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2 Quantification of uncertainty in product stage embodied carbon calculations for buildings

3
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9
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16 Abstract

17 Decarbonisation of the energy industry and enforcement of strict targets for operational energy
18 consumption means that non-operational greenhouse gases (GHG) emissions, also known as
19 embodied carbon (EC), will soon represent the majority of whole life carbon associated with buildings.
20 EC assessments are often presented as deterministic, single-point values but contain a high degree
21 of variability which is typically unacknowledged. Common sources of uncertainty are variability, data
22 gaps, measurement error and epistemic uncertainty such as absence of detailed material
23 specification (e.g. manufacturer, concrete mix, recycled content etc). Particularly during early design
24 stages when such information is unconfirmed, average material data is used by necessity. While
25 some material databases and LCA software can provide ranges of embodied carbon coefficients
26 (ECC) between some materials and/or the uncertainty within individual manufacturers' carbon data,
27 the practice of reporting this is uncommon and has limited practicality for whole building assessments.

28 This paper presents a simple procedure that selects the highest impact materials of the EC of an
29 asset and implements a Monte-Carlo simulation to estimate the uncertainty behind the product stage
30 EC assessment. Material coefficients of variation (CoV) are obtained from database values where
31 available, and interpolated values are used in the absence of such data.

32 A product stage EC assessment of a UK educational building, initially undertaken using single data
33 points for each material, gave an EC prediction of 525 kgCO₂e/m² GIFA. Two scenarios were then
34 assessed using our proposed procedure: 1) the full building scope and 2) substructure and
35 superstructure only.

36 It was demonstrated that, for scenario one, the EC can range from 50-140% of the original result
37 when considering the extreme results from the Monte-Carlo simulation. Scenario one (considering the
38 full building scope) resulted in an average EC value (mean ± CoV) of 526 kgCO₂e/m² GIFA±10.0%.
39 The second scenario (sub- and super-structure only) resulted in an average EC value of 312
40 kgCO₂e/m² GIFA ± 11.9% with a full range of 45-155% of the original result.

41 This paper shows that a straightforward uncertainty analysis procedure can support designers in
42 understanding the possible range of asset product-stage EC and, therefore, inform construction
43 product selections at an early stage where detailed information is not known. The variation also gives
44 a degree of confidence/caution in the average EC prediction in lieu of a single-point result. The
45 construction product CoV results can be used to set target ECCs on projects to help ensure reliable
46 low-carbon products are specified. If these target ECCs were met, a minimum of 29% and 33% (excl.
47 EPD uncertainty) in product stage EC reductions could be achieved. Future work should extend this
48 method to include additional life cycle assessment (LCA) stages and other uncertainty factors. And,
49 the method could be applied to comparative life cycle assessments and optioneering exercises, as
50 well as including more specific construction product variability data.

51

52 1 Introduction

53 In order to achieve the Paris Climate agreement targets by 2050, the UK construction sector must
54 drastically reduce its greenhouse gases (GHG) emissions. The GHG emissions associated with
55 buildings refer to only 100-year global warming potentials (GWP) measured in kilograms of carbon
56 dioxide equivalent (kgCO₂e) and are divided into operational and embodied impacts. In this paper,
57 GHG emissions are referred to as “carbon”, as defined in PAS 2080 (BSI, 2016). Decarbonisation of
58 the energy supply system and the improvement of building energy performance means that
59 operational carbon are decreasing, and that non-operational carbon (embodied carbon) will soon
60 represent the majority of whole life carbon associated with buildings. For example, embodied carbon
61 (EC) can make up 67% of the whole life carbon of a typical office building (RICS, 2014). This shift in
62 focus will require assessments to demonstrate whether assets are net zero carbon, as defined by
63 Twinn et al. (2019), with clear reporting of assumed assessment scope, material data sources, life
64 cycle assessment (LCA) boundary and reference study period (RICS, 2017).

65 Each of these estimations introduces variability into EC predictions, but assessment results are often
66 reported as a single deterministic value without acknowledging the range of uncertainty. Other
67 sources of uncertainty in life-cycle assessments (LCA) include, but are not limited to, data accuracy,
68 data gaps unrepresentative data, spatial and temporary variability and epistemic uncertainty
69 (Björklund, 2002), and can broadly be categorised into three categories - parameter (input data such
70 as quantities and material carbon data), scenario (normative choices such as future scenarios) and
71 model (mathematical relationships) (Lloyd and Ries, 2007). Uncertainty can refer to both random and
72 systematic error (measurement uncertainty) and unknowns caused by limited data and knowledge
73 (epistemic uncertainty) (Björklund, 2002). Variability can be linked to geographical, environmental and
74 temporal differences and can be improved by better sampling but not reduced (Björklund, 2002). In
75 addition, errors due to simplified calculations (including incomplete scopes and LCA boundaries) and
76 approximations are also sources of uncertainty. For a comprehensive list of uncertainty types, please
77 refer to Björklund (2002) and Lloyd and Ries (2007). This paper deals with epistemic uncertainty
78 where detailed material information (such as specification, manufacturer, performance characteristics)
79 is unknown and/or unavailable.

80 Carbon assessments, in accordance with BS EN 15978:2011 (BSI, 2011) for buildings (currently
81 under revision) and BS EN 15804:2012+A2:2019 (BSI, 2019) for products, are becoming more
82 common amongst practitioners. This has been driven, in part, by the release of industry guidance
83 documents with a focus on whole life carbon assessments for buildings (RICS, 2017) and the
84 incorporation of EC into client briefs (UKGBC, 2017). Best practice relies on the comparison against
85 EC case studies and industry databases to benchmark and verify the performance of projects.
86 However, this is challenging due to a sparsity in both case studies and sufficiently detailed reporting,
87 including material data sources. Within the material carbon data, there is also a lack of consistent
88 environmental product declarations (EPDs), despite the presence of product category rules (PCR).
89 Consequently, access to data, lack of standardisation and data transparency have been identified as
90 issues with EC assessments for buildings (Gieseckam and Pomponi, 2017), and mean that
91 quantification of uncertainty is rare.

92 In order to accurately inform reduction strategies on projects, designers require a good quality
93 baseline estimate of EC and, ideally, an appreciation of the potential variation in EC results. This is
94 important both in cases where the design is “fixed” (during or post-tender) and most products and
95 materials are confirmed but also in early stage estimates where the final material information is
96 unknown and there are multiple design options (e.g. steel vs. concrete frame). In the latter case,
97 designers may apply a specific manufacturer EPD upfront before this is confirmed. There is
98 substantial variation in manufacturing global warming potential (GWP in kgCO_{2e} per functional unit) of
99 common structural material EPDs, with the ratio of maximum to minimum GWP ranging from 284 -
100 1044% in different materials and can be due to regional, process and material specification
101 differences (Pomponi and Moncaster, 2018). In addition, oversight (quality control), inconsistent
102 functional units, allocation rules and transparency have been identified as key reasons for the lack of
103 comparability (and, hence, variation) in EPDs (Gelowitz and McArthur, 2017). This can lead to
104 unrealistic predictions of EC in comparison to the final constructed building and incorporating a range
105 of EPD data into assessments, by using statistical measures of uncertainty such as coefficient of
106 variation (CoV), would help to mitigate this.

107 Product stage EC, emissions associated with raw material extraction and manufacturing, often
108 represents the majority of EC across multiple building typologies over 60-years (Zhang and Wang,
109 2016, Pomponi et al., 2018, London Energy Transformation Initiative, 2020). Building elements with

110 high in-use replacement rates, such as services and equipment, can make up a significant proportion
111 of whole life carbon – particularly where long life spans are considered (Sturgis, 2017, Pomponi et al.,
112 2018). However, the structure (sub-structure and superstructure) is often the largest contributor to
113 product stage EC in new buildings, (Kaethner and Burridge, 2012, London Energy Transformation
114 Initiative, 2020, Dimoudi and Tompa, 2008, Pomponi et al., 2018). Although, it is worth noting that this
115 is dependent on the primary structural material as timber structures have significantly lower carbon.
116 And, as shown above, the variation in structural material embodied carbon coefficients (ECCs) is
117 large.

118 Structural design choices, such as span length, main structural material, flooring solution etc, can
119 have a large impact on EC (D'Amico and Pomponi, 2020, Dunant et al., 2021). Therefore, highly
120 variable comparative structural LCA studies could result in differing conclusions and, consequently,
121 recommendations on projects. In addition, the material quantities during early stages can be uncertain
122 and reinforcement rates, connection allowances are used prior to detailed design. ECC and mass
123 parameter variation have been incorporated into parametric tools for use in early stage steel frame
124 design (D'Amico and Pomponi, 2018). For an 8-storey steel structural frame a CoV of 24.8% was
125 found when used as part of a mass optimisation procedure (D'Amico and Pomponi, 2018).

126 This paper provides a methodology to quantify uncertainty in EC assessments for product stage
127 carbon only. Mendoza Beltran et al. (2018) has previously reviewed a broad range of different
128 statistical analyses that could be applied to compare the relative impacts of multiple LCA
129 assessments, but this is beyond the scope of this paper. The uncertainty analysis method proposed
130 here is applied to a single building assessment and builds on the method from Pomponi et al. (2017)
131 and uses a Monte-Carlo simulation, as the uncertainty propagation method. However, the process
132 could also be applied to multiple assessments or design options and could be used for comparisons.

133 1.1 Structure

134 This paper investigates a UK educational building case study and assesses the potential range of
135 results in product stage EC based on the uncertainty of ECCs. An uncertainty analysis procedure
136 using Monte-Carlo simulation was developed and tested on a case study, in two scenarios - 1) full
137 building and 2) substructure and structural frame. The availability and range of data for the most
138 impactful materials were gathered from Hammond and Jones (2019) and used for the analysis. The

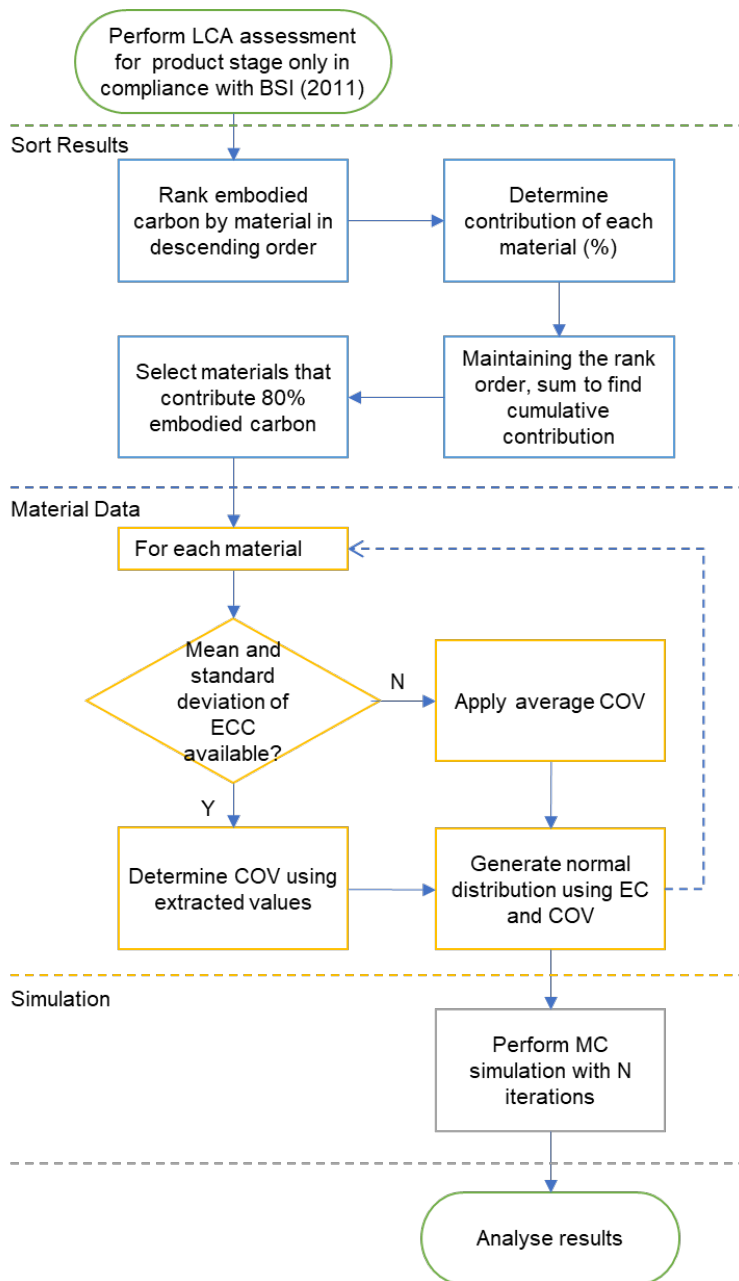
139 paper finishes with a discussion, conclusions and recommendations for future EC assessments and
140 research outputs.

141 2 Methodology

142 This paper describes a methodology, built on techniques from Pomponi et al. (2017), to estimate
143 parameter uncertainty through simulation, designed to be performed as part of a LCA assessment
144 using material inventory data from Hammond and Jones (2019) and calculated CoV, Figure 1.

145 Stochastic modelling is the most common method for uncertainty propagation; therefore, a Monte-
146 Carlo simulation is used in this study (Lloyd and Ries, 2007). Monte-Carlo simulations facilitate
147 uncertainty analysis for multiple design variables using basic statistical parameters (European
148 Commission, 2010). The analysis method, described here in further detail, is as follows:

- 149 1. Perform LCA assessment for product stage only (Modules A1-A3), in compliance with BSI
150 (2011).
- 151 2. Rank the EC results by material, from highest impact to lowest GWP impact (kgCO_{2e})
- 152 3. Maintaining the rank order, select the materials that contribute 80% of the estimated EC.
- 153 4. For each of the selected materials:
 - 154 a. Extract, where possible, the mean and standard deviation of the material ECC from the
155 ICE material inventory (Hammond and Jones, 2019). In the absence of material data,
156 the average CoV of the other materials is used.
 - 157 b. Using the values above, calculate CoV and plot a corresponding normal distribution.
- 158 5. For pragmatic reasons, sum the remaining 20% of the EC to include in the simulation and apply
159 the average CoV.
- 160 6. Perform a Monte-Carlo simulation with N number of iterations. During each iteration, a random
161 value is selected from each material normal distribution. Sum these to produce a building total
162 EC. Total EC is summarised as mean, standard deviation, CoV and range.



163

164 *Figure 1 Uncertainty methodology flow chart*

165

166 The methodology is software agnostic and simply applies a variation in material (Cradle-to-Gate) EC
 167 parameters. As a result, a distribution of building total EC helps to indicate the range and standard
 168 deviation, as well as providing a total estimated CoV for the assessment. Where a standard deviation
 169 value was unavailable for material parameters, the average CoV of the other materials was used.
 170 The calculated CoVs and Monte-Carlo simulation can be used to inform on materials with the highest

171 variability and their impact on the assessment. As a result, the CoVs can be used to inform decisions
172 on ECC targets for EPDs to achieve carbon reductions.

173 During each iteration of the MC simulation, a random material ECCs is generated from an assumed
174 distribution defined by the mean and standard deviation. For this assessment, it is assumed that the
175 possible range of ECCs of each material are best represented by a normal distribution. However,
176 additional analysis is conducted applying the methodology using two alternative distributions (uniform
177 and truncated normal). Normal and triangle distributions are the most common distribution used for
178 uncertainty studies (Lloyd and Ries, 2007) and is discussed in more detail later in the paper.

179 The method is used for the EC of LCA Modules A1-3 only (product stage), as per BSI (2011). The
180 methodology could be applied to assessments of different scope boundaries, if CoVs are available,
181 such as those applied in Hoxha et al. (2017). The ICE database (Hammond and Jones, 2019), used
182 in this study, only provides ECCs for product stage. Alternatively, the assessor could choose to collect
183 EPDs manually and calculate standard deviations and means, or consult with experts to determine
184 the variability of the material data. However, this can be time-consuming (Pomponi et al., 2017). The
185 Ecoinvent (Ecoinvent, 2015) and EC3 (Labs, 2019) databases display uncertainty for Cradle-to-Gate
186 ECCs and could also be used. However, EC3 (Labs, 2019) EPDs are predominantly American
187 products and therefore the ICE database, consisting of UK EPDs, (Hammond and Jones, 2019) is
188 deemed better suited to the UK case study building and reflects the uncertainty in UK products.

189 The treatment of biogenic carbon in the amendment to EN-15804 (2019), which will become
190 mandatory in 2022, uses the -1/+1 approach - where the carbon uptake occurs during product stage
191 A1 and the carbon release occurs at the end-of-life (C3) stage. Biogenic GWP will need to be
192 reported alongside fossil GWP and LULUC (Land Use and Land Change) GWP. It also requires that
193 materials that contain biogenic carbon must declare modules product (A1-3), end-of-life (C1-4), and D
194 stage benefits. However, IStructE (2020) suggests reporting carbon sequestration separately when
195 presenting assessments results to practical completion (A1-A5). This follows the more widely used
196 0/0 approach that the carbon uptake is equivalent to the carbon release at the end of life and ensures
197 that product stage carbon is not under reported. As per RICS (2017), biogenic carbon has been
198 excluded from the product stage results in this study because end-of-life impacts are not considered

199 and were beyond the assessment scope. Arehart et al. (2021) and Hoxha et al. (2020) provide a
200 detailed review of carbon sequestration and storage treatment in LCAs.

201 The post-processing method was written in Python 3.8.1. In order to check the optimum number of
202 iterations to generate accurate simulations whilst limiting runtime, a sensitivity check is conducted.
203 Measures of runtime, central tendency and variance (average and standard deviation) are evaluated
204 whilst increasing the number of iterations (1,000 to 2,000,000 iterations) in the Monte-Carlo
205 simulation. Test-retest reliability of the methodology is assessed by performing 25 identical
206 simulations and calculating CoV, expressed as a percentage of the mean.

207 2.1 Application

208 2.1.1 Case Study Building

209 This section summarises the scope of an EC assessment for an educational building in the UK using
210 the RICS methodology (RICS, 2017). Material quantities were obtained from the Bill of Quantities.

211 The project parameters are summarised below in Table 1. The full assessment contained 93
212 individual materials. The product stage EC represented 77% of the whole life carbon emissions. The
213 results for the product-stage only are summarised below.

214 It should be noted that the following case study includes both products (assemblies such as windows
215 and doors) and raw materials (i.e. concrete and steel). From this point forward, the term “construction
216 products” will refer to both products and raw materials. Concrete 1 represents the concrete used for
217 substructure only and has a different specification from Concrete 2.

218 *Table 1 Assessment summary, adapted from reporting template provided in RICS (2017)*

Project Type	New build
Assessment Objective	EC only
Property type	Educational
Size	Gross internal floor area (GIFA) – 1760 m ²
Project design life	60-year design life
Assessment scope	A1-3 (Product stage only)
Data sources	Material quantities - Bill of Quantities Carbon data – OneClickLCA (Bionova Ltd, 2020) Coefficient of variations (CoV) - ICE database (Hammond and Jones, 2019) and OneClickLCA ((Bionova Ltd, 2020) using methodology from EC3 (Labs, 2019))

219

220 Building elements included, and excluded, in the analysis are displayed in Table 2. Two scenarios
221 have been evaluated – superstructure (structural i.e. NRM 2.1-2.4 (RICS, 2017)) plus substructure
222 and the full building analysis. Due to a lack of data, services other than lifts were excluded from the
223 study. Services can have a high replacement rate and are often made from high impact materials
224 therefore the services results will be underestimated across all LCA stages.

225 Table 2 Building elements included in assessments (two scenarios)

	Scenario One – Full Scope	Scenario Two – Substructure and Superstructure (2.1 – 2.4) Only
1 Substructure	Y	Y
2.1 Frame	Y	Y
2.2 Upper floors	Y	Y
2.3 Roof	Y	Y
2.4 Stairs and Ramps	Y	Y
2.5 External Walls	Y	N
2.6 Windows and External Door	Y	N
2.7 Internal Wall and Partitions	Y	N
2.8 Doors	Y	N
3 Finishes	Y	N
5 Services (Lifts only)	Y	N

226 3 Results

227 3.1 Case Study – Product stage EC Assessment from Bill of Quantities

228 Table 3 indicates the product stage EC (absolute, kgCO₂e, and kgCO₂e/m² GIFA), by building
 229 element, for the full building. The full superstructure (NRM 2.1-2.8) accounts for 54.6% of the product
 230 stage EC with the structural frame (NRM 2.1-2.4) contributing 21.5%. The second largest contributor
 231 is the substructure (38%) and, therefore, the structural frame and substructure account for 59.2% of
 232 the total EC, Figure 2.

233 Table 3 Product stage EC, scenario one i.e. full scope, by building element.

	Scenario One (kgCO ₂ e)	Scenario One - (kgCO ₂ e/m ² GIFA)	Percentage contribution to total (%)
1 Substructure	350,000	198	37.7%
2.1-2.4 Superstructure	200,000	113	21.5%
2.1 Frame			
2.2 Upper floors			
2.3 Roof			
2.4 Stairs and Ramps			
2.5-2.6 Superstructure	227,000	128	24.4%
2.5 External Walls			
2.6 Windows and External Door			
2.7-2.8 Superstructure	80,800	45.9	8.74%
2.7 Internal Wall and Partitions			
2.8 Doors			
3 Finishes	58,800	33.4	6.36%
5 Services (Lifts only)	11,600	6.59	1.26%
Total kgCO₂e	928,000	525	-



234

235 *Figure 2 Product stage embodied Carbon (EC), by building element*

236 3.2 Uncertainty Analysis Results

237 3.2.1 Scenario One – Full Scope

238 This section presents the result of the post-assessment uncertainty analysis. This includes a
 239 discussion of the initial construction product inputs for the analysis and their contribution to the
 240 building total. The CoV from the extracted values are also shown, followed by the corresponding
 241 results. Fifty thousand iterations were deemed adequate for the analysis with respect to running time,
 242 sensitivity and repeatability, discussed at the end of this section.

243 The highest impact construction products, contributing up to 80% of total product-stage EC were
 244 identified, as shown in Table 4. Their total and cumulative contribution to the whole building total was
 245 calculated. In rank order, the top five construction products account for 58.0% of the estimated total
 246 building product stage EC. All thirteen construction products listed represent 80.1% of the estimated
 247 total.

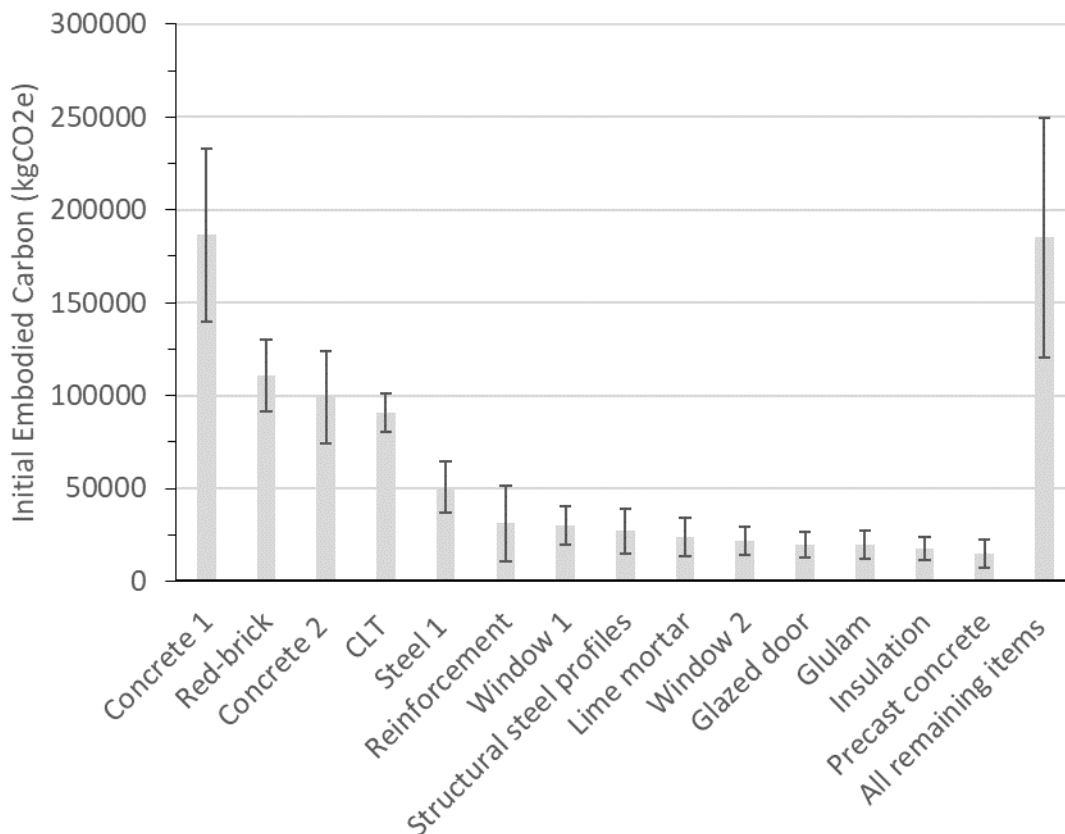
248 *Table 4 Product stage embodied carbon (EC) by construction product, ordered by impact. Percentage*
 249 *contribution to total EC and cumulative percentage contribution also shown. Average and standard deviation*
 250 *ECC from (Hammond and Jones, 2019) . Calculated coefficient of variation (CoV).*

Construction product description	Absolute EC (kgCO ₂ e)	% Total EC	Cumulative EC %	Average EC coefficient (kgCO ₂ e/kg)	Standard deviation EC coefficient (kgCO ₂ e/kg)	Coefficient of variation , CoV (± %)
Concrete 1	187,000	20.1%	20.1%	0.112	0.028	25.0%
Red brick	111,000	11.9%	32.0%	0.225	0.045	20.0%
Concrete 2	99,200	10.7%	42.7%	0.112	0.028	25.0%
CLT	90,900	9.79%	52.5%	1.20	0.136	11.3%
Steel 1	50,800	5.48%	58.0%	2.37	0.645	27.2%
Reinforcement	31,200	3.36%	61.3%	1.09	0.707	64.9%
Window 1	29,800	3.21%	64.6%	N/A	N/A	N/A
Structural steel profiles	27,000	2.90%	67.5%	2.10	0.940	44.8%

Lime mortar	23,600	2.55%	70.0%	0.737	0.319	43.3%
Window 2	21,800	2.35%	72.4%	N/A	N/A	N/A
Glazed door	19,800	2.13%	74.5%	N/A	N/A	N/A
Glulam	19,600	2.11%	76.6%	0.896	0.361	40.3%
Insulation	17,400	1.87%	78.5%	N/A	N/A	N/A
Precast concrete	14,800	1.59%	80.1%	0.152	0.075	49.3%
All remaining items	184,000	19.9%	100%	N/A	N/A	N/A

251

252 The CoV for the construction product EC has been calculated using the extracted values from the ICE
 253 database (Hammond and Jones, 2019), Table 4. Using these values, a normal distribution of possible
 254 EC impacts for each construction product was produced. Figure 3 shows a bar chart for each
 255 construction product with CoV error bars indicated. The average of the overall calculated CoV is 35%
 256 and has been applied to all remaining items and construction products where variability information
 257 was not available, i.e. window 1, window 2, glazed door and insulation.

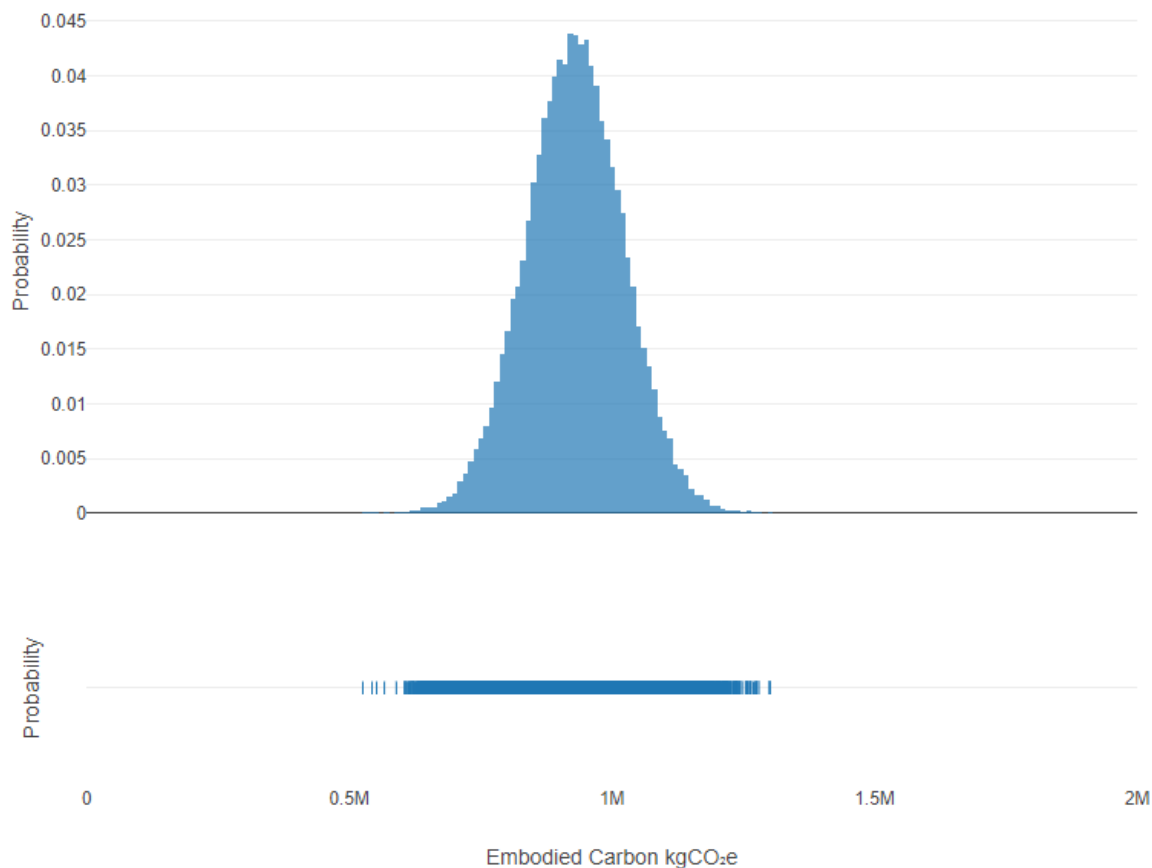


258

259 *Figure 3 EC (kgCO₂e) for scenario one by construction products*

260 Uncertainty analysis was performed on a simulation of 50,000 iterations for the full building. The
 261 average EC was 930,000 kgCO₂e, with a standard deviation of 93,000 kgCO₂e (± 10.0%). The results

262 varied from 513,000 kgCO₂e to 1,300,000 kgCO₂e, Figure 4. The vertical axis represents the
 263 probability and the histogram bin size is 10,000 kgCO₂e.



264
 265 *Figure 4 Histogram of total product stage EC (kgCO₂e) for 50,000 iterations*

266 3.2.2 Scenario Two – Substructure and Superstructure (NRM 2.1-2.4)

267 The highest impact construction products, for substructure and superstructure, contributing up to 80%
 268 of total product stage EC, are listed in Table 5. The top five construction products represent 82.2% of
 269 the estimated total product stage EC. The average of the calculated construction products CoV is
 270 31% and has been applied to all remaining items in scenario two.

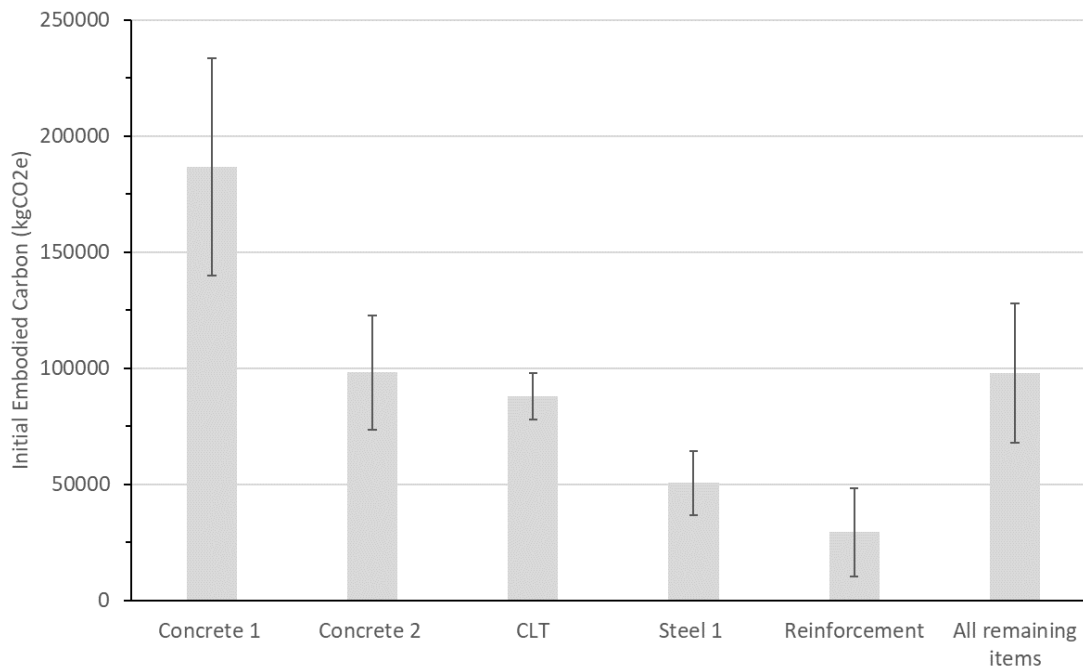
271 *Table 5 Embodied Carbon (EC) by material, ordered by impact, scenario two. Percentage contribution to total EC*
 272 *and cumulative percentage contribution also shown. Average and standard deviation ECC from (Hammond and*
 273 *Jones, 2019). Calculated coefficient of variation (CoV)*

Construction product description	Absolute EC (kgCO ₂ e)	% Sup. + Sub EC	Cumulative EC %	Average EC coefficient (kgCO ₂ e/kg)	Standard deviation EC coefficient (kgCO ₂ e/kg)	Coefficient of variation, CoV (± %)
Concrete 1	187,000	33.9%	33.9%	0.112	0.028	25.0%
Concrete 2	98,000	17.8%	51.7%	0.112	0.028	25.0%
CLT	87,800	16.0%	67.7%	1.200	0.136	11.3%

Steel 1	50,700	9.20%	76.9%	2.37	0.645	27.2%
Reinforcement	29,300	5.32%	82.2%	1.09	0.707	64.9%
All remaining items	97,900	17.8%	100%	N/A	N/A	N/A

274

275 The CoV for the construction product EC has been calculated using the extracted values from the ICE
 276 database (Hammond and Jones, 2019), Table 5. Using these values, a normal distribution of possible
 277 EC impacts for each construction product was produced. Figure 6 shows a bar chart for each
 278 construction product with CoV errors bar indicated.



279

280 *Figure 5 Scenario two (substructure and superstructure NRM 2.1 - 2.4) EC by material, with CoV error bar*

281 Uncertainty analysis was performed on a simulation of 50,000 iterations for the substructure and
 282 superstructure (NRM 2.1-2.4). The average product stage EC was 551,000 kgCO_{2e}, with a standard
 283 deviation of 65,700 kgCO_{2e} ($\pm 11.9\%$). The results varied from 247,000 kgCO_{2e} to 858,000 kgCO_{2e}.

284 3.3 Summary

285 The average, standard deviation, CoV, minimum and maximum for both scenarios have been
 286 summarised, Table 6.

287 *Table 6 Uncertainty analysis results summary, embodied carbon (kgCO_{2e} and kgCO_{2e}/m² GIFA)*

		Average	St. Dev	CoV (%)	Minimum	Maximum
Scenario One - Full Building	Absolute EC (kgCO _{2e})	930,000	93,000	10.0%	513,000	1,300,000

	EC (kgCO ₂ e/m ² GIFA)	526	52.0	10.0%	290	736
Scenario Two - Substructure and Superstructure NRM 2.1-4	Absolute EC (kgCO ₂ e)	551,000	65,700	11.9%	247,000	858,000
	EC (kgCO ₂ e/m ² GIFA)	312	37.1	11.9%	140	485

288

289 3.4 Sensitivity check

290 A sensitivity check was performed by varying the number of iterations in the Monte-Carlo simulation
 291 from 50,000 (used in this study) to between 1,000 and 2,000,000. The time taken for the analysis was
 292 recorded. A Dell Inspiron laptop with 16GB of memory RAM, running on an Intel(R) Core™ i7-
 293 4712HQ CPU at 2.30GHz was used for the analysis. As expected, as the number of iterations, N,
 294 increased, the running time increased. The largest analysis, with two million iterations, took 208
 295 seconds to complete. For the purpose of a post-analysis assessment, the running time is less
 296 important. However, if the uncertainty procedure were integrated into an assessment tool this running
 297 time would not allow real-time interaction. Additionally, if fewer construction products were used in the
 298 analysis, similar to scenario two, the running time would reduce as the random value generator for
 299 each construction products at each iteration would need to run fewer times. A 50,000-iteration
 300 simulation took 6 seconds, for scenario one.

301 The variation between both mean EC and standard deviation decreased as the number of iterations
 302 increased. However, the mean difference for average and standard deviation was ≤1% after 10,000
 303 and 4,000 iterations for scenario one and two, respectively.

304 3.4.1 Reliability check

305 For both scenarios, the reliability of the uncertainty analysis was checked by performing 25 identical
306 analyses. The average and standard deviation EC varied by less than 1% across the 25 tests with the
307 same number of iterations. However, the minimum and maximum EC values varied significantly (\pm
308 7%) and, therefore, this parameter is less reliable across multiple repetitions. This is because a
309 normal distribution is assumed for each construction products and therefore the probability of the
310 minimum and maximum values being selected is low.

311 3.5 Alternative distributions

312 The construction products EC average values and standard deviations from ICE database (Hammond
313 and Jones, 2019) were used to create a normal distribution of possible values for the EC. Multiple
314 distributions can be used to represent data variability and have been surveyed (Lloyd and Ries,
315 2007). Random square distribution, a normal distribution (used in this study) and a truncated normal
316 distribution were tested to see how the total product-stage EC result could vary. The analysis has
317 been performed for both scenarios for 50,000 iterations. Table 7 and Table 8 provide a summary of
318 the key parameters for each scenario, respectively. The CoV is equal to the standard deviation
319 divided by the average.

320 *Table 7 Average, standard deviation, coefficient of variation (CoV), minimum, maximum and range values for*
321 *initial EC (kgCO₂e) for scenario one (full scope).*

Analysis	Average	St. Dev	CoV (%)	Minimum	Maximum
Normal	930,000	93,000	10.0%	513,000	1,300,000
Square	929,000	53,600	5.77%	746,000	1,110,000
Truncated normal	929,000	92,000	9.90%	549,000	1,300,000

322 *Table 8 Average, standard deviation, coefficient of variation (CoV), minimum, maximum and range values for*
323 *initial EC (kgCO₂e) for scenario two (superstructure only)*

Analysis	Average	St. Dev	CoV (%)	Minimum	Maximum
Normal	551,000	65,700	11.9%	247,000	858,000
Square	550,000	38,200	6.94%	423,000	676,000
Truncated normal	551,000	64,800	11.8%	294,000	823,000

324 4 Discussion

325 This paper set out to provide a methodology to quantify uncertainty in EC assessments for product
326 stage carbon only. This procedure was tested on two scenarios for an educational case study
327 building. The aim of the uncertainty analysis is to provide designers with an understanding of possible
328 CoV in construction product ECCs across the high-impact construction products and determine a

329 confidence level in product stage EC prediction based on variance, particularly in early stage
330 assessments. In the context of designers needing to demonstrate that assets are zero carbon, this
331 also assists in decision making and material selection choices to ensure carbon reductions. The
332 procedure is intended for use in supporting design decisions and not for demonstrating compliance
333 with legal requirements

334 It was identified that 13 construction products in scenario one (full scope) and 5 construction products
335 in scenario two (substructure and superstructure NRM2.1 – 2.4) represented 80% EC. The number of
336 construction products used in the assessment directly affects the running time of the simulation, which
337 may be a consideration for future use. Secondly, the identification of these construction products
338 helps to prioritise the areas of focus for EC reductions. The average material CoV for the two
339 scenarios were 35% and 31%, respectively, where reinforcement had the largest individual variability
340 (64.9%) based on 44 data points. Other construction products, such as steel structural sections
341 (27.2% CoV from ten data points), are based on fewer data points. The overall EC resulted in a CoV
342 of $\pm 10.0\%$ (scenario one) and $\pm 11.9\%$ (scenario two) representing 68.2% solutions from the Monte-
343 Carlo simulations. Sensitivity and repeatability checks were performed and alternative distributions for
344 material ECCs examined.

345 Reinforcement exhibited the highest construction products CoV of 64.9%, followed by structural steel
346 profiles with 44.8%. Despite this high variability, these construction products represent only 6.3% of
347 the total EC. Concrete, in contrast, has a lower variation (25.0%) but a high quantity and high
348 contribution (30.8%) to the total EC. As a preliminary step in industry/reporting practice, the lower
349 CoV bound, which equates to one standard deviation below the ECC average, could be used to
350 define ECC reduction targets in order to select EPDs. For scenario one, adopting this approach would
351 result in potential reductions for concrete and reinforcement of 71,500 and 20,000 kgCO_{2e},
352 respectively, and a 10.0% reduction in total EC. While it should be encouraged for designers to seek
353 out construction products with an ECC below these thresholds, it is worth noting that construction
354 products that fall below one standard deviation in a normal distribution inherently represent only
355 15.9% of possible solutions, which could represent an increasing challenge when searching for EPDs
356 for specific projects.

357 In the absence of mean and standard deviation values for some construction products (four
358 construction products in scenario one), interim CoV values have been used. This interim value was
359 calculated from the average CoV from the other construction products. If the methodology were to be
360 developed further, data points from other sources could be collected and used to calculate these
361 values for the missing construction products. In addition, multiple databases could be used to
362 generate CoVs based on larger datasets. The average construction product CoV for scenario one
363 and two were 35% and 31%, respectively, and were used for construction products without variability
364 data available. This is comparable to the highest possible variation from the EC3 (Labs, 2019)
365 uncertainty methodology, used for approximating uncertainty in individual EPDs, also used in
366 OneClickLCA (Bionova Ltd, 2020) which equates to $\pm 34.6\%$.

367 Alternatively, individual EPDs could be collected and compared to determine average values,
368 standard deviation and, therefore, CoV to be used in the uncertainty analysis. Construction product
369 data could also be divided into finer categories such as concrete strength, recycled content and
370 geographical location etc. However, the numbers of data points available in these categories may be
371 low with high variability. As projects progress and designs become more “fixed”, products and
372 manufacturer will be selected. The methodology could be adjusted to use specific EPD information for
373 “confirmed” construction products. Although, as previously discussed, EPDs inherently have a degree
374 of uncertainty and this should be included in the assessment (Labs, 2019).

375 Each individual construction product type may have a different range and distribution of EPDs (i.e.
376 with most EPDs toward the upper or lower extremes of ECC) and, therefore, be more/less accurately
377 represented by non-normal distributions in a simulation (e.g. left- or right-skewed, log-normal etc).
378 Depending on the number of data points and variability of data, this could include log-normal
379 distribution or perhaps only a single data point. As such, a further development of the proposed
380 uncertainty methodology could account for different distribution by construction product, depending on
381 its data availability and quality. ICE material database (Hammond and Jones, 2019) materials
382 generally indicate log-normal or normal distribution for ECC. In this study, the CoV is lower when
383 assuming a square distribution compared to normal and is unlikely to accurately represent the data
384 available.

385 The uncertainty analysis currently selects the construction products that contribute approximately
386 80% of the building EC. However, in different real-world scenarios, practitioners may have access to
387 differing amounts of accurate data, which would shift reliance more or less onto assumed/interim CoV
388 values employed in this method. In the present study, for scenarios one and two, 13 and 5
389 construction products were selected, respectively. Theoretically, if an alternative contribution value of
390 50% were adopted in scenario one then only 5 construction products (rather than 13) would be
391 included and the other 8 construction products would be added to the remaining items. This would
392 result in an almost identical average EC (525 vs. 526 kgCO₂e/m² GIFA) and similar CoV (± 11.3% vs.
393 10.0%) but increased range of results by ~18% (from ± 40 up to 47%). In contrast though, due to the
394 lower number of construction products being assessed, the method running time would be reduced by
395 69% which may be of greater value than the increase in uncertainty.

396 In contrast, it could be argued that the methodology should address more than 80% EC. In the case
397 study here though, 93 construction products were included in the original assessment and only 13
398 construction products were required to reach the 80% selection criteria for the uncertainty procedure.
399 Of these, the lowest contributor in scenario one (Precast concrete) represented only 1.7% of the total
400 EC in comparison to 20.1% from the largest contributor, concrete 1. In this scenario, any one of the
401 remaining unselected construction products would represent less than 1.7% of the total EC and their
402 additional inclusion would result in a greater duration of data collection and analysis run time. Given
403 that one aim of the methodology was to identify and target high-impact construction products for
404 carbon reductions while approximating uncertainty for the remaining lower-impact construction
405 products, selecting construction products up to 80% EC appears to strike a good balance for this case
406 study but may differ for other projects.

407 Figure 4 and Figure 6 present the relative construction product carbon results, including CoV errors
408 bars. These figures can be used to identify the effect of choosing lower-carbon EPDs for different
409 construction products relative to other products in the project. This could also apply to EC
410 comparisons of design options or multiple projects. Depending on the construction products, the
411 standard deviation could be large in the lower impact construction products and, therefore, the
412 analysis could be under-predicting the “all remaining items” carbon variation. Alternative analysis
413 could be undertaken such that construction products are investigated, and ranked, by weight as well
414 as GWP impact.

415 This study has a number of limitations to consider. Product stage (cradle to gate) assessments have
416 been shown to miss up to 40% of whole-life carbon emissions (Pomponi et al., 2018). For scenario 2,
417 the exclusion of other LCA stages is less of a concern because the carbon associated with
418 replacement and refurbishment is lower in structures over the 60-year life cycle compared to other
419 building elements such as finishes, façades and services. The uncertainty procedure proposed in the
420 paper could be extended to account for additional LCA stages. However, EPDs do not always include
421 data for stages beyond the product stage (A1-3). Approximation of CoV for input values for other
422 stages has been used elsewhere and has shown that the resultant CoV for the full life-cycle of a case
423 study building was 17% (GWP, not including biogenic carbon) compared to the pre-use and
424 maintenance stages which had a CoV of 20% (Blengini and Di Carlo, 2010). Additionally, it should be
425 noted that the authors applied CoV to parameters additional to those used in the present study,
426 including quantity, transport distance, waste percentages and maintenance. It has also been
427 identified that 38% of EPDs are missing information required by ISO standards (ISO, 2006a, ISO,
428 2006b), partly resulting from poor harmonisation between product category rules (PCRs) across
429 materials and EPD data (Gelowitz and McArthur, 2017) and the underlying material source
430 information in the ICE database (Hammond and Jones, 2019) has not been reviewed as part of this
431 study.

432 It is important to note that the consideration of product stage only and the 0/0 approach to biogenic
433 carbon is conservative and assumes that the sequestered carbon is released at the end-of-life and
434 balanced across the life cycle. If the -1/+1 approach were adopted, this would underpredict the
435 product stage carbon and materials containing biogenic carbon could be negative. This would change
436 the material ranking as part of the uncertainty procedure and identification of the highest contributing
437 materials. The assessment also wouldn't consider the end-of-life impact. If biogenic carbon were
438 included, the initial result for product stage carbon would be 45% lower. Alternative end-of-life impacts
439 could be considered if the procedure were extended to include additional LCA stages.

440 Additionally, due to a lack of material and quantity information, services (other than lifts) were
441 excluded from the study and therefore the scope of assessment isn't representative of the whole
442 building. However, the minimum scope requirements according to RICS (2017) do not include the
443 product stage EC of services. In addition, building elements with high replacement rates, such as
444 services and internal elements, accumulate large amounts of EC over the building life cycle but may

445 have a comparatively small impact at product stage. The accuracy of material quantities at different
446 project stages may differ, particularly at early stage stages where structural calculations can be based
447 on approximations (such as reinforcement rates). Mass parameter uncertainty is not currently
448 considered in the uncertainty methodology. Previous studies have considered this by design stage or
449 as a single quantity CoV (Blengini and Di Carlo, 2010).

450 Operational greenhouse gases emissions contribute approximately 33% whole life carbon emissions
451 in typical office buildings but are beyond the scope of this paper (RICS, 2017). If the proposed
452 methodology were used for optioneering exercises where alternative materials are being considered,
453 the operational impacts could be affected by changes in performance characteristics. An example of
454 this could be the thermal resistance of insulation and the benefits of thermal mass from exposed
455 concrete. Passive design strategies, including natural ventilation, high fabric efficiency and thermal
456 mass, may cause a “penalty” in EC but a whole life carbon saving when considering the operational
457 benefits. As operational carbon is not included as part of the uncertainty procedure, these effects are
458 unable to be quantified.

459 The proposed uncertainty method is intended to be able to give designers the possible range of error
460 and, therefore, an indication of confidence/caution in their product stage assessments. This would be
461 particularly important when tracking carbon over the course of a project relative to a baseline value.
462 Without accounting for uncertainty, issues could arise with false reporting of carbon savings due to
463 construction product replacements. Alternatively, designers could find that at a later project stage,
464 where specific products or manufacturers are being selected, the carbon assessment increases due
465 to original underestimation. Therefore, practitioners could use this approach to identify key
466 construction products with high-impact or high-uncertainty (such as concrete and reinforcement in this
467 case study), as hotspots for carbon, and better focus their efforts when specifying construction
468 products. The lower-bound material CoV has been proposed as guidance for an ECC target.
469 However, the selection of low-carbon materials should be considered alongside other performance
470 characteristics such as durability, thermal resistance and efficiency of equipment, as these choices
471 may increase the life cycle impacts.

472 5 Conclusions

473 As the energy supply system decarbonises and operational greenhouse gases emissions reduce, EC
474 will soon make up most of the whole-life carbon in new buildings and the construction industry must
475 reach net-zero by 2050. This will require designers to demonstrate that assets are achieving net-zero
476 with accurate and detailed reporting.

477 Based on the literature and the results from the presented study, the possible range of results for
478 carbon assessments is large and introduces a significant margin of error in prediction. However, this
479 methodology for post-analysis of epistemic uncertainty in product-stage carbon assessments can
480 support designers to estimate the uncertainty associated with the variability of material ECCs. This is
481 particularly important in the early stages of a project where the level of detail in material and/or
482 product selection is low. This approach can help designers to see the implications of their material
483 choices, good or bad, in order to make informed decisions to reduce product stage carbon through
484 prioritisation, and ensure those assumptions follow through to construction. In addition, this will help to
485 not overpromise on carbon reductions.

486 If the methodology were to be developed further, data points from other sources could be collated and
487 used to improve the interim CoV values (calculated as the average variation of all construction
488 products used in the study). Similarly, alternative distributions could be used for representing the data
489 variability such as uniform or log normal. The method demonstrated here considered product stage
490 ECC uncertainty only. Future work will investigate the inclusion of additional LCA stages and other
491 forms of parameter uncertainty, such as mass parameters. It will be also extended to be used for LCA
492 assessment comparisons.

493 CRedit authorship contribution statement

494 Ellie Marsh: Conceptualisation, Data curation, Formal analysis, Investigation, Methodology, Software,
495 Validation, Visualization, Writing - original draft. John Orr: Funding acquisition, Project administration,
496 Methodology, Resources, Supervision, Writing - review & editing. Tim Ibell: Resources, Supervision,
497 Writing - review & editing.

498 **Data Access Statement**

499 The data created in this research is openly available from the University of Cambridge data repository
500 at XXX (DOI to follow) .

501 **Declaration of Competing Interest**

502 None.

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506

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