Coupling between positronium formation and elastic positron scattering channels in the rare gases

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Abstract

Measurements of elastic scattering cross sections are presented for positron collisions with helium, neon, argon, krypton and xenon around the threshold energy for positronium (Ps) formation. The elastic cross section falls slowly with increasing energy above the Ps formation threshold in helium and neon, whereas in argon, krypton and xenon it exhibits an increase which appears both more prominent and more sustained as the atomic number of the gas increases. It is proposed that this coupling is a result of an intermediate virtual Ps state which enhances branching into the (atom plus positron) final state.

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I. INTRODUCTION

There have been many experimental studies of positron-atom scattering cross sections for collisions involving elastic scattering and the first inelastic process, involving the formation of positronium (Ps), the electron-positron bound state.\textsuperscript{1,2} Of particular interest in recent years has been the possibility of coupling between the cross sections for these two processes immediately above the threshold for Ps formation ($E_{Ps}$, which is 6.8 eV – the ground-state Ps binding energy – below the first ionization potential $E_{ion}$).

It is difficult to calculate the two cross sections in the energy range from $E_{Ps}$ to $E_{ion}$ and theorists have taken the approach of subtracting experimental Ps formation cross sections ($Q_{Ps}$) from total cross sections ($Q_{tot}$), often measured at different times and with different apparatus. Following the early work of Campeanu et al.,\textsuperscript{3} Laricchia and co-workers published a series of papers combining theory and experiment in which the elastic cross section $Q_{el}$ exhibited a cusp-like behavior on positron energy around $E_{Ps}$,\textsuperscript{4} which generally falls with increasing energy above $E_{Ps}$ – an effect which is very small for He but which increases in magnitude as the atomic number of the scattering gas species increases.

Two experimental studies of positron-helium scattering have suggested that no cusp is observable (in agreement with ref. 4),\textsuperscript{5,6} but recently Coleman et al.\textsuperscript{7} found a significant upward step in $Q_{el}$ in xenon at $E_{Ps}$, and a possible smaller effect in argon. This result was attributed to the enhancement of the elastic scattering channel by the existence of an intermediate (positron + atom) state which proceeds either to (ion + Ps) or (positron + atom) final states – the latter being influenced by the former. Their results suggested that in the first 0.5 eV or so above $E_{Ps}$, most of the increase seen in $Q_{tot}$ for xenon was in fact associated with an increase in $Q_{el}$ rather than with the onset of real Ps formation. The reader is referred to ref. 7 for a fuller discussion of earlier work on this problem.

The aim of the work presented here is to investigate the extent of channel coupling at $E_{Ps}$ for all five stable noble gases, primarily to investigate the dependence of the energy dependence of $Q_{el}$ at $E_{Ps}$ on atomic number. This work was encouraged
by preliminary data for neon from Buckman et al.,\textsuperscript{8} which suggested that a small change in neon could be seen at $E_{Ps}$ (i.e., lying between the earlier null result for helium and the small result of ref. 7 for argon).

II. EXPERIMENTAL DETAILS

A schematic of the apparatus is shown in Fig. 1. Basic experimental details were given in ref. 7 and so the modified system will only be summarized here. A 115 MBq $^{22}$Na source capsule is positioned 1mm from the moderator assembly, comprising two 4mm-diameter well-annealed 50%-transmission tungsten meshes held at a potential $V_{M}$, which determines the positron beam energy. $(V_{M}+2)$ V is applied to a double 92% tungsten mesh placed immediately in front of the moderator meshes to (a) decrease the energy spread (to $\sim$0.5 eV FWHM) and the angular divergence of the positron beam, and (b) to reflect any backward-scattered positrons towards the detector. The slow positrons are guided by a 5mT axial magnetic field through the 7cm-long gas cell and a further 25cm through vacuum, via a cylindrical-geometry retarding field analyzer (RFA) to the channel electron multiplier (CEM) detector, whose output pulses are counted by a multi-channel scaler (MCS). A potential $V_{R}$ is applied to the RFA, which stops positrons with axial momenta less than $(2meV_{R})^{1/2}$ after deflection and/or energy loss in the gas cell. With $V_{R} = (V_{M} + 1.5)$ V only essentially unscattered positrons are transmitted through the RFA. The relative sizes of the diameters of the incident beam, holes in the gas cell exit plate and RFA tube were chosen such that essentially all positrons scattered through any angle could be constrained to helical paths which ended on the CEM detector.

The beam attenuation $A$ was measured with $V_{R} = 0$ and $(V_{M} + 1.5)$ V with vacuum and gas in the cell, for incident positron energies from 4eV below to 4eV above $E_{Ps}$ in helium, neon, argon, krypton and xenon. The gas densities were kept low enough so that $A$ was less than $\sim$ 15%, to reduce the probability of multiple scattering in the cell. By increasing $V_{R}$ to $(V_{M} + 10)$ V the background count rate could be measured. Signal count rates were recorded by the MCS for each incident positron energy $E$, which was
stepped automatically from \((E_{Ps}-4)\) to \((E_{Ps}+4)\) eV by controlling the moderator potential \(V_M\) using the MCS ramp output.

\(A_{Ps}\), the attenuation due only to Ps formation, was measured by comparing signal vacuum and gas count rates with \(V_R = 0\) V, and the total attenuation \(A_T\) due to all scattering events, was measured with \(V_R = (V_M + 1.5)\) V. Angular discrimination for elastic scattering ranged from approximately 23º at 2eV to 7º at 22eV.

The detection of ions resulting from Ps formation would reduce the measured \(A_{Ps}\) and therefore increase the deduced values of \(Q_{el}\) above \(E_{Ps}\). Measurements of \(A_{Ps}\) were consequently also made with \(V_R = 0.75\) V, to stop any ions which may have been otherwise guided to the CEM following Ps formation. It was found that this small positive potential was sufficient to prevent ion detection (the probability of which was found to decrease with the atomic number of the target atoms) and did not significantly affect the results presented. Ion detection can therefore be eliminated as a possible source of systematic error in these experiments.

\(Q_{el}\) is then given by \(\{\ln[(1-A_T)/(1-A_{Ps})]\}/nL\), where \(n\) is the gas density and \(L\) the effective length of the gas cell. \(nL\) was found using measured values of \(A_T\) and \(A_{Ps}\) and previously measured values of \(Q_T\) and \(Q_{Ps}\) for the five gases studied, as the energy dependence of \(Q_{el}\), rather than its absolute value, was the focus of the present work.

### III. RESULTS AND DISCUSSION

The results for all five rare gases are shown in Fig. 2. Apart from the 2009 Bath results for Ar and Xe\(^7\) the only other experimental results for \(Q_{el}\) in these gases are the early work of Coleman et al.\(^6\) and the recent measurements for He of Caradonna et al.\(^5\) Preliminary results for \(Q_{el}\) for Ne from the ANU group, as yet unpublished, appear similar to those shown in Fig. 2.\(^8\) Selected earlier absolute measurements of \(Q_T\) are shown for He, Ne and Kr\(^5,9,10\); the Ar results are shown alongside those of ref. 7, which were normalized using the \(Q_T\) values of Karwasz et al.\(^11\) For Xe the disagreement between published \(Q_T\) values is so great that the current measurements were normalized using as a guide the values of ref. 12 below \(E_{Ps}\) and the \(Q_{Ps}\) values reported in ref. 13 above \(E_{Ps}\).
The results all show a change in $Q_{\text{el}}$ at $E_{\text{Ps}}$. In He and Ne this change can be described as a small – but there is an indication in both gases that $Q_{\text{el}}$ exhibits a broad peak extending over several eV. In both gases this may be regarded as a reduction above $E_{\text{Ps}}$ in the small positive slope in $Q_{\text{el}}(E)$, which is more prominent in Ne as there is a more prominent upward trend in $Q_{\text{el}}$ below $E_{\text{Ps}}$ in this gas. These features are not dissimilar to the cusp-like features at $E_{\text{Ps}}$ discussed by Meyerhof and Laricchia,\textsuperscript{4} except that the data indicate that the cusp-like feature is peaked at 1 eV or so above $E_{\text{Ps}}$, especially in He.

The data for Ar reproduce well our 2009 results near $E_{\text{Ps}}$, with a small but pronounced peak in $Q_{\text{el}}$ occurring at $\sim$ 1 eV above $E_{\text{Ps}}$. This difference is too large to be explained by incorrect assignment of positron energy, and indicates that, although cusp-like in shape, $Q_{\text{el}}(E)$ is does not have the expected maximum at $E_{\text{Ps}}$. The broad peak can instead be thought of as an enhancement of $Q_{\text{el}}$ in the energy region between $E_{\text{Ps}}$ and the direct ionization threshold $E_{\text{ion}}$, 6.8 eV higher.

This enhancement becomes more pronounced in Kr and Xe. While giving the impression of increasing in a step-wise fashion above $E_{\text{Ps}}$, the increase may also be considered to be an enhancement between $E_{\text{Ps}}$ and $E_{\text{ion}}$, especially if the underlying trend in $Q_{\text{el}}$ is a slow increase with increasing energy.

While not showing the predicted cusp-like behavior, the increase in the strength of coupling between $Q_{\text{el}}$ and $Q_{\text{Ps}}$ above $E_{\text{Ps}}$ with the atomic number of the target atom is evident. The cusps predicted in refs. 4 and 14 are stronger when $Q_{\text{el}}$ increases more prominently with positron energy below $E_{\text{Ps}}$, and this happens for the heavier gases. Meyerhof, Laricchia and co-workers\textsuperscript{4} studied the coupling in terms of the angular momenta of the initial and final states. Whereas the present measurements do not completely rule out this possibility, there would appear to be a second, stronger coupling which – in the heavier gases at least – which outweighs any cusp-like behavior. We propose that the enhancement of $Q_{\text{el}}$ between $E_{\text{Ps}}$ and $E_{\text{ion}}$ is a result of the existence of an intermediate positron-atom state in this energy region. Here the incident positrons do not have enough energy to eject a free electron from the atom, but can leave in the bound Ps state. The possibility of Ps formation strengthens the
positron-atom interaction and consequently increases the possibility of branching into both final (positron + atom) or (Ps + ion) states. Thus both $Q_{el}$ and $Q_{Ps}$ increase above $E_{Ps}$. We suggest that the enhancement of $Q_{el}$ is most marked just above $E_{Ps}$, and as $E$ increases towards $E_{ion}$ the branching into the two final states progressively favors Ps formation.

It is interesting to note that Weber et al.\textsuperscript{14} observed elastic scattering of Ps from a LiF surface when only inelastic scattering was expected; they concluded that the imaginary part of the scattering potential, which mimics the inelastic channel, leads to much more elastic scattering than would be obtained from the real part of the potential by itself – implying that, in the present experiment, the onset of inelastic scattering would enhance the elastic scattering probability.

The question remains as to why the enhancement of $Q_{el}$ becomes more pronounced with atomic number. One possible explanation is that if the intermediate state contains more electrons (rising from 2 for He to 54 for Xe) then the probability of branching into the (Ps + ion) final state is reduced by the increased screening of the positron-electron interaction by the other electrons in the atom. This highly speculative proposal is clearly in need of careful theoretical consideration.

**IV. CONCLUSIONS**

The present experimental results confirm that there is coupling between elastic scattering and Ps formation above the Ps threshold energy, but that the most significant feature resulting from this coupling – at least in the heavier gases (Ar, Kr and Xe) is not the expected cusp in $Q_{el}$ at $E_{Ps}$, but instead an increase in $Q_{el}$ from $E_{Ps}$ to about ($E_{Ps} +1$) eV – above which it falls again or levels out. This enhancement in $Q_{el}$ may result from a strengthening of the positron-atom interaction via a ‘virtual Ps’ intermediate state. The increasing prominence of the enhancement of $Q_{el}$ above $E_{Ps}$ in the heavier gases mimics the behavior predicted for the cusp, but a full understanding would require further theoretical research. It is hoped that these measurements will stimulate further experiments and calculations in the interesting –
and unique – energy range between the first inelastic thresholds for positron scattering.

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8 S.J. Buckman, private communication.
A 50, 3129 (1994).

Figure captions

**Fig. 1.** Schematic diagram of the apparatus. $S = ^{22}\text{Na}$ source capsule, $V_M =$ potential applied to moderator, RFA = tube retarding field analyzer, CEM = channel electron multiplier. Source-CEM distance ~ 400mm.

**Fig. 2.** Total (white circles) and elastic (black circles) cross sections for positron scattering by He, Ne, Ar, Kr and Xe. Open triangles: earlier absolute total cross sections for He,$^5$ Ne,$^9$ Ar$^{11}$ and Kr.$^{10}$ White squares: $Q_{el}$ for He from ref. 5. Gray circles and squares: 2009 results of Coleman et al. for $Q_{el}$ and $Q_{T}$ for Ar and Xe.$^7$
gas cell

$V_M, V_M+2V$

e$

gas cell

axial magnetic field

$V_M, V_M+1.5V, V_M+10V$

RFA

vacuum

CEM

Figure 1
Figure 2