Lithium Intercalation in Anatase Titanium Vacancies and the Role of Local Anionic Environment

Jiwei Ma,*† Wei Li,† Benjamin J. Morgan,# Jolanta Świątowska,‡ Rita Baddour-Hadjean,§ Monique Body,† Christophe Legein,‡ Olaf J. Borkiewicz,§ Sandrine Leduc,‡ Henri Groult,† Frédéric Lantelme,† Christel Laberty-Robert,○∥ and Damien Dambournet*‡,△

†Sorbonne Université, CNRS, Physico-chimie des électrolytes et nano-systèmes interfaciaux, PHENIX, F-75005 Paris, France
‡Institute of New Energy for Vehicles, School of Materials Science and Engineering, Tongji University, Shanghai 201804, China
§Department of Chemistry, University of Bath, BA2 7AY Bath, United Kingdom
∥PSL Research University, CNRS – Chimie ParisTech, Institut de Recherche de Chimie Paris (IRCP), 11 rue Pierre et Marie Curie, 75005 Paris, France
○Institut de Chimie et des Matériaux Paris-Est, GESMAT, UMR 7182, CNRS-Université Paris Est, 2 rue Henri Dunant 94320 Thiais France
¶Le Mans Université-CNRS, IMMM, UMR 6283, Institut des Molécules et Matériaux du Mans, Avenue Olivier Messiaen, 72085 Le Mans, Cedex 9, France
⊥X-ray Science Division, Advanced Photon Source, Argonne National Laboratory, Argonne, Illinois 60439, USA
§Sorbonne Université, CNRS, Collège de France, Laboratoire de Chimie de la Matière Condensée de Paris, F-75005 Paris, France
△Réseau sur le Stockage Electrochimique de l’Energie (RS2E), FR CNRS 3459, 80039 Amiens cedex, France

ABSTRACT: The structure of bulk and non-defective compounds is generally described with crystal models built from well mastered techniques such as the analysis of an x-ray diffractogram. The presence of defects, such as cationic vacancies, locally disrupt the long-range order, with the appearance of local structures with order extending only a few nanometers. To probe and describe the electrochemical properties of cation-deficient anatase, we investigated a series of materials having different concentrations of vacancies, i.e., Ti_{1-x} O_{2-y} F_x (OH)_{y}, and compared their properties with respect to defect-free stoichiometric anatase TiO_2. At first, we characterized the series of materials Ti_{1-x} O_{2-y} F_x (OH)_{y} by means of pair distribution function (PDF), ^{19}F nuclear magnetic resonance (NMR), Raman and x-ray photoelectron spectroscopies, to probe the compositional and structural features. Secondly, we characterized the insertion electrochemical properties vs. metallic lithium where we emphasized the beneficial role of the vacancies on the cyclability of the electrode under high C-rate, with performances scaling with the concentration of vacancies. The improved properties were explained by the change of the lithium insertion mechanism due to the presence of the vacancies, which act as host sites and suppress the phase transition typically observed in pure TiO_2 and further favor diffusive transport of lithium within the structure. NMR spectroscopy performed on lithiated samples provides evidence for the insertion of lithium in vacancies. By combining electrochemistry and DFT-calculations, we characterized the electrochemical signatures of the lithium insertion in the vacancies. Importantly, we found that the insertion voltage largely depends on the local anionic environment of the vacancy with a fluoride and hydroxide-rich environments, yielding high and low insertion voltages, respectively. This work further supports the beneficial use of defects engineering in electrodes for batteries and provides new fundamental knowledge in the insertion chemistry of cationic vacancies as host sites.

INTRODUCTION

Introducing defects, particularly cationic vacancies, into host intercalation compounds has been shown to be a viable way to modify the electrochemical properties of electrode materials for lithium storage. Works on defect chemistry for battery materials are, however, rare. Up to now, the stabilization of cation vacancies has been achieved in certain metal oxides (manganese, iron and vanadium) by synthetic procedures, including oxidative electrodeposition at high current density, doping a fraction of the native metal cations with higher oxidation state dopants, and heating ordered oxides at high temperature in a defect-inducing environment. Recently, we reported on a novel methodology for modifying the chemical composition of titanium dioxide, which stabilizes cation va-
Cationic vacancies were introduced by substituting divalent oxides with monovalent fluorides and hydroxides, yielding the general chemical formula $\text{Ti}_{1-x,y}\square_{x+y}\text{O}_2\text{F}_4\text{H}_4\text{O}_y$, where $\square$ represents a cationic vacancy. When used as an electrode for lithium-ion battery, this compound showed a modified and enhanced Li activity compared to the stoichiometric TiO$_2$, illustrating the beneficial effect of defects.

A better understanding of the relationship between defect chemistry and electrochemical performance is an essential task to generalize the use of vacancies in improving Li-ion batteries. Such a task requires the fine characterization of cationic vacancies, which is, however, particularly challenging.

In the present study, we intended to understand how cationic vacancies impact electrochemical properties vs. Li. This work was motivated by the possibility of controlling the vacancy concentration in anatase $\text{Ti}_{1-x,y}\square_{x+y}\text{O}_2\text{F}_4\text{H}_4\text{O}_y$. We first provide detailed characterization of materials with distinct vacancy concentrations, by means of pair distribution function (PDF). $^{19}$F solid-state nuclear magnetic resonance (NMR), Raman spectroscopy, and X-ray photoelectron spectroscopy (XPS) analyses. Thereafter, the role of the cationic vacancies with respect to lithium intercalation properties was studied by electrochemistry, NMR, and DFT calculations, allowing us to identify the electrochemical signatures of lithium intercalation in vacancies. Our work further emphasizes the impact of the anionic environment of the vacancy, with the redox potential decreasing as the local intercalation environment changes from purely fluorinated to purely hydroxylated. Finally, we demonstrate superior lithium transport within vacancy-containing electrode materials, which can be due to the concomitant formation of percolating network favoring the lithium diffusion and the suppression of the phase transition typically observed in pure TiO$_2$.

**EXPERIMENTAL SECTION**

**Synthesis.** Anatase $\text{Ti}_{1-x,y}\square_{x+y}\text{O}_2\text{F}_4\text{H}_4\text{O}_y$ featuring different compositions/vacancy concentrations have been prepared following a previously reported method. Briefly, solvothermal process was carried out in a stainless steel autoclave with a 45 mL Teflon liner cup inside. 1.2 mL aqueous hydrofluoric acid (CAUTION: HF solutions are highly hazardous, and special protective equipment is required) solution was added to the mixture of 24.8 mL isopropanol and 4 mL Titanium isopropoxide in the Teflon liner cup. After sealing the autoclave, the mixed solution was heated inside an oven at different temperatures, i.e., 90 °C, 110 °C and 130 °C for 12 h. After cooling down to room temperature, the obtained white precipitate was washed with ethanol and centrifuged, then dried at 100 °C under air for 10 h. For comparison purpose, anatase TiO$_2$ was synthesized without HF.

$\text{Ti}_{1-x,y}\square_{x+y}\text{O}_2\text{F}_4\text{H}_4\text{O}_y$ Samples were further outgassed at 150 °C overnight under primary vacuum prior to chemical lithiation and electrochemical analyses.

Chemical lithiation were carried out using n-butyl lithium (Sigma-Aldrich, 1.6 M in hexanes). After dispersing anatase $\text{Ti}_{1-x,y}\square_{x+y}\text{O}_2\text{F}_4\text{H}_4\text{O}_y$ powder prepared at 90°C in hexane, an excess of n-butyl lithium (0.2, 0.5 and 0.8 Li per formula unit) was slowly added under stirring. The solution was stirred for 48 hours at room temperature. Lithiation process produces a color change from white to dark purple. After reaction, the products were washed several times with hexane and dried under vacuum. All operations were carried out in an argon-filled glove box.

**Characterization methods.** X-ray powder diffraction analysis were carried out using a Rigaku Ultima IV X-ray diffractometer equipped with a Cu Ka radiation source ($\lambda = 1.54059$ Å).

Total scattering data were collected at the 11-ID-B beamline at the Advanced Photon Source at Argonne National Laboratory, using high energy X-rays ($\lambda = 0.2128$ Å) with high values of momentum transfer $Q_{max} = 22$ Å$^{-1}$. One-dimensional diffraction data were obtained by integrating the raw 2D total scattering data in Fit2D. PDFs, G(r), were extracted from the background and Compton scattering corrected data following Fourier transform within PDFgetX2. The PDFs were subsequently modeled using PDFgui. PDF peak fitting was performed using Fityk.

Raman spectroscopy. Raman spectra were recorded at room temperature using a micro-Raman system with a Labram HR800 (Jobin-yvon-Horiba) spectrometer including Edge filters and equipped for signal detection with a back illuminated charge-coupled device detector (Spx CD) cooled by Peltier effect to 200 K. A He–Ne laser (633 nm) was used as the excitation source. The spectrum was measured in the back-scattering geometry with a resolution of about 0.5 cm$^{-1}$. A 100× objective was used to focus the laser beam to a spot of 1 μm$^2$ size on the sample surface. The laser power was adjusted to 0.2-0.5 mW with neutral filters of various optical densities to avoid local heating of the sample.

X-ray photoelectron spectroscopy. XPS chemical analysis was carried out using a VG ESCALAB 250 spectrometer operating at a residual pressure of 10$^{-9}$ mbar. An Al Kα monochromatized radiation ($h\nu = 1486.6$ eV) was employed as X-ray source. The spectrometer was calibrated against the reference binding energies (BE) of clean C, Ag (368.2 eV) and Au (84 eV) samples. The photoelectrons were collected at a 90° take-off angle with respect to the substrate surface. Survey and high resolution spectra were recorded with pass energy of 100 and 20 eV, respectively. Binding energies were calibrated versus the C1s signal (−CH$_2$−CH$_2$− bonds) set at 285.0 eV. The data processing was performed with the Advantage software version 5.954 using a Shirley background and Gaussian/Lorentzian peak shapes at a fixed ratio of 70/30.

$^{19}$F and $^7$Li Solid-State NMR Spectroscopy. $^{19}$F and $^7$Li solid-state magic angle spinning (MAS) NMR experiments were performed on a Bruker Avance 300 spectrometer operating at 7.0 T ($^{19}$F and $^7$Li Larmor frequencies of 282.2 and 116.7 MHz, respectively), using a 1.3 mm and a 2.5 mm CP-MAS probe head, for recording $^{19}$F NMR spectra of the $\text{Ti}_{1-x,y}\square_{x+y}\text{O}_2\text{F}_4\text{H}_4\text{O}_y$ samples and $^{19}$F and $^7$Li NMR spectra of the chemically lithiated samples, respectively. The 2.5 mm rotors containing the chemically lithiated samples have been filled in glove-box. The room temperature $^{19}$F MAS spectra of the $\text{Ti}_{1-x,y}\square_{x+y}\text{O}_2\text{F}_4\text{H}_4\text{O}_y$ samples were recorded using a Hahn echo sequence with an interpulse delay equal to one rotor period. The 90° pulse length was set to 1.25 μs or 1.55 μs, and the recycle delay was set to 20 s. The room temperature $^{19}$F MAS spectra of the chemically lithiated samples were recorded using a single pulse sequence. The 90° pulse length was set to 1.75 μs, and the recycle delay was set to 10 s. The resonance $^7$Li MAS spectra of the chemically lithiated samples were recorded using a single pulse sequence. The 90° pulse length was set to 0.8 μs, and the recycle delay was set to 10 s. $^{19}$F and $^7$Li spectra are referenced to CFCls and 1 M LiCl aqueous solution, respectively, and they were fitted by using the DMFit software. $^{19}$F solid-state NMR spectroscopy was also used to quantify the fluorine content of the $\text{Ti}_{1-x,y}\square_{x+y}\text{O}_2$-
Electrochemistry. Electrochemical measurements were carried out with CR2032-type coin cells and three-electrode Swagelok-type cells. The composition of the electrode was 80 wt.% active materials, 10 wt.% Super P, and 10 wt.% polyvinylidene difluoride (PVDF). Copper was used as the current collector. The electrolyte was 1 M LiPF$_6$ dissolved in a mixture of ethylene carbonate (EC) and dimethyl carbonate (DMC) (1:1, v/v). The cells were assembled and tested with lithium metal as the anode and the reference electrode in the voltage range of 2.5–1.0 V vs. Li$^+/Li$.

Density Functional Theory (DFT) calculations. Our density functional theory (DFT) calculations were performed using the code VASP$^{16-17}$, with valence electrons described by a plane-wave basis with a cutoff of 500 eV. Interactions between core and valence electrons were described using the projector augmented wave (PAW) method$^{19}$, with cores of [Ar] for Ti, [He] for O, [He] for F, [He] for Li, and [H$^+$] for H. The calculations used the revised Perdew-Burke-Ernzerhof generalized gradient approximation function PBEsol$^{19}$, with a Dudarev $+U$ correction applied to the Ti d states (GGA+$U$).$^{21-24}$ We used a value of $U_{Ti_{d}}=4.2$ eV, which has previously been used to model intercalation of lithium and other metal ions in anatase TiO$_2$ and TiO$_2$(B).$^{21-24}$ To model anatase TiO$_2$, we first performed a full geometry optimisation on a single TiO$_6$ unit cell, with optimized lattice parameters obtained by fitting a series of constant volume calculations to the Murnaghan equation of state. All subsequent calculations were fixed to the resulting optimised lattice parameters. Intercalation into stoichiometric anatase TiO$_2$ was modelled using a $3 \times 3 \times 1$ supercell (108 atoms), with a single Li ion inserted at an interstitial site (LiTi$_{3}$O$_{7}$). To identify the preferred positions of F$^-$ and OH$^-$ ions in relation to a cationic Ti vacancy, we performed a series of calculations in $4 \times 4 \times 2$ supercells, with 1 Ti vacancy, and 4 charge compensating X$_0$ species, with X=F, OH. The cell stoichiometries of Ti$_{12}$O$_{24}$:X$_4$. These calculations agree with previous studies, that reported that fluoride ions preferentially occupy sites adjacent to the titanium vacancy.$^{25}$ In equatorially-coordinated sites. We find the same trend for OH units (Figures S11 and S12, Supporting Information). Intercalation into Ti$_{12}$O$_{24}$:4(F$^-$,OH)$_4$ was modelled using $3 \times 3 \times 1$ supercells, with 1 Ti vacancy, and 4 charge compensating X$_0$ species (X=F, OH) occupying the four equatorial anion sites adjacent to the vacancy. Lithium intercalation energies were calculated for 4X=(4F, 3F+OH, 2F+2OH, F+3OH, and 4OH). In the case of 4X=2F+2OH, we considered like anions arranged in adjacent (cis) and opposite (trans) equatorial site pairs.

Individual calculations were deemed optimised when all atomic forces were smaller than 0.01 eV Å$^{-1}$. All calculations were spin polarized, and used a $4 \times 4 \times 2$ Monkhorst-Pack grid for sampling k-space in the single unit cell, a $2 \times 2 \times 2$ grid for the $3 \times 3 \times 1$ cells, and only the gamma-point for the $4 \times 4 \times 2$ cells. To calculate intercalation energies, reference calculations for metallic Li was performed using the same convergence criteria as above. We considered a 2-atom cell for Li, with a $16 \times 16 \times 16$ Monkhorst-Pack grid for k-space sampling. A data set containing all DFT calculation inputs and outputs is available at the University of Bath Data Archive$^{26}$, published under the CC-BY-SA-4.0 license. Analysis scripts containing intercalation energy calculations, and code to produce Figure 9 are available as an open-source repository as reference [27], published under the MIT license.

RESULTS AND DISCUSSION

Chemical and physical characterizations. To control the vacancy concentration in anatase Ti$_{1-x-y}$O$_{2-x-y}$F$_4$O$_y(4x)$, we performed solvothermal synthesis at three different temperatures that are 90, 110 and 130 °C.$^{28}$ The phase purity was confirmed by x-ray diffraction analysis revealing similar patterns characteristic of tetragonal symmetry (I4$_1$/amd space group) of anatase crystal structure (Figure S1, Supporting Information). To determine the chemical composition of the series of samples, we assessed the vacancy content by structural analysis of total scattering data, evaluated the fluorine content using solid-state $^{19}$F NMR and the OH content was deduced according to the general chemical formula Ti$_{12-x-y}$O$_{24}$:4(x+y)F$_4$OH(4y).

Structural analysis was performed by measuring total scattering data from which we obtained the pair distribution function, a technique suitable to study nanostructured materials at the atomic scale.$^{29}$ To assess the titanium vacancy concentration, we used and compared two approaches that are (i) the real-space refinement of PDF data and (ii) individual peaks fitting. First, PDF data were refined against structural model based on the tetragonal symmetry of anatase using a real-space refinement (Figure 1a and Table 1). The refinement of the Ti (4a Wyckoff site) rate occupancy confirmed that the titanium vacancy concentration decreases upon increasing the synthesis temperature.$^{28}$ All the samples show similar unit cell parameters values and close particle sizes (coherence length)$^{28}$.
Figure 1. (a) PDF refinements of anatase TiO$_2$ and Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$OH$_{4y}$ prepared at 90 °C, 110 °C and 130 °C. (b) Zoom on the short-range order of PDF data for anatase samples. (c) Determination of the titanium vacancy concentration using real-space refinement and peak fitting for anatase Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$OH$_{4y}$.

To determine the vacancy concentration, we also used the intensity of the peak located at 1.93 Å corresponding to Ti-O/F(OH) bond length (Figure 1b). Because the intensity of a PDF peak is related to the atomic density, atom occupancy can be deduced by comparing peak intensity with respect to a stoichiometric sample. Using the first peak intensity, we obtained Ti occupancy of 69, 79 and 87 % for the samples prepared at 90, 110 and 130 °C, respectively. A comparison between the vacancies content assessed by real-space refinement and peak fitting (Figure 1c) shows a good agreement for high vacancy content while we expect that peak fitting becomes more accurate for low concentration vacancy containing materials.

Fluorine was quantified by $^{19}$F NMR for samples prepared at different temperatures (Table 2). Upon increasing the reaction temperature, the weight percentage of fluorine decreases. Chemical compositions were determined by using the general chemical formula Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$OH$_{4y}$ (Table 2) where the fluorine and vacancy contents were assessed as aforementioned.

Table 2. Estimated vacancy concentration (□), fluorine content and chemical composition of anatase Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$OH$_{4y}$ samples prepared at different temperatures.

<table>
<thead>
<tr>
<th>T (°C)</th>
<th>□</th>
<th>F (wt%)</th>
<th>Composition</th>
</tr>
</thead>
<tbody>
<tr>
<td>90</td>
<td></td>
<td>0.31</td>
<td>Ti$<em>{0.69}$□$</em>{0.31}$O$<em>{0.76}$F$</em>{0.48}$OH$_{0.76}$</td>
</tr>
<tr>
<td>110</td>
<td>0.21</td>
<td>11.9</td>
<td>Ti$<em>{0.79}$□$</em>{0.21}$O$<em>{1.16}$F$</em>{0.44}$OH$_{0.40}$</td>
</tr>
<tr>
<td>130</td>
<td>0.13</td>
<td>8.8</td>
<td>Ti$<em>{0.87}$□$</em>{0.13}$O$<em>{1.48}$F$</em>{0.36}$OH$_{0.16}$</td>
</tr>
</tbody>
</table>

Insight into the fluorine local environments in Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$OH$_{4y}$ samples was obtained using $^{19}$F solid-state MAS NMR spectroscopy (Figure 2). The spectra show three distinct lines that were previously assigned to fluorine in the vicinity of different numbers of titanium atoms and titanium vacancies, i.e., species Ti$_3$=F, Ti$_2$□=F and Ti□=F. Upon increasing the reaction temperature from 90 °C to 130 °C, the relative intensities of the $^{19}$F NMR lines assigned to the species Ti$_3$=F (from $\approx$ 3 % to $\approx$ 5 %) and Ti□=F (from...
$\approx 60\%$ to $\approx 65\%$) increase, whereas the relative intensity of the $^{19}F$ NMR lines assigned to the species Ti$_2$O$_2$F (from $\approx 37\%$ to $\approx 30\%$) decreases (Figures S2-4, Tables S1-3, Supporting Information, Table 3). The concentrations of these species point toward a preferential localization of F atoms close to vacancies. Moreover, the average number of neighboring Ti atoms of the F atoms increases only slightly, from 1.66 to $\approx 1.74$, when the reaction temperature increases from 90 °C to 130 °C, whereas the amount of titanium vacancies decreases from 0.31 to 0.13. Accordingly, the average number of neighboring Ti atoms of the O atoms and OH groups increases from 2.20 to 2.80 in relation with the increase of the $O/(O+OH)$ ratio (Table 3).

![Figure 2](image)

**Figure 2.** $^{19}F$ solid-state MAS (64 kHz) NMR spectra of Ti$_{1-x-y}$O$_2$F$_4$O$_{4y}$ samples prepared at 90 °C (Ti$_{0.87}O_{0.13}$F$_{4y}$O$_{0.16}$, green), 110 °C (Ti$_{0.79}O_{0.21}$F$_{4y}$O$_{0.40}$, blue) and 130 °C (Ti$_{0.87}O_{0.13}$F$_{3y}$O$_{0.16}$, red). The dashed lines indicate the three NMR lines corresponding to the three-fluorine species occurring in these samples.

**Table 3.** Estimated proportions of fluorine species (%), average F coordination number (F CN), $O/(O+OH)$ ratio and $O(\text{OH})$ coordination number ($O(\text{OH})$ CN) of anatase Ti$_2$O$_2$F$_4$O$_{4y}$ samples.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Ti$_2$F</th>
<th>Ti$_2$-F</th>
<th>Ti$_2$O$_2$-F</th>
<th>F CN</th>
<th>O/(O+OH)</th>
<th>O(\text{OH}) CN</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ti$<em>{0.87}O</em>{0.13}$F$<em>{4y}$O$</em>{0.16}$</td>
<td>2.6</td>
<td>60.5</td>
<td>37.0</td>
<td>1.66</td>
<td>0.50</td>
<td>2.20</td>
</tr>
<tr>
<td>Ti$<em>{0.79}O</em>{0.21}$F$<em>{4y}$O$</em>{0.40}$</td>
<td>4.3</td>
<td>66.0</td>
<td>29.7</td>
<td>1.75</td>
<td>0.74</td>
<td>2.55</td>
</tr>
<tr>
<td>Ti$<em>{0.87}O</em>{0.13}$F$<em>{3y}$O$</em>{0.16}$</td>
<td>4.6</td>
<td>64.8</td>
<td>30.6</td>
<td>1.74</td>
<td>0.90</td>
<td>2.80</td>
</tr>
</tbody>
</table>

Raman spectroscopy is a sensitive tool to detect the structural distortions at the scale of the chemical bond. According to the factor group analysis31–32, six fundamental transitions are expected in the Raman spectrum of anatase, with the following wavenumbers32–33: $E_g(1)$ at 144 cm$^{-1}$, $E_g(2)$ at 197 cm$^{-1}$, $B_{1g}(1)$ at 399 cm$^{-1}$, $B_{1g}(2)$ at 519 cm$^{-1}$, $A_{1g}$ at 513 cm$^{-1}$ and $E_g(3)$ at 638 cm$^{-1}$. The overlapping between $B_{1g}(2)$ and $A_{1g}$ prevents the detection of the weaker $A_{1g}$ component in unpolarized measurements at room temperature. The doubly degenerate $E_g$ modes involve atom displacements perpendicular to the c axis, while for the other modes, atoms move parallel to the c axis.31–32,34 Most of the modes are predicted to involve both Ti and O atom displacements, except the $B_{1g}(1)$ that is dominated by Ti atom motions and the $A_{1g}$ that is a pure oxygen vibration.34–36

Raman phonon modes belonging to anatase TiO$_2$ phase (tetragonal D$^{4h}_{4h}(I4_1/amd)$ space group) are clearly identified for the Ti$_{1-x-y}$O$_2$F$_4$O$_{4y}$ samples (Figure 3a). While TiO$_2$ exhibits the five characteristic Raman bands at 143, 196, 397, 517 and 639 cm$^{-1}$, several changes can be detected upon increasing the vacancy concentration: the $E_g(1)$ Raman peak is continuously broadened and blue-shifted (Figure 3b); the $B_{1g}(2)$ and $E_g(3)$ modes are gradually red-shifted (Figure 3c); the intensity of the $B_{1g}(1)$ mode decreases progressively.

The most intense $E_g(1)$ Raman feature is largely investigated in the literature. Many works focus on the variation of position, width and shape of this peak in relation to several effects: defects in the stoichiometry, phonon confinement in nanoparticles, presence of minority phases, pressure and temperature effects, substitutional dopant atoms, O or Ti vacancies, charge carrier density.37 It is not straightforward to distinguish the influence of a single effect among the others because they are often simultaneously present in the investigated sample. However, according to the phonon band structure of anatase37, a shift toward higher wavenumbers is expected for the $E_g(1)$ peak as soon as the fundamental Raman selection rule is relaxed. The presence of a growing local disorder of the perfect crystalline structure in the Ti$_{1-x-y}$O$_2$F$_4$O$_{4y}$ samples induced by the presence of titanium vacancies, probably explains the blue shift from 143 to 155 cm$^{-1}$ observed when the titanium vacancy increases from 0 to 0.3 (Figure 3b). On the other hand, the existence of up to three types of anions yielding to multiple X-Ti-X (X= O$^2_2$, F$^-$, OH$^-$) bending vibrations, may account for the broadening of this peak upon increasing the anionic doping.

The evolution toward lower wavenumbers of the $B_{1g}(2)$ (517 to 505 cm$^{-1}$) and $E_g(3)$ (639 to 628 cm$^{-1}$) vibrations (Figure 3c) which are mixes of both X-atom and Ti-atom motions, is indicative of an overall decreasing of the Ti-X bond strength. This can be understood by considering the higher electronegativity of the fluorine anion leading to a greater ionicity of the Ti-X bond as compared to the Ti-O bond.

Finally, the progressive intensity decline of the pure Ti-atom $B_{1g}(1)$ vibration can be easily related to the decreasing amount of vibrating Ti species as the concentration of vacancies increases.

X-ray photoelectron spectroscopy was performed on anatase TiO$_2$ and Ti$_{1-x-y}$O$_2$F$_4$O$_{4y}$ samples (Figure 4). On one hand, the spectrum of TiO$_2$ displays a Ti 2p$_{3/2}$ peak that can be fitted with a single component centered at 458.8 eV characteristic of the binding energy for stoichiometric TiO$_2$.38 On the other hand, the Ti 2p$_{3/2}$ peak of Ti$_{1-x-y}$O$_2$F$_4$O$_{4y}$ samples is red-shifted to 459.1 eV probably due to the presence of the more electronegative environment i.e., F$^-$ anion. Furthermore, upon increasing the monovalent doping (F$^-$ and OH$^-$), i.e., the heterogeneity of anionic environment in the vicinity of Ti atoms, the full width at half maximum (FWHM) increases from 1.15 to 1.35 eV. In Ti$_{1-x-y}$O$_2$F$_4$O$_{4y}$ samples, the F 1s core spectra were reconstructed using a broad single component (FWHM=1.7 eV) centered at 684.6 eV characteristic of Ti-F bonds.39–41 The broadness of the F 1s core peak expresses the various F environments in these samples.
Electrochemical properties.

The electrochemical properties of anatase TiO$_2$ and Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$O$_{2-4(y)}$(OH)$_{4y}$ were evaluated and compared with the stoichiometric anatase TiO$_2$ using galvanostatic discharge/charge experiments. Figure 5 shows the discharge/charge cycles obtained under galvanostatic conditions within a range of 2.5 and 1.0 V at 0.1 C and 1 C rates (note that 1 C = 335 mAh g$^{-1}$). Under 0.1 C rate, the samples Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$O$_{2-4(y)}$(OH)$_{4y}$ prepared at 90 °C, 110 °C and 130 °C show slightly higher discharge capacities with 255 mAh g$^{-1}$, 248 mAh g$^{-1}$ and 241 mAh g$^{-1}$, respectively (corresponding to 0.68, 0.70 and 0.52 Li$^+$ per formula unit) at 90 °C, 110 °C and 130 °C. The samples Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$O$_{2-4(y)}$(OH)$_{4y}$ prepared at 90 °C, 110 °C and 130 °C maintain high discharge capacities of 229 mAh g$^{-1}$, 208 mAh g$^{-1}$ and 174 mAh g$^{-1}$, respectively (corresponding to 0.68, 0.62 and 0.52 Li$^+$ per formula unit). In contrast, a capacity decreases down to 110 mAh g$^{-1}$ (corresponding to 0.33 Li$^+$ per formula unit) is observed for TiO$_2$. Strikingly, we noted that the discharge/charge curves at 1 C show lower polarization than at 0.1 C. Although this point remains unclear, it might be due to a concomitant effect of lower resistivity obtained at lower lithium concentration and/or an effect of the vacancies favoring the diffusion of lithium. Overall, higher capacities are obtained for anatase containing vacancies. Such a trend is also observed for long-term cycling experiments, shown in Figure 5e. The samples Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$O$_{2-4(y)}$(OH)$_{4y}$ prepared at 90 °C, 110 °C and 130 °C show stable cycling performance over 500 cycles with superior capacity retention on cycling of 80%, 70% and 62%, respectively, compared to 30% for TiO$_2$ anatase after 500 cycles.

Intercalation mechanism.

The lithium intercalation mechanism that takes place in anatase Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$O$_{2-4(y)}$(OH)$_{4y}$ and TiO$_2$ electrodes was first investigated using the quasi-equilibrium voltage obtained by the galvanostatic intermittent titration technique (GITT) shown in Figure 6. As expected, a constant voltage plateau is observed for anatase TiO$_2$ corresponding to the phase transition from tetragonal to orthorhombic Li-rich phase.$^{42-44}$ Upon increasing the vacancy concentration, the plateau region characteristic of the phase transition progressively vanishes, indicating a change toward a solid solution behavior. The latter was tentatively explained by the presence of vacancies acting as additional sites for lithium ions that can minimize the formation of the edge-shared LiO$_6$ octahedra driving the phase transition.$^{22}$ In this study, anatase TiO$_2$ and Ti$_{1-x-y}$O$_{2-4(x+y)}$F$_{4x}$O$_{2-4(y)}$(OH)$_{4y}$ samples present similar particle size/coherence length suggesting that the presence of titanium vacancies is the predominant factor influencing the lithium storage mechanism, i.e., phase transition vs. solid solution.$^{45}$
Figure 5. (a, b, c, d) Galvanostatic discharge-charge curves (2\textsuperscript{nd} cycle) at 0.1C and 1C rates, and (e) long cycling performance at 1C rate for anatase \( \text{TiO}_2 \) and \( \text{Ti}_{1-x-y} \square_{x+y} \text{O}_{2-4(x+y)} \text{F}_{4x} \text{OH}_{4y} \) prepared at 130 °C, 110 °C and 90 °C (the cells were activated at 0.1C for the first cycle).
induce a decrease of the $\Delta \delta$ value of the neighboring fluorine. When the concentration of n-butyl lithium increases, the relative intensities of the NMR resonances of higher (smaller) chemical shift decrease (increase) and the NMR lines assigned to $\text{Ti}^{\text{IV}}\square_2\text{F}$ and $\text{Ti}^{\text{IV}}\square_3\text{F}$ vanish (from 0.2 $\text{Li}^+$ per formula unit and from 0.5 $\text{Li}^+$ per formula unit, respectively), evidencing the insertion of lithium in vacancies. However, considering the number of species which may exist (see discussion in Supporting Information and Table S5) and the low resolution of the $^{19}\text{F}$ NMR spectra, the assignment of the NMR lines is complex and could not be achieved.

Figure 7. $^{19}\text{F}$ solid-state MAS NMR spectra of (a) $\text{Ti}_{0.78}\square_{0.22}\text{O}_{1.12}\text{F}_{0.48}(\text{OH})_{0.48}$ (60 kHz) and chemically lithiated (b) 0.2, (c) 0.5 and (d) 0.8 $\text{Li}^+$ per formula unit samples) (34 kHz). The asterisks indicate the main spinning sidebands. The dashed lines indicate the $^{19}\text{F}$ $\Delta \delta$ values of the $\text{Ti}^{\text{IV}}\square_2\text{F}$, $\text{Ti}^{\text{IV}}\square_3\text{F}$, and $\text{Ti}^{\text{IV}}\square_2\text{F}$ environments in $\text{Ti}_{0.78}\square_{0.22}\text{O}_{1.12}\text{F}_{0.48}(\text{OH})_{0.48}$. Solid lines indicate the $^{19}\text{F}$ $\Delta \delta$ values of the $\text{Ti}^{\text{IV}}\square_2\text{F}$ environment in $\text{LiF}$ and the $\text{Li}^-$ environment in $\text{LiF}$. $\text{Ti}^{\text{IV}}$ are in black and $\text{Ti}^{\text{III}}$ are in red. The narrow lines observed on the spectra of the lithiated samples are assigned to adsorbed $\text{F}^-$ ions.

Slow scanning linear sweep voltammetry was used to investigate the electrochemical signatures of the lithium insertion in the various host sites of anatase $\text{Ti}_{1-x-y}\square_{x}\text{O}_{2-4y}(\text{OH})_{4y}$ and $\text{TiO}_2$. A slow-scan rate of 0.05 mV s$^{-1}$ at the condition approaching equilibrium was applied, which allows excluding the capacitive contribution. Figure 8 shows the anodic part of the Li insertion process obtained after one activating cycle. For anatase $\text{TiO}_2$, the cyclic voltammogram was reconstructed using two signals (signal I and II) at 1.71 and 1.56 V vs. $\text{Li}^+/\text{Li}$. The higher redox potential corresponds to the lithium insertion reaction in the interstitial sites of anatase. The occurrence of a second peak at lower potential can be due to a concentration dependence of lithium insertion in anatase. Particularly, this second peak can be related to the insertion of lithium in the titanium-rich orthorhombic phase $\text{Li}_x\text{Ti}_2\text{O}_5$. The introduction of Ti vacancies yields significant changes in slow scan rate cyclic voltammograms. Upon increasing the vacancy concentration, we observed the appearance of new redox peaks occurring at a broader potential window. Moreover, the signals I and II were observed at higher potentials ($\Delta E=0.07$ V) in anatase $\text{Ti}_{1-x-y}\square_{x}\text{O}_{2-4y}(\text{OH})_{4y}$. Furthermore, the signal I was reconstructed using a broad line suggesting that the lithium insertion occurred in sites featuring different energies which can be related to the heterogeneous anionic environment found in $\text{Ti}_{1-x-y}\square_{x}\text{O}_{2-4y}(\text{OH})_{4y}$ samples.
Figure 8. Slow scanning linear sweep voltammetries of TiO₂ and Ti₁₋ₓFₓO_{2−4(x+y)}F₆(OH)ₓ electrodes at a scan rate of 0.05 mV s⁻¹ obtained after one activating cycle. The lithium insertion energies of Ti₁₋ₓFₓO_{2−4(x+y)}F₆(OH)ₓ were calculated from the voltammetry data and are shown in Figure 9.

To better understand the effect of local anion environment on the lithium insertion energies, we performed a series of DFT calculations. We have previously calculated insertion energies of lithium at the octahedral interstitial site in stoichiometric anatase TiO₂ and at titanium vacancies in fluorine-substituted anatase TiO₂,7–24 For Li insertion into stoichiometric anatase, we found intercalation energy of -1.23 eV. For the cation-deficient anatase TiO₂ system, we considered systems with one single vacancy (Ti_{25}O_{46}Fₓ) and two adjacent vacancies (Ti_{25}O_{24}Fₓ), which gave favorable intercalation energies of -2.68 eV and -2.88 eV, respectively. These more favorable insertion energies translate to higher redox potentials of 2.68 and 2.88 V which are, however, higher than the redox potentials observed in CV, i.e., 1.87 and 2.07 V. To supplement these previous results, we considered the single vacancy system (Ti_{25}O_{46}Xₓ) with X varied from fully fluorinated (with the Ti vacancy coordinated by 20 and 4F), through hydroxylfluorinated (coordination by 20, xOH, and (4−x)F), to fully hydroxylated (coordination by 20 and 4OH) environments. In each case we consider the four X anions to occupy equatorial sites around the Ti vacancy (see Supporting Information, Figures S11 and S12, and the supporting data in the reference [27]). Figure 9 shows the variation in lithium insertion energies with changes in the local anionic environment surrounding the vacancy.

Figure 9. Intercalation energy of lithium in a Ti₁₋ₓFₓO_{2−4(x+y)}F₆(OH)ₓ supercell with X = F, OH. The horizontal dashed line shows the intercalation energy for lithium in stoichiometric anatase TiO₂. Source: The data set and code to generate this figure, and the figure file, are available under the MIT licence as part of [ref 27].

Kinetic aspects.

The evolution of the diffusion coefficients for Li⁺ in both TiO₂ and Ti₁₋ₓFₓO_{2−4(x+y)}F₆(OH)ₓ electrodes was followed during the discharge process (Figures 10a and d) using GITT.51–52 The variation of the diffusion coefficients as a function of the Li⁺ concentration was plotted in Figures 10b and e.

At the early stage of lithiation of anatase TiO₂, the diffusion coefficient decreases from 8.3 × 10⁻¹² cm² s⁻¹ for x=0.03 Li⁺ to 1 × 10⁻¹³ cm² s⁻¹ for x=0.2 Li⁺. The origin of such a decrease is related to the reduction of Ti⁴⁺ causing the progressive shortening of the O-O pairs through which Li⁺ diffuses, further increasing the site migration barriers.53 Upon increasing x to 0.5 Li⁺, the diffusion coefficient increases back to 2.5 × 10⁻¹² cm² s⁻¹ which is caused by the structural transition toward the ordered lithiated orthorhombic phase. Thereafter, it further decreases during the solid solution lithiation in the orthorhombic phase. Finally, we observed a subsequent increase of the diffusion coefficient to 9 × 10⁻¹³ cm² s⁻¹ which can be related to a second phase transition toward the Li-rich tetragonal phase. We note that the diffusion coefficients obtained in this study differ from the literature values due to the different thickness of the electrode films.

In the case of Ti₁₋ₓFₓO_{2−4(x+y)}F₆(OH)ₓ, the evolution of the lithium diffusion coefficient showed less pronounced variation. At the early stage of lithiation, the diffusion coefficient decreases from 8.0 × 10⁻¹² cm² s⁻¹ for x=0.03 Li⁺ to 4.6 × 10⁻¹³ cm² s⁻¹ for x=0.26 Li⁺. Thereafter, the diffusion coefficient value remains stable with a value of 8.3 × 10⁻¹³ cm² s⁻¹ for x=0.8 Li⁺.
The above-mentioned results clearly show that the crystal structural features such as vacancies largely impact the lithium diffusion. We showed that the presence of vacancies in anatase modifies the insertion mechanism by supressing the phase transition toward a solid solution behavior. At the early stage of lithiation (x=0.03-0.2 Li⁺), it is striking how the presence of vacancies that act as host sites can mitigate the structural impact of the Ti⁺⁺ reduction and in turn the migration barriers with a decrease of the diffusion coefficient by a factor of 83 and 10 in anatase TiO₂ and Ti₈.7₆O₂·2H₂O.4₆a(OH)₀.₄₈a, respectively. The absence of the phase transition suppresses the large variation of the diffusion coefficient observed for TiO₂ which can be at the origin of the higher rate capability observed for vacancies containing materials.

Thermodynamic considerations.

In order to establish a link between the thermodynamic properties and the electrochemical behavior of the batteries it is worth to introduce the analysis previously developed to describe the lithium insertion in solid substrates. The electrochemical investigation shows that the studied systems exhibit large deviations from ideality. Then, an activity factor, $f_{Li}$ must be introduced in the Nernst’s equation that binds the open circuit voltage, $E$, to the concentration of the active material, $C_{Li}$,

$$E = E^0 - \frac{RT}{\bar{F}} \ln(f_{Li}C_{Li})$$

where

$$E^0 = \frac{RT}{\bar{F}} \ln C_{0}^{0}$$

$C_{0}^{0}$ is the concentration of lithium metal. The values of $f_{Li}$ can be deduced from the potential curve $E$ vs. $C_{Li}$ or $E$ vs. $n$, where the lithium compound is written as TiO₂Liₙ; $n$ and $C_{Li}$ are linked through the equation

$$C_{Li} = \frac{n}{v_{TiO_2Li_n}}$$

$V_{TiO_2Li_n}$ is the molar volume of the compound.

The activity factor, $f_{Li}$, is an important physical value since it represents the excess Gibbs energy ($\Delta G_{f}^{E}$) of formation of the lithium insertion in the substrate, which is the heart of the battery operation. For a compound TiO₂Li₂, the insertion of one mole of Li, i.e. formation of [TiO₂]₃Li (with z = ½) is

$$\Delta G_{f}^{E} = -RT \ln f_{Li}$$

the more negative $\Delta G_{f}^{E}$ is, the more positive the electrode potential is.

The deviation from ideality has a direct influence on the kinetic properties of the battery; indeed the real diffusion driving force is the gradient of the chemical potential, as shown by Darken, an enhancement factor, $\zeta = \varphi \left(1 + \frac{\partial f_{Li}}{\partial nC_{Li}}\right)$ should be introduced in the diffusion equation; then the diffusion flux writes

$$J_{Li} = D \varphi \left(1 + \frac{\partial f_{Li}}{\partial nC_{Li}}\right) \frac{dC_{Li}}{dx}$$

where $D$ is the chemical diffusion coefficient, and $\varphi$ is a damping factor introduced to take account of the thermodynamic properties of the system.

In previous papers, it was shown that a suitable representation of the variation of the activity factor was given by the series:

$$\ln f_{Li} = \sum_{n=2} f_{Li} - ln f_{Li-1} \text{erfc} \left( \psi_{i}(C_{Li} - C_{Tj}) \right)$$

$\Psi_{i}$ is the steepness of the change from one factor to the next; $C_{Tj}$ is the concentration at the inflexion point of the potential curve.

The various parameters $f_{Li}$ and $\psi_{i}$ were adjusted to obtain a suitable representation of the OCV curves (Figures 10a and d); four terms in the sum ($n=4$, Eq.6) were used, the first one (index 1) and the last one (index 4) are relative to the high and very low lithium concentrations respectively. The other two correspond to the operative range of the battery.

These theoretical considerations have a major impact on the analysis of the system:

- The two potential plateaus of the potential curve (clearly visible on the Li-TiO₂ system, Figure 10a) correspond to the composition TiO₂Li₀.₆₅ and TiO₂Li₀.₃.

In order to consider the implementation of one mole of lithium, the compounds can be written as Li(TiO₂)₁.₅₄ and Li(TiO₂)₃.₃₃. The excess Gibbs energy of formation of these compounds, deduced from the value of the activity coefficient $f_2$ and $f_3$, are: -144 kJ and -156 kJ, respectively.

- The classical formula used to analyze the GITT curves is based on the Fick’s law which states that, for an ideal system, the lithium flux $J_{Li}$ is proportional to the concentration gradient:

$$J_{Li} = \frac{D_{Fick}}{v_{TiO_2Li_n}} \frac{dC_{Li}}{dx}$$

However, in this determination the important departure to ideality of the system was neglected. Then, as shown by the analysis of the diffusion process (Eq. 6), the quantity $D_{Fick}$ is linked to the chemical diffusion coefficient $D$ through the equation:

$$D_{Fick} = \zeta D$$

According to the curves in Figures 10b and e, it should be noted that the important variations of the $D_{Fick}$ versus the lithium concentration arise mainly from the thermodynamic properties of the system as shown by the concomitant values of the enhancement factor Figures 10c and f.

- For the Li-TiO₂ system, the lithium insertion gives rise to well defined phases, and the transition from one potential plateau to the other is quite sharp that induces a very large change in the enhancement factor; the lithium transport is enhanced by a factor greater than ten (Figure 10c). The structural changes in the fluorinated compounds are less marked; the steepness factors become smaller, and various structures can coexist. It results in a more continuous value of the enhancement factor, con-
comitant to a continuous value of the diffusion coefficient $D_{\text{Fick}}$ (Figures 10e and f).

The thermodynamic properties of the lithium intercalation into anatase or fluorinated anatase described in the above study are useful to establish a link between the structural properties of the electrode material and their influence on the electrochemical behavior of the system.

Figure 10. (a) and (d) Equilibrium voltage profiles via GITT and calculated OCV profiles, (b) and (d) extracted diffusion coefficient for TiO$_2$ and Ti$_{0.78}$O$_{0.22}$F$_{0.4}$O$(OH)_{0.4}$ electrodes. (c) and (f) corresponding calculated enhancement factor profiles.
In this work, we prepared cation-deficient anatase having different concentration of vacancies i.e., Ti_{1-x-y}V_{x+y}O_{2x+6y} (x=0-0.5, y=0-0.3) which chemical formulas were determined using PDF analysis (both using real-space refinements and peak fitting methods) and 19F NMR spectroscopy. Raman spectroscopy confirmed the presence of titanium vacancies while X-ray photoelectron spectroscopy attested of the broad anionic heterogeneity in the samples. Galvanostatic experiments showed the beneficial role of the vacancies on the cyclability of the electrode under high C-rate, with performances scaling with the concentration of vacancies. Deeper understanding of the vacancy's insertion chemistry was obtained using low scan rate cyclic voltammetry showing the appearance of new and shifted redox peaks. The assignment of these peaks was done using DFT calculations performed on vacancies featuring fluoride- to hydroxide-rich anionic environment in the vicinity of the vacancy. Moreover, we found that the presence of vacancies favors the diffusion transport of lithium within the structure in part due to the suppression of the phase transition typically encountered in pure TiO2. This work further supports the beneficial use of defects engineering in electrode materials for batteries and provides new fundamental knowledge in the insertion chemistry of cationic vacancies as host sites.

ASSOCIATED CONTENT

Supporting Information. Additional information such as XRD patterns and fits of 19F MAS NMR spectra. This material is available free of charge via the Internet at http://pubs.acs.org.

Data Access Statement. The DFT dataset supporting this study is available from the University of Bath Research Data Archive (doi:10.15125/BATH-00473) [26], published under the CC-BY-SA-4.0 license. This dataset contains all input parameters and output files for the VASP DFT calculations, and Python scripts for collating the relevant data used in our analysis. Jupyter notebooks containing code to produce Figs 9, S11 & S12 are available [Ref [27], doi: 10.5281/zenodo.1181872], published under the MIT license.

AUTHOR INFORMATION

Corresponding Authors
*Email: jiwei.ma@tongji.edu.cn (JM)
  damien.dambournet@sorbonne-universite.fr (DD)

Notes
The authors declare no competing financial interests.

ACKNOWLEDGMENT

The research leading to these results has received funding from the French National Research Agency under Idex@Sorbonne University for the Future Investments program (No. ANR-11-IDEX-0004-02). Region Ile-de-France is acknowledged for partial funding of the XPS equipment. This research used resources of the Advanced Photon Source, a U.S. Department of Energy (DOE) Office of Science User Facility operated for the DOE Office of Science by Argonne National Laboratory under Contract No. DE-AC02-06CH11357. B. J. M. acknowledges support from the Royal Society (UF130329).

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