A Summary of the Theory of Velocity Selective Neural Recording

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Abstract—This paper describes improvements to the technique of velocity selective recording (VSR) in which multiple neural signals are matched and summed to identify excited axon populations in terms of velocity. This form of recording has been termed intrinsic velocity selective recording (IVSR). The signals are acquired using a multi-electrode cuff (MEC) which is now available as a component for use in implantable neuroprotheses. The improvements outlined in the paper involve the use of bandpass filters at the output of the system which allows a higher level of selectivity to be obtained than is possible using IVSR.

I. INTRODUCTION

Velocity selective recording (VSR) is a technique which should allow more information to be extracted from an intact nerve with a recording set-up that does not allow action potentials from single fibres to be seen at spikes [1]-[3]. The method is in essence very simple and relies on taking measurements of a propagating action potential (AP) at two or more points. The distance between the sample points divided by the delay between the appearance of the two replicas of the AP provides a measure of the propagation velocity. Perhaps unsurprisingly, this very simple idea is not new and various researchers have investigated practical adaptations of it in the past (e.g. [6]-[8]).

However, at present the idea has not been demonstrated with naturally-occurring nerve traffic though experimenters have used multi-electrode cuffs (MECs) to observe appropriate outputs from compound action potentials [3]-[5]. The authors have published two papers about the theory of VSR [1]-[2]. The first presented a spectral analysis of a single axon in an MEC with a tripolar (double-differential) amplifier system and the signal processing arrangement shown in Figure 1. The bandpass filter (BPF) that follows the adder was shown to improve selectivity in the velocity domain. The second paper [2] considered the thermal noise generated by the detection system and compared its amplitude to that of the signal resulting from the summation of multiple single fibre action potentials (SFAPs) which were assumed to occur at random times. This allows the calculation of the firing rates required from various sizes of nerve fibre in a given MEC to provide a signal that could be detected above the background noise.

The current paper presents material which supplements and expands the earlier work described in refs [1] and [2]. In essence it is a study (by simulation) of improvements in velocity selectivity obtainable by the use of BPFs, investigating in particular the limitations of the method with and without additive noise. Preliminary measured data in pigs is also presented.

![Figure 1](image-url)

Figure 1. This shows a multielectrode cuff (MEC) connected to a tripolar (double differential) amplifier array. The $N$ tripolar outputs (where $N$ is typically about 10) are digitised and processed in the signal processing unit on the right of the figure.

II. BACKGROUND

A. Basic principles

The input to the MEC is a trans-membrane action potential function (TMAP), $V_m(t)$, with the corresponding spectrum $V_m(f)$. The resulting SFAP is a propagating wave with the time dependence of the underlying TMAP function, the relationship between the two being explained in [1]. We represent the TMAP function and its spectrum by the following Fourier transform pair [1]:

$$V_m(t) = At e^{Bt}$$

$$V_m(f) = \frac{n!A}{(B + j2\pi f)^n}$$ \quad ... (1)

where $A$, $B$ and $n$ are constants and $f$ is frequency (the symbology has been preserved from [1]). The output $Y(f, v)$, which is a function of both frequency and velocity, is obtained by treating the MEC as a linear time-invariant system with transfer function $H(f, v)$ [1]. At matched
velocities (i.e. where the inserted delay \( \tau = d/v \) and \( v = v_o \)), \( Y(f, \nu) \), reduces to:

\[
Y(f, \nu_o) = 4N \frac{R_e}{R_i} \sin^2 \left( \frac{\pi d}{\nu_o} \right) \frac{A}{B + f(2\pi)^2} \quad \cdots (2)
\]

where \( R_e \) and \( R_i \) are the intra- and extra-axonal resistances per unit length, respectively. The output of the system \( Y(f, \nu) \) is a function of two variables and it was pointed out in [1] that if \( f \) is fixed by passing the output through a bandpass filter (so that \( f = f_o \)), \( Y \) becomes a function of propagation velocity \( \nu \) only, enabling the velocity selectivity profile (see the tuning curves in [1]) to be calculated readily.

We define a velocity quality factor, \( Q_v \), by analogy with linear systems in the frequency domain [2]:

\[
Q_v = \frac{\nu_0}{\nu_3 - \nu_2} \quad \cdots (3)
\]

where \( \nu_0 \) is the matched (i.e. peak) velocity and \( \nu_3 \) and \( \nu_2 \) are the velocities at which the output has fallen to \( 1/\sqrt{2} \) (3 dB) of the peak value. Close to the matched velocities, the velocity selectivity is dominated by the function \( G(f, \nu) \) and in [2] an approximate formula for \( Q_v \) was derived:

\[
Q_v \approx \frac{N\pi d f_o^2}{2.64 \nu_0} \quad \cdots (4)
\]

B. The intrinsic velocity spectrum (IVS)

If filtering is not applied, the output will depend on \( \nu \) and on frequency dependent elements in the system including the spectral properties of the input signal (i.e. the TMAP function) and the characteristics of the channel. For these reasons, unlike the bandpass filtered version, the intrinsic velocity spectrum (IVS) is quite difficult to interpret.

### Table 1

<table>
<thead>
<tr>
<th>Parameter</th>
<th>TMAP #1</th>
<th>TMAP #2</th>
</tr>
</thead>
<tbody>
<tr>
<td>( A )</td>
<td>7.44 x 10^4</td>
<td>4.08 x 10^3</td>
</tr>
<tr>
<td>( B )</td>
<td>10^9</td>
<td>1.5 x 10^7</td>
</tr>
<tr>
<td>( n )</td>
<td>3</td>
<td>1</td>
</tr>
</tbody>
</table>

Fig 2 is the time-domain output of the adder in Fig 1 when the system is stimulated with a TMAP resulting in an SFAP propagating at a velocity of 30 m/s. Two TMAP functions are considered, both of which have been proposed as suitable approximations for the simulation of mammalian ENG [9]. The functions are in the form of eqn (1) with the parameters given in Table 1 (the scaling parameter \( A \) has been adjusted so that the peak amplitudes of the functions are normalised to unity). The matched velocity \( \nu_0 \) is treated as a parameter leading to the family of curves shown in the figure. The peak value is reached when the artificial delays exactly match (cancel) the naturally-occurring delays at which point the output signal has the same form as a single SFAP, with amplitude multiplied by \( N [1] \).

Fig 3 shows the IVS of the system, stimulated by an SFAP generated by TMAP#1. This is a plot of the peak values of the output time record (Fig 2) as a function of velocity after the tripoole signals have been subjected to delay and add operations only. Each curve in the time record shown in Fig 2 has three peaks, labelled \( A \), \( B \) and \( C \). Two positive and one negative, corresponding to the phases of the tripoole SFAP. Whilst it is possible to calculate the IVS at all the peaks, this paper considers only the two larger-amplitude peaks \( A \) and \( B \). The resulting spectra peak at the same matched velocity (40 m/s), but have different selectivities as shown in Fig 3, where the two IVS plots are shown together with the values of \( Q_v \), calculated from the figure using eqn (3). These values of intrinsic velocity selectivity are used as baseline references for the enhancements described in the next section.
3. The actual selectivity obtainable is quite low and declines with increasing velocity. This accords with the theory presented below (see also ref [2]).

These issues are considered in the next section.

III. IMPROVED VELOCITY SELECTIVE RECORDING USING BANDPASS FILTERS (BPFVS)

Suppose a BPF is placed at the output of each tripolar amplifier of the VSR system as shown in Fig 1. The effect is to replace each SFAP (which is a tri-phasic pulse in the time domain) with a burst of damped sinewaves whose frequency is the centre frequency of the BPF. The ‘delay matching’ process is therefore transformed into matching delayed sinewaves rather than complex SFAP waveforms as in the intrinsic case. Unlike the SFAP waveform itself, the BPF output has no dependence on the characteristics of the TMAP except for its amplitude and its exact position in the time record. In addition, since the voltage excursions at the outputs of each BPF are approximately symmetrical (i.e. ±V), there is only one velocity spectrum. It is simply necessary to measure the peak (+ve. or –ve.) of the delayed and summed BPF outputs. The addition of BPFs in this way allows the measurement of velocity selectivity to be decoupled from the spectral properties of the TMAP and to be controlled by means of the centre frequency of the filters which is, at least to some extent, a free parameter.

IV. SIMULATED AND MEASURED RESULTS

A. Simulated results without noise

In order to demonstrate the effects of adding BPFs to a delay-matched IVS system, the MATLAB simulations shown in Figs 2 and 3 were repeated with a single bandpass filter of centre frequency f0 placed at the output of the system, as shown in Fig 1 (this is electrically equivalent to placing a filter at the output of each channel due to the linearity of the system). The SFAP was generated using TMAP#1 and the system was noiseless. The filter was an 8th-order digital Butterworth BPF and centre frequencies of 1 kHz, 2 kHz, 4 kHz, 8 kHz or 16 kHz and relative bandwidth 20% were used. The velocity spectra are plotted in Fig 4 and show good responses at the matched velocities. It can be shown that it is possible to obtain satisfactory responses for BPFs with centre frequencies up to the Nyquist frequency (50 kHz in this case). Repeating the simulation using TMAP#2 produces responses that are identical to those shown in Fig 5 in the sense that the values of Q, measured at the matched velocities are the same in both cases. This supports the assertion that the bandpass filtered velocity selectivity depends only on N, f0 and v and some physical constants, not on the characteristics of the TMAP function, as is the case for IVS. The values of Q, are listed in Table 2 together with values calculated from eqn (4). The calculated values fit the simulated ones very well.

B. Simulated results with additive noise

Zero-mean white Gaussian noise was added to the system in a manner consistent with the approach adopted in [2] (i.e., 11 sources of uncorrelated voltage noise were introduced, one at the input to each monopolar channel). These noise sources represent the total noise present in each channel referred to the input. As noted in [2] the total input-referred noise is the sum of several individual sources which are assumed to be independent and uncorrelated.

![Figure 4: Bandpass filtered version of the IVS plot shown in Fig 2 using TMAP function #1 to generate an SFAP with a propagation velocity of 30 m/s. The filters are 8th order Butterworth digital units with centre frequencies f0 are (a) 1 kHz, (b) 2 kHz, (c) 4 kHz, (d) 8 kHz, (e) 16 kHz and (f) 32 kHz. The corresponding values of Q, are 1.4, 2.9, 5.7. The velocity step is 1 m/s and there is no additive noise.]

In order to test the effect of the noise on the system and in particular on the ability of the BPFs to increase the velocity selectivity compared to IVS, the simulations described in Section A. were repeated with varying levels of additive white Gaussian noise. The results are presented in Table 3 for three values of SNR (1, 10, 100) for each of the two TMAPs. The frequency in column A for each value of SNR gives the maximum frequency (fmax) at which an intelligible output is obtainable from a BPF centred at that frequency. Once fmax has been determined, the maximum available velocity selectivity (Q) can be calculated from eqn (10) (column B) and the enhancement factor found (i.e. compared to IVS-column C). In general TMAP#2 performs better than TMAP#1, due to the wider bandwidth of the signal. There is thus more energy at higher frequencies in SFAPs generated from TMAP#2, whilst the additive noise has the same

### Table 2

Comparison of Simulated and Calculated Values of Q, for a 9-Channel Filtered VSR System for a Single SFAP with propagation Velocity 30 m/s

<table>
<thead>
<tr>
<th>BPF Centre Frequency, f0 (kHz)</th>
<th>TMAP #1</th>
<th>TMAP #2</th>
<th>Calculated value*</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.8</td>
<td>0.8</td>
<td>0.8</td>
</tr>
<tr>
<td>2</td>
<td>1.9</td>
<td>1.9</td>
<td>2.0</td>
</tr>
<tr>
<td>4</td>
<td>4.3</td>
<td>4.0</td>
<td>4.2</td>
</tr>
<tr>
<td>8</td>
<td>7.5</td>
<td>7.5</td>
<td>8.5</td>
</tr>
<tr>
<td>16</td>
<td>17.0</td>
<td>16.0</td>
<td>17.1</td>
</tr>
<tr>
<td>32</td>
<td>33.3</td>
<td>33.3</td>
<td>34.2</td>
</tr>
</tbody>
</table>

*Calculated using equation (4)
Finally, in order to provide some preliminary validation of the theory and simulated results presented in this paper, acute in vivo recordings were made from the medial nerve of a Danish Landrace pig. These experiments were part of a larger study and the detailed description is given elsewhere [10]. The set-up consisted of an 11-electrode MEC (i.e. N = 9) and a tripolar stimulating cuff and the data was captured processed using MATLAB in the same manner as the simulated data reported above. Fig 5 shows the BPFVS for four 8th-order Butterworth digital BPFs with centre frequencies (f_v) of (a) 4 kHz, (b) 8 kHz, (c) 10 kHz and (d) 16 kHz. The Q_v values of the output corresponding to the fast fibre population (approx 60 m/s) are 1.6, 3.3, 4.6 and 6.5. The output of the population at about 30 m/s is clearly visible. The vertical arrows also indicate the appearance of other populations (e.g. 38 m/s, 44 m/s approx.) as the selectivity is increased. The presence of images can also be noted, at low velocities (i.e. < 30 m/s), dependent on f_o.

### Table 3

Simulated maximum available velocity selectivity (Q_v) as a function of signal-to-noise ratio for a 9-tripole system. The input is an SFAP propagating at 30 m/s and the limiting resolution is 10-bits.

<table>
<thead>
<tr>
<th>SNR</th>
<th>1 kHz</th>
<th>10 kHz</th>
<th>100 kHz</th>
</tr>
</thead>
<tbody>
<tr>
<td>TMAP1</td>
<td>A</td>
<td>B</td>
<td>C</td>
</tr>
<tr>
<td>4 kHz</td>
<td>2.9</td>
<td>1</td>
<td>8 kHz</td>
</tr>
<tr>
<td>TMAP2</td>
<td>16 kHz</td>
<td>12.5</td>
<td>3.5</td>
</tr>
</tbody>
</table>

Column A: maximum available frequency, f_max; column B: resulting maximum velocity selectivity; column C: velocity selectivity enhancement compared to IVS.

*limited by analogue bandwidth (32 kHz)

### References