresponds to the C–H⋯N contacts, while this signature feature is not seen in the fingerprint plot for form I. The torsion angle around the azo bond in form II results in increased C–H⋯N and C–H⋯π interactions. The Hirshfeld surface analysis diagrams (ESI† Fig. S1) supports the fingerprint plots and clearly shows the intermolecular interactions present between the molecules in each polymorph.

The dimethylamino group is largely responsible for the large displacements found between the layered DAB molecules and centrosymmetric pairs in form I and II respectively. The molecular displacement is consistent with increased electron density in the phenyl rings, and therefore an increase in intermolecular π-repulsion. Electrostatics play an important role in the molecular arrangement of both polymorphs as there are no true π-stacking interactions present.
in either structure. The azo and N(CH₃)₂ moieties are the electron deficient groups which are in close proximity to the repulsive π-electron regions of the two phenyl rings.

3.3 Thermal analysis

The DSC results for the raw material as supplied, and samples of form I and form II of DAB are illustrated in Fig. 4. The accurate heats of transition (ΔHₜ) and fusion (ΔHₖ) as well as their extrapolated onset temperatures (Tᵢ and Tₖ) for the three samples are listed in Table 2. The DSC trace of the raw material illustrates two endothermic peaks (A and B). A pure sample of form I, crystallised from ethanol at room temperature, contains one endothermic event (melting, peak B). This thermal transition occurs at 116 °C and can be seen in the hot stage microscope images (upper panel of Fig. 5). Due to purification limitations, it was challenging to isolate a powder composed of purely form II (PXRD analysis showed a small quantity of form I, ESI† Fig. S2). This pseudo-pure sample showed the expected endothermic peak associated with the melting event of form I (peak B), and also a much lower energy melting event at a lower temperature (peak A, ca. 80 °C). The DSC trace associated with form II closely matches the as-purchased material. However, the change in enthalpy for DAB form II (peak A) was significantly greater than that of the raw material (Table 2), further confirming that the raw material is a physical mixture of the two polymorphs. Hot stage microscopy images of form II (lower panel of Fig. 5) shows a loss of crystallinity and darkening of the crystal occurring at 80 °C. This event can be associated with a phase transition from form II to form I. According to the heat of transition rule,²⁸ these polymorphs are enantiotropically related to one another with form II being the stable polymorph below 80 °C. Form I is the thermodynamically stable form between the thermodynamic transition point and its melting point. Despite form II having two weak intermolecular interactions, the heat supplied at 80 °C is sufficient to collapse the structure and allow the ‘twisted’ azo bond to relax into the more planar conformation.

Table 2 DSC data for the raw material (as supplied) and for forms I and II

<table>
<thead>
<tr>
<th>Samples</th>
<th>Onset Tᵢ (°C)</th>
<th>ΔHᵢ (J g⁻¹)</th>
<th>Onset Tₖ (°C)</th>
<th>ΔHₖ (J g⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Raw material – peak A</td>
<td>80.7 ± 0.5</td>
<td>1.9 ± 0.1</td>
<td>(n = 2)</td>
<td></td>
</tr>
<tr>
<td>Raw material – peak B</td>
<td>114.7 ± 0.1</td>
<td>96.4 ± 0.8</td>
<td>(n = 2)</td>
<td></td>
</tr>
<tr>
<td>DAB form I – peak B</td>
<td>113.3 ± 0.2</td>
<td>93 ± 1</td>
<td>(n = 2)</td>
<td></td>
</tr>
<tr>
<td>DAB form II – peak A</td>
<td>79.5 ± 0.5</td>
<td>8 ± 2</td>
<td>(n = 2)</td>
<td></td>
</tr>
<tr>
<td>DAB form II – peak B</td>
<td>116.5 ± 0.2</td>
<td>107.4 ± 0.1</td>
<td>(n = 2)</td>
<td></td>
</tr>
</tbody>
</table>

3.4 Solid-state electronic structure

Using the structures obtained from the solid-state DFT optimisations, total crystal lattice energies and electronic structures were obtained for both DAB polymorphs. Form I was computed to be less stable than form II by 1.6 kJ mol⁻¹ per molecule. The difference in relative lattice energies for these two polymorphs is small and supports the postulation by Cruz-Cabeza et al. that 74% of conformational polymorphs differ in lattice energy by less than 6 kJ mol⁻¹.²⁹ Spectroscopic measurements elucidated that form I has an absorption onset at 510 nm while form II has an absorption onset at 525 nm. These are in qualitative agreement with experimentally determined UV-vis absorption onsets (form I at 553 nm, form II at 575 nm). This result is somewhat surprising as the molecular-favoured geometry (i.e. the planar π-system like that of form I) is certainly more favoured than deviations from planarity.

Both theoretically and experimentally determined spectra are presented in Fig. 6. Examination of the origin of the highest occupied crystalline orbitals (HOCOs) and lowest unoccupied crystalline orbitals (LUCOs) (Fig. 6(b)–(e)), show that the fundamental electronic transition corresponds to an azo-bridge-to-planar π-system transition. However, form I is noticeably different in HOCO charge locality. Electron density is observed to be more centred on the azo bridge in form I, rather than the peripheral functionality in form II. This increased orbital interaction is stabilising. The LUCO for both systems are similar. As a result, it is predicted that form I will

Fig. 4 DSC traces of the DAB samples illustrating the dominant melting peak B and the inset illustrates peak A that is present for sample (a) and (c) (∆endo).

Fig. 5 HSM images of the single crystals of form I (upper) and form II (lower), used for the X-ray data-collections, being heated at a rate of 10 °C min⁻¹.
exhibit a wider gap electronic transition due to increased stabilising \( \pi \)-delocalisation.

Thus, the molecular geometry of the crystal constituents is a good indication of the spectroscopic energetics (as the transitions are intramolecular and highly localised, the crystal packing contributions are minimal), but the molecular geometry is not a good indication of net crystal energy. The latter fails because molecular arguments do not consider both intermolecular multipole stabilising interactions and crystal density.

The difference in crystal energy can be thought of as a product of two interactions; i) intermolecular multipole stabilising interactions, and ii) crystal density. Given form I’s overall decrease in stability, we can conclude that the energy deficit is a product of intermolecular interactions. It is likely that form II is stabilised by the stronger C–H⋯N and C–H⋯\( \pi \) interactions and overall electrostatics present within the crystal structure and the conformational strain around the azo bond plays a much smaller role.

4. Conclusion

We have presented the discovery of a second, more stable, polymorph of the azobenzene dye DAB. The conformational polymorphs are enantiotropically related to one another and their relative lattice energies are very similar. Both polymorphs are obtained simultaneously in the production of the dye and sold to consumers. The origin of the difference in structure may be attributed to a macroscopic crystal packing rather than being determined by molecular torsions. Furthermore, our methods have elucidated that the unfavourable molecular torsions are the origin of the decreased absorption onset, but the long absorption onset tail associated with form II imparts an orange hue on the crystals.

As the scientific community moves towards advanced solid-state applications of these types of molecules in films and sensing devices, their polymorphic nature will become increasingly important; one polymorph may have preferred physical and spectroscopic properties than another, and the relative stability and possibility of transformations between the polymorphs must be taken into account in formulating, storing and using the resulting DAB-containing functional product.

Acknowledgements

This work was funded by a Leverhulme Trust Visiting Fellowship (to DLC), the EPSRC (grants EP/K004956/1 & EP/I033459/1) as well as a South African National Research Foundation Fellowship (NRF RCA to DLC). The computational work was facilitated by access to the UK National Supercomputer, ARCHER (EPSRC Grant EP/L000202) and XSEDE (NSF Grant ACI-1053575).

Notes and references